

Chapter 10, Problem 1.

Determine i in the circuit of Fig. 10.50.

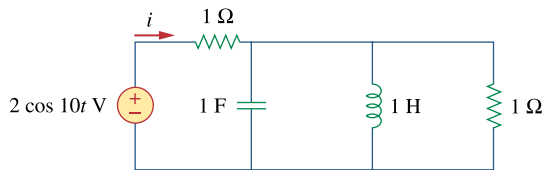


Figure 10.50

For Prob. 10.1.

Chapter 10, Solution 1.

We first determine the input impedance.

$$1\text{H} \longrightarrow j\omega L = j1 \times 10 = j10$$

$$1\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j10 \times 1} = -j0.1$$

$$Z_{in} = 1 + \left(\frac{1}{j10} + \frac{1}{-j0.1} + \frac{1}{1} \right)^{-1} = 1.0101 - j0.1 = 1.015 \angle -5.653^\circ$$

$$I = \frac{2 \angle 0^\circ}{1.015 \angle -5.653^\circ} = 1.9704 \angle 5.653^\circ$$

$$i(t) = \underline{1.9704 \cos(10t + 5.653^\circ) \text{ A}} = \underline{1.9704 \cos(10t + 5.65^\circ) \text{ A}}$$

Chapter 10, Problem 2.

Solve for V_o in Fig. 10.51, using nodal analysis.

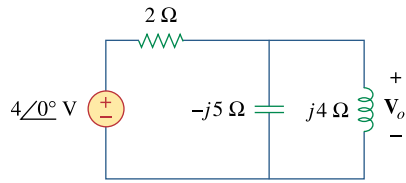
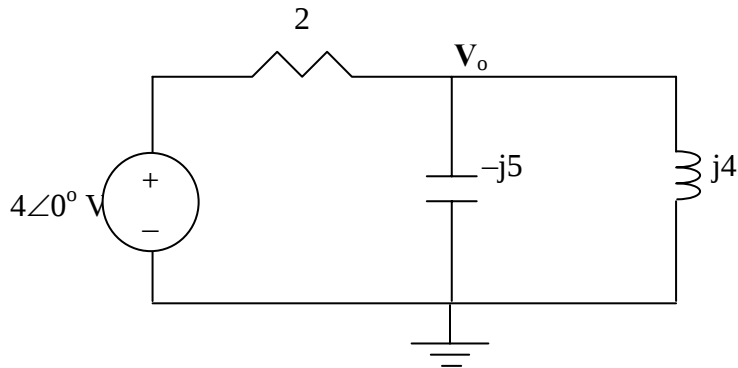


Figure 10.51
For Prob. 10.2.

Chapter 10, Solution 2.

Consider the circuit shown below.



At the main node,

$$\frac{4 - V_o}{2} = \frac{V_o}{-j5} + \frac{V_o}{j4} \longrightarrow 40 = V_o(10 + j)$$

$$V_o = \frac{40}{10 - j} = \underline{3.98 \angle 5.71^\circ \text{ A}}$$

Chapter 10, Problem 3.

Determine v_o in the circuit of Fig. 10.52.

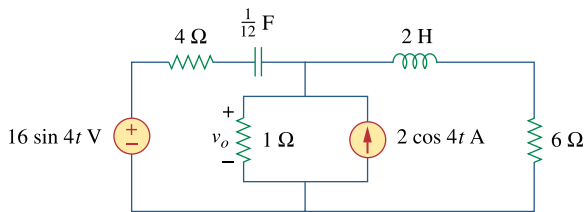


Figure 10.52

For Prob. 10.3.

Chapter 10, Solution 3.

$$\omega = 4$$

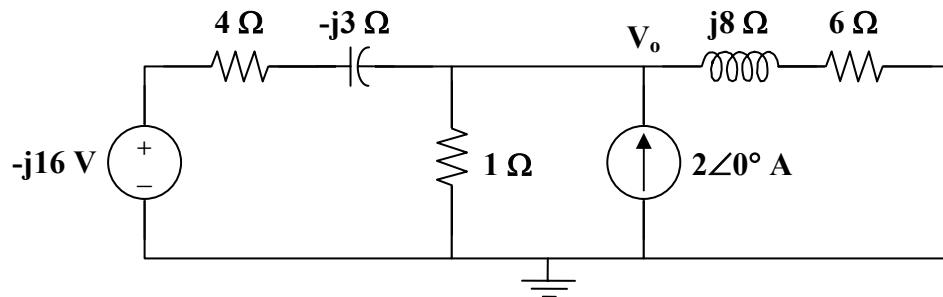
$$2 \cos(4t) \longrightarrow 2 \angle 0^\circ$$

$$16 \sin(4t) \longrightarrow 16 \angle -90^\circ = -j16$$

$$2 \text{ H} \longrightarrow j\omega L = j8$$

$$1/12 \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(4)(1/12)} = -j3$$

The circuit is shown below.



Applying nodal analysis,

$$\frac{-j16 - V_o}{4 - j3} + 2 = \frac{V_o}{1} + \frac{V_o}{6 + j8}$$

$$\frac{-j16}{4 - j3} + 2 = \left(1 + \frac{1}{4 - j3} + \frac{1}{6 + j8}\right) V_o$$

$$V_o = \frac{3.92 - j2.56}{1.22 + j0.04} = \frac{4.682 \angle -33.15^\circ}{1.2207 \angle 1.88^\circ} = 3.835 \angle -35.02^\circ$$

Therefore, $v_o(t) = \underline{\underline{3.835 \cos(4t - 35.02^\circ) \text{ V}}}$

Chapter 10, Problem 4.

Determine i_1 in the circuit of Fig. 10.53.

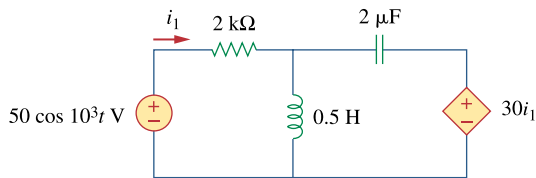


Figure 10.53

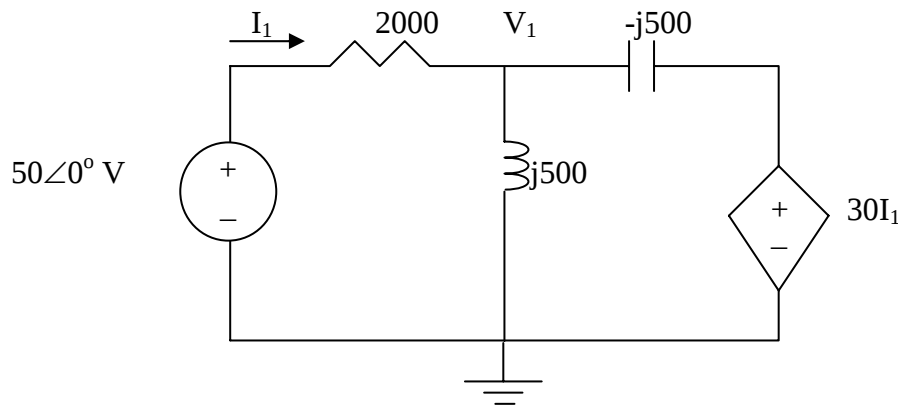
For Prob. 10.4.

Chapter 10, Solution 4.

$$0.5\text{ H} \longrightarrow j\omega L = j0.5 \times 10^3 = j500$$

$$2\text{ }\mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j10^3 \times 2 \times 10^{-6}} = -j500$$

Consider the circuit as shown below.



At node 1,

$$\frac{50 - V_1}{2000} + \frac{30I_1 - V_1}{-j500} = \frac{V_1}{j500}$$

$$\text{But } I_1 = \frac{50 - V_1}{2000}$$

$$50 - V_1 + j4 \times 30 \left(\frac{50 - V_1}{2000} \right) + j4V_1 - j4V_1 = 0 \quad \rightarrow \quad V_1 = 50$$

$$I_1 = \frac{50 - V_1}{2000} = 0$$

$$i_1(t) = \underline{0\text{ A}}$$

Chapter 10, Problem 5.



Find i_o in the circuit of Fig. 10.54.

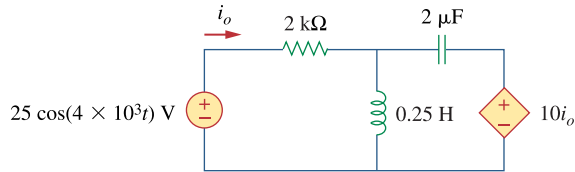


Figure 10.54

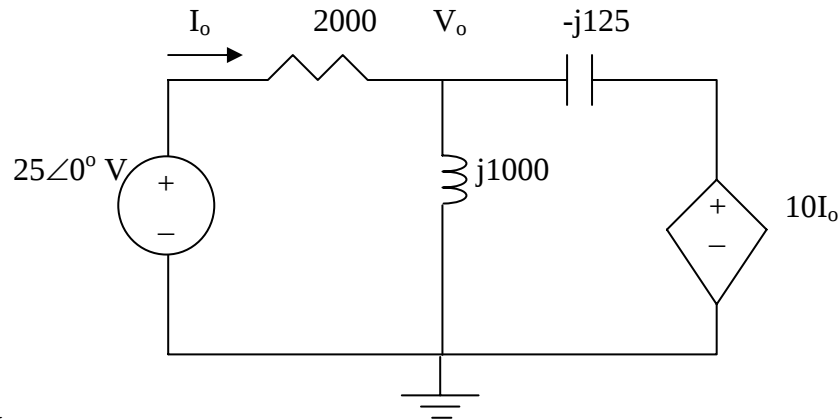
For Prob. 10.5.

Chapter 10, Solution 5.

$$0.25H \longrightarrow j\omega L = j0.25 \times 4 \times 10^3 = j1000$$

$$2\mu F \longrightarrow \frac{1}{j\omega C} = \frac{1}{j4 \times 10^3 \times 2 \times 10^{-6}} = -j125$$

Consider the circuit as shown below.



At node V_o ,

$$\frac{V_o - 25}{2000} + \frac{V_o - 0}{j1000} + \frac{V_o - 10I_o}{-j125} = 0$$

$$V_o - 25 - j2V_o + j16V_o - j160I_o = 0$$

$$(1 + j14)V_o - j160I_o = 25$$

But $I_o = (25 - V_o)/2000$

$$(1 + j14)V_o - j2 + j0.08V_o = 25$$

$$V_o = \frac{25 + j2}{1 + j14.08} = \frac{25.08 \angle 4.57^\circ}{14.115 \angle 58.94^\circ} = 1.7768 \angle -81.37^\circ$$

Now to solve for i_o ,

$$\begin{aligned} I_o &= \frac{25 - V_o}{2000} = \frac{25 - 0.2666 + j1.7567}{2000} = 12.367 + j0.8784 \text{ mA} \\ &= 12.398 \angle 4.06^\circ \end{aligned}$$

$$i_o = \underline{\underline{12.398 \cos(4 \times 10^3 t + 4.06^\circ) \text{ mA}}}$$

Chapter 10, Problem 6.

Determine V_x in Fig. 10.55.

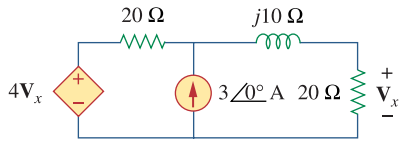


Figure 10.55
For Prob. 10.6.

Chapter 10, Solution 6.

Let V_o be the voltage across the current source. Using nodal analysis we get:

$$\frac{V_o - 4V_x}{20} - 3 + \frac{V_o}{20 + j10} = 0 \quad \text{where} \quad V_x = \frac{20}{20 + j10} V_o$$

Combining these we get:

$$\frac{V_o}{20} - \frac{4V_o}{20 + j10} - 3 + \frac{V_o}{20 + j10} = 0 \rightarrow (1 + j0.5 - 3)V_o = 60 + j30$$

$$V_o = \frac{60 + j30}{-2 + j0.5} \quad \text{or} \quad V_x = \frac{20(3)}{-2 + j0.5} = \underline{\underline{29.11 \angle -166^\circ \text{ V}}}.$$

Chapter 10, Problem 7.

Use nodal analysis to find V in the circuit of Fig. 10.56.

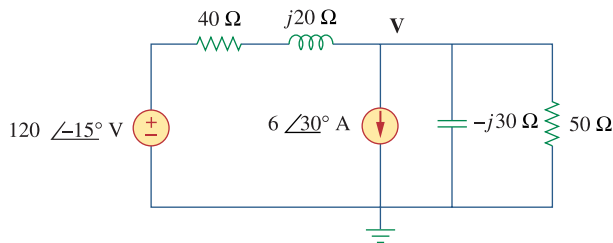


Figure 10.56
For Prob. 10.7.

Chapter 10, Solution 7.

At the main node,

$$\frac{120\angle -15^\circ - V}{40 + j20} = 6\angle 30^\circ + \frac{V}{-j30} + \frac{V}{50} \longrightarrow \frac{115.91 - j31.058}{40 + j20} - 5.196 - j3 =$$

$$V \left(\frac{1}{40 + j20} + \frac{j}{30} + \frac{1}{50} \right)$$

$$V = \frac{-3.1885 - j4.7805}{0.04 + j0.0233} = \underline{124.08\angle -154^\circ \text{ V}}$$

Chapter 10, Problem 8.



Use nodal analysis to find current i_o in the circuit of Fig. 10.57. Let

$$i_s = 6 \cos(200t + 15^\circ) \text{ A.}$$

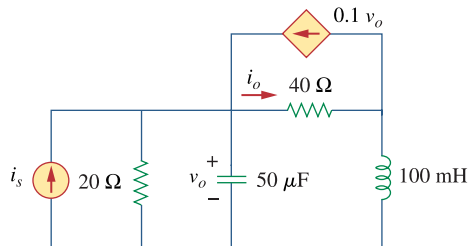


Figure 10.57

For Prob. 10.8.

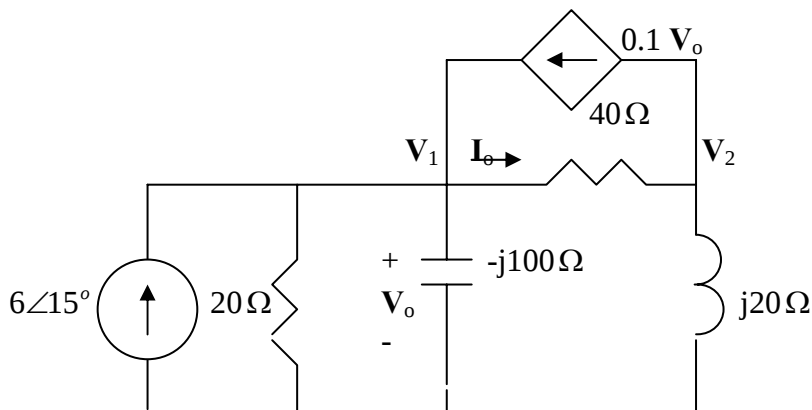
Chapter 10, Solution 8.

$$\omega = 200,$$

$$100\text{mH} \longrightarrow j\omega L = j200 \times 0.1 = j20$$

$$50\mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j200 \times 50 \times 10^{-6}} = -j100$$

The frequency-domain version of the circuit is shown below.



At node 1,

$$6\angle 15^\circ + 0.1V_1 = \frac{V_1}{20} + \frac{V_1}{-j100} + \frac{V_1 - V_2}{40}$$

$$\text{or} \quad 5.7955 + j1.5529 = (-0.025 + j0.01)V_1 - 0.025V_2 \quad (1)$$

At node 2,

$$\frac{V_1 - V_2}{40} = 0.1V_1 + \frac{V_2}{j20} \quad \longrightarrow \quad 0 = 3V_1 + (1 - j2)V_2 \quad (2)$$

From (1) and (2),

$$\begin{bmatrix} (-0.025 + j0.01) & -0.025 \\ 3 & (1 - j2) \end{bmatrix} \begin{pmatrix} V_1 \\ V_2 \end{pmatrix} = \begin{pmatrix} (5.7955 + j1.5529) \\ 0 \end{pmatrix} \quad \text{or} \quad AV = B$$

Using MATLAB,

$$V = \text{inv}(A)*B$$

leads to $V_1 = -70.63 - j127.23$, $V_2 = -110.3 + j161.09$

$$I_o = \frac{V_1 - V_2}{40} = 7.276\angle -82.17^\circ$$

Thus,

$$\underline{i_o(t) = 7.276 \cos(200t - 82.17^\circ) \text{ A}}$$

Chapter 10, Problem 9.



Use nodal analysis to find v_o in the circuit of Fig. 10.58.

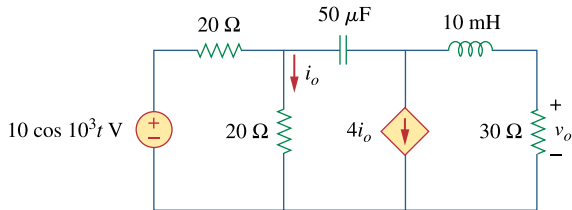


Figure 10.58

For Prob. 10.9.

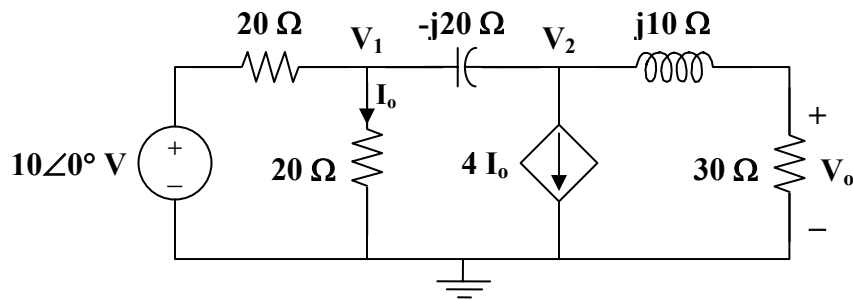
Chapter 10, Solution 9.

$$10 \cos(10^3 t) \longrightarrow 10 \angle 0^\circ, \quad \omega = 10^3$$

$$10 \text{ mH} \longrightarrow j\omega L = j10$$

$$50 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10^3)(50 \times 10^{-6})} = -j20$$

Consider the circuit shown below.



At node 1,

$$\begin{aligned} \frac{10 - V_1}{20} &= \frac{V_1}{20} + \frac{V_1 - V_2}{-j20} \\ 10 &= (2 + j)V_1 - jV_2 \end{aligned} \quad (1)$$

At node 2,

$$\begin{aligned} \frac{V_1 - V_2}{-j20} &= (4) \frac{V_1}{20} + \frac{V_2}{30 + j10}, \text{ where } I_o = \frac{V_1}{20} \text{ has been substituted.} \\ (-4 + j)V_1 &= (0.6 + j0.8)V_2 \\ V_1 &= \frac{0.6 + j0.8}{-4 + j} V_2 \end{aligned} \quad (2)$$

Substituting (2) into (1)

$$10 = \frac{(2 + j)(0.6 + j0.8)}{-4 + j} V_2 - jV_2$$

or

$$V_2 = \frac{170}{0.6 - j26.2}$$

$$V_o = \frac{30}{30 + j10} V_2 = \frac{3}{3 + j} \cdot \frac{170}{0.6 - j26.2} = 6.154 \angle 70.26^\circ$$

Therefore,

$$v_o(t) = \underline{\underline{6.154 \cos(10^3 t + 70.26^\circ) \text{ V}}}$$

Chapter 10, Problem 10.



Use nodal analysis to find v_o in the circuit of Fig. 10.59. Let $\omega = 2 \text{ krad/s}$.

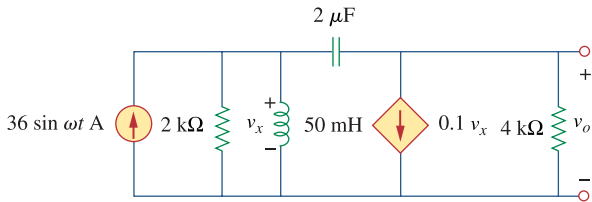


Figure 10.59

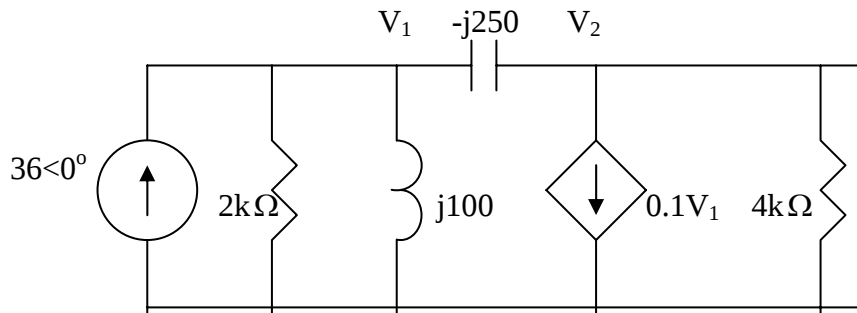
For Prob. 10.10.

Chapter 10, Solution 10.

$$50 \text{ mH} \longrightarrow j\omega L = j2000 \times 50 \times 10^{-3} = j100, \quad \omega = 2000$$

$$2 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j2000 \times 2 \times 10^{-6}} = -j250$$

Consider the frequency-domain equivalent circuit below.



At node 1,

$$36 = \frac{V_1}{2000} + \frac{V_1}{j100} + \frac{V_1 - V_2}{-j250} \longrightarrow 36 = (0.0005 - j0.006)V_1 - j0.004V_2 \quad (1)$$

At node 2,

$$\frac{V_1 - V_2}{-j250} = 0.1V_1 + \frac{V_2}{4000} \longrightarrow 0 = (0.1 - j0.004)V_1 + (0.00025 + j0.004)V_2 \quad (2)$$

Solving (1) and (2) gives

$$V_o = V_2 = -535.6 + j893.5 = 8951.1 \angle 93.43^\circ$$

$$v_o(t) = \underline{\underline{8.951 \sin(2000t + 93.43^\circ) \text{ kV}}}$$

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Chapter 10, Problem 11.



Apply nodal analysis to the circuit in Fig. 10.60 and determine $\mathbf{I}_o$.

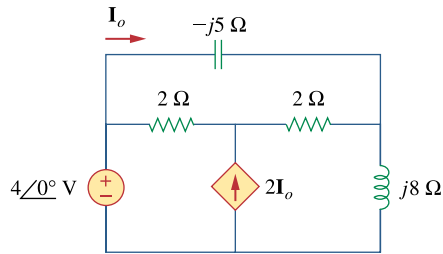
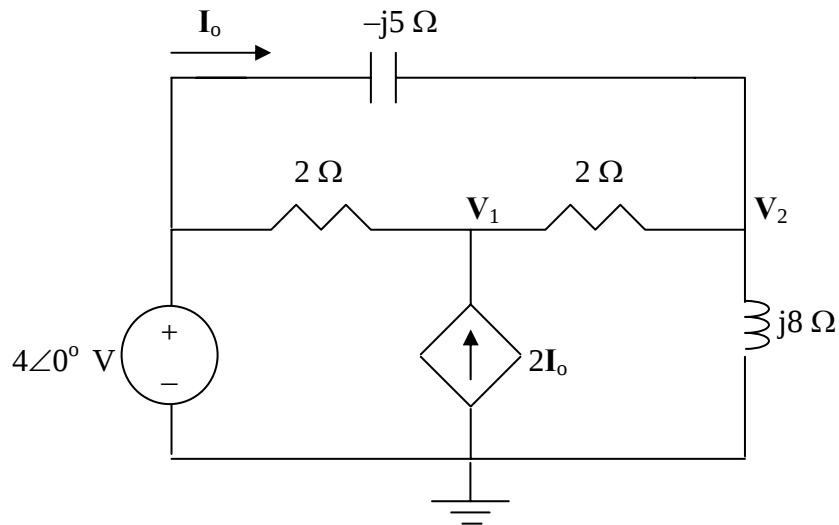


Figure 10.60

For Prob. 10.11.

Chapter 10, Solution 11.

Consider the circuit as shown below.



At node 1,

$$\frac{V_1 - 4}{2} - 2I_o + \frac{V_1 - V_2}{2} = 0$$
$$V_1 - 0.5V_2 - 2I_o = 2$$

$$\text{But, } I_o = (4 - V_2)/(-j5) = -j0.2V_2 + j0.8$$

Now the first node equation becomes,

$$V_1 - 0.5V_2 + j0.4V_2 - j1.6 = 2 \text{ or}$$
$$V_1 + (-0.5 + j0.4)V_2 = 2 + j1.6$$

At node 2,

$$\frac{V_2 - V_1}{2} + \frac{V_2 - 4}{-j5} + \frac{V_2 - 0}{j8} = 0$$
$$-0.5V_1 + (0.5 + j0.075)V_2 = j0.8$$

Using MATLAB to solve this, we get,

$$>> Y = [1, (-0.5 + 0.4i); -0.5, (0.5 + 0.075i)]$$

$$Y =$$

$$\begin{array}{cc} 1.0000 & -0.5000 + 0.4000i \\ -0.5000 & 0.5000 + 0.0750i \end{array}$$

$$>> I = [(2 + 1.6i); 0.8i]$$

$$I =$$

$$\begin{array}{c} 2.0000 + 1.6000i \\ 0 + 0.8000i \end{array}$$

$$>> V = \text{inv}(Y) * I$$

$$V =$$

$$\begin{array}{c} 4.8597 + 0.0543i \\ 4.9955 + 0.9050i \end{array}$$

$$I_o = -j0.2V_2 + j0.8 = -j0.9992 + 0.01086 + j0.8 = 0.01086 - j0.1992$$

$$= \underline{\underline{199.5 \angle 86.89^\circ \text{ mA}}}.$$

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Chapter 10, Problem 12.



By nodal analysis, find i_o in the circuit of Fig. 10.61.

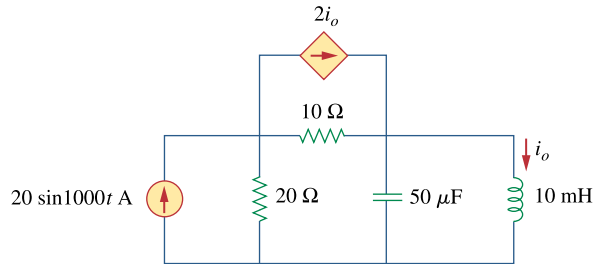


Figure 10.61

For Prob. 10.12.

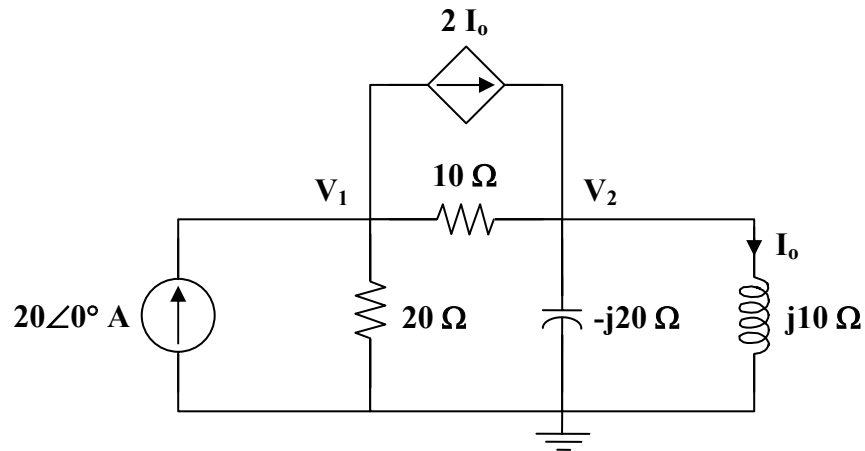
Chapter 10, Solution 12.

$$20 \sin(1000t) \longrightarrow 20 \angle 0^\circ, \quad \omega = 1000$$

$$10 \text{ mH} \longrightarrow j\omega L = j10$$

$$50 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10^3)(50 \times 10^{-6})} = -j20$$

The frequency-domain equivalent circuit is shown below.



At node 1,

$$20 = 2\mathbf{I}_o + \frac{\mathbf{V}_1}{20} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{10}, \quad \text{where}$$

$$\mathbf{I}_o = \frac{\mathbf{V}_2}{j10}$$

$$20 = \frac{2\mathbf{V}_2}{j10} + \frac{\mathbf{V}_1}{20} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{10}$$

$$400 = 3\mathbf{V}_1 - (2 + j4)\mathbf{V}_2 \quad (1)$$

At node 2,

$$\frac{2\mathbf{V}_2}{j10} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{10} = \frac{\mathbf{V}_2}{-j20} + \frac{\mathbf{V}_2}{j10}$$

$$j2\mathbf{V}_1 = (-3 + j2)\mathbf{V}_2$$

or

$$\mathbf{V}_1 = (1 + j1.5)\mathbf{V}_2 \quad (2)$$

Substituting (2) into (1),

$$400 = (3 + j4.5)\mathbf{V}_2 - (2 + j4)\mathbf{V}_2 = (1 + j0.5)\mathbf{V}_2$$

$$\mathbf{V}_2 = \frac{400}{1 + j0.5}$$

$$\mathbf{I}_o = \frac{\mathbf{V}_2}{j10} = \frac{40}{j(1 + j0.5)} = 35.74 \angle -116.6^\circ$$

Therefore, $i_o(t) = \underline{\underline{35.74 \sin(1000t - 116.6^\circ) \text{ A}}}$

Chapter 10, Problem 13.



Determine V_x in the circuit of Fig. 10.62 using any method of your choice.

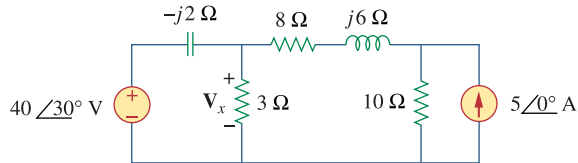
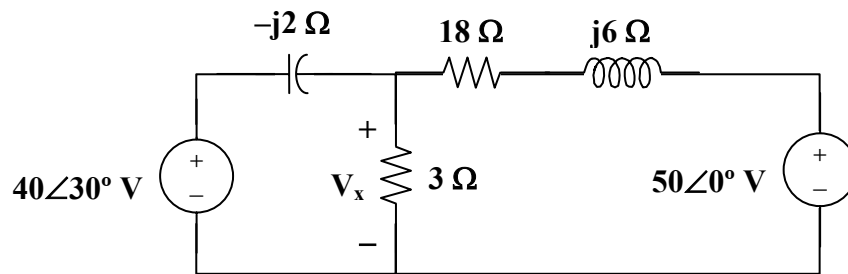


Figure 10.62

For Prob. 10.13.

Chapter 10, Solution 13.

Nodal analysis is the best approach to use on this problem. We can make our work easier by doing a source transformation on the right hand side of the circuit.



$$\frac{V_x - 40\angle 30^\circ}{-j2} + \frac{V_x}{3} + \frac{V_x - 50}{18 + j6} = 0$$

which leads to $V_x = \underline{29.36\angle 62.88^\circ \text{ A}}$.

Chapter 10, Problem 14.



Calculate the voltage at nodes 1 and 2 in the circuit of Fig. 10.63 using nodal analysis.

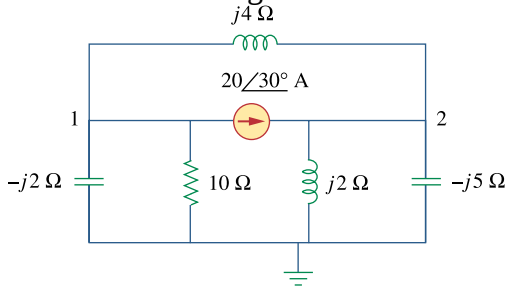


Figure 10.63

For Prob. 10.14.

Chapter 10, Solution 14.

At node 1,

$$\begin{aligned} \frac{0 - V_1}{-j2} + \frac{0 - V_1}{10} + \frac{V_2 - V_1}{j4} &= 20 \angle 30^\circ \\ -(1 + j2.5)V_1 - j2.5V_2 &= 173.2 + j100 \end{aligned} \quad (1)$$

At node 2,

$$\begin{aligned} \frac{V_2}{j2} + \frac{V_2}{-j5} + \frac{V_2 - V_1}{j4} &= 20 \angle 30^\circ \\ -j5.5V_2 + j2.5V_1 &= 173.2 + j100 \end{aligned} \quad (2)$$

Equations (1) and (2) can be cast into matrix form as

$$\begin{bmatrix} 1 + j2.5 & j2.5 \\ j2.5 & -j5.5 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} -200 \angle 30^\circ \\ 200 \angle 30^\circ \end{bmatrix}$$

$$\Delta = \begin{vmatrix} 1 + j2.5 & j2.5 \\ j2.5 & -j5.5 \end{vmatrix} = 20 - j5.5 = 20.74 \angle -15.38^\circ$$

$$\Delta_1 = \begin{vmatrix} -200 \angle 30^\circ & j2.5 \\ 200 \angle 30^\circ & -j5.5 \end{vmatrix} = j3(200 \angle 30^\circ) = 600 \angle 120^\circ$$

$$\Delta_2 = \begin{vmatrix} 1 + j2.5 & -200 \angle 30^\circ \\ j2.5 & 200 \angle 30^\circ \end{vmatrix} = (200 \angle 30^\circ)(1 + j5) = 1020 \angle 108.7^\circ$$

$$V_1 = \frac{\Delta_1}{\Delta} = 28.93 \angle 135.38^\circ$$

$$V_2 = \frac{\Delta_2}{\Delta} = 49.18 \angle 124.08^\circ$$

Chapter 10, Problem 15.



Solve for the current $\mathbf{I}$ in the circuit of Fig. 10.64 using nodal analysis.

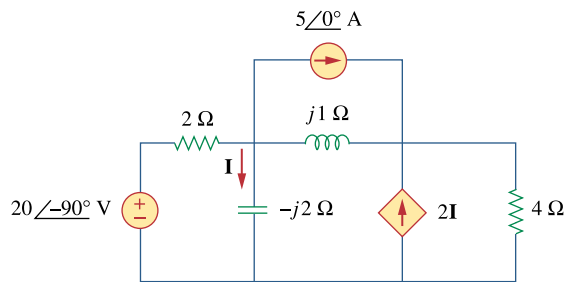
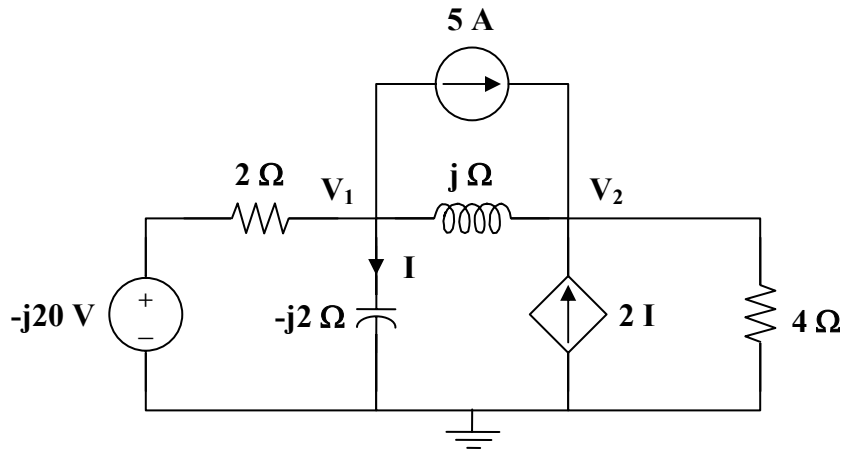


Figure 10.64

For Prob. 10.15.

Chapter 10, Solution 15.

We apply nodal analysis to the circuit shown below.



At node 1,

$$\frac{-j20 - V_1}{2} = 5 + \frac{V_1}{-j2} + \frac{V_1 - V_2}{j}$$

$$-5 - j10 = (0.5 - j0.5)V_1 + jV_2 \quad (1)$$

At node 2,

$$5 + 2I + \frac{V_1 - V_2}{j} = \frac{V_2}{4},$$

$$\text{where } I = \frac{V_1}{-j2}$$

$$V_2 = \frac{5}{0.25 - j} V_1 \quad (2)$$

Substituting (2) into (1),

$$-5 - j10 - \frac{j5}{0.25 - j} = 0.5(1 - j)V_1$$

$$(1 - j)V_1 = -10 - j20 - \frac{j40}{1 - j4}$$

$$(\sqrt{2} \angle -45^\circ)V_1 = -10 - j20 + \frac{160}{17} - \frac{j40}{17}$$

$$V_1 = 15.81 \angle 313.5^\circ$$

$$I = \frac{V_1}{-j2} = (0.5 \angle 90^\circ)(15.81 \angle 313.5^\circ)$$

$$I = \underline{\underline{7.906 \angle 43.49^\circ \text{ A}}}$$

Chapter 10, Problem 16.



Use nodal analysis to find V_x in the circuit shown in Fig. 10.65.

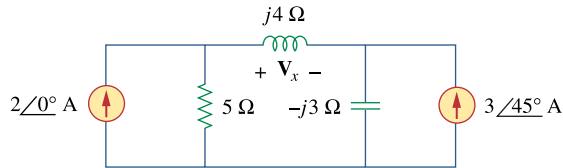
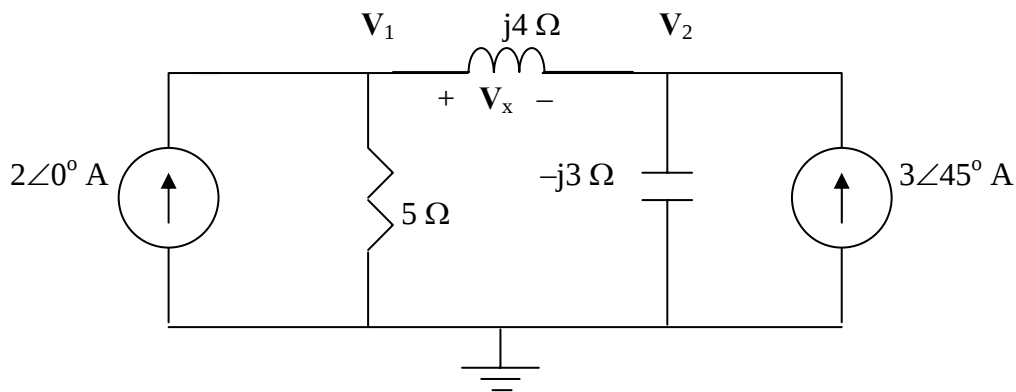


Figure 10.65

For Prob. 10.16.

Chapter 10, Solution 16.

Consider the circuit as shown in the figure below.



At node 1,

$$-2 + \frac{V_1 - 0}{5} + \frac{V_1 - V_2}{j4} = 0 \quad (1)$$

$$(0.2 - j0.25)V_1 + j0.25V_2 = 2$$

At node 2,

$$\frac{V_2 - V_1}{j4} + \frac{V_2 - 0}{-j3} - 3\angle 45^\circ = 0 \quad (2)$$

$$j0.25V_1 + j0.08333V_2 = 2.121 + j2.121$$

In matrix form, (1) and (2) become

$$\begin{bmatrix} 0.2 - j0.25 & j0.25 \\ j0.25 & j0.08333 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} 2 \\ 2.121 + j2.121 \end{bmatrix}$$

Solving this using MATLAB, we get,

```
>> Y=[(0.2-0.25i),0.25i;0.25i,0.08333i]
```

Y =

```
0.2000 - 0.2500i    0 + 0.2500i
0 + 0.2500i    0 + 0.0833i
```

```
>> I=[2;(2.121+2.121i)]
```

I =

```
2.0000
2.1210 + 2.1210i
```

```
>> V=inv(Y)*I
```

V =

```
5.2793 - 5.4190i
9.6145 - 9.1955i
```

$$V_s = V_1 - V_2 = -4.335 + j3.776 = \underline{\underline{5.749\angle 138.94^\circ \text{ V}}}.$$

Chapter 10, Problem 17.



By nodal analysis, obtain current $\mathbf{I}_o$ in the circuit of Fig. 10.66.

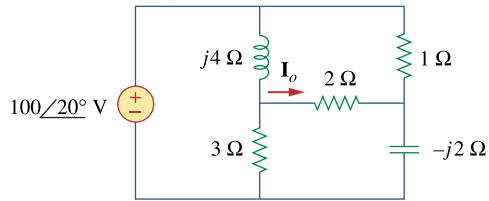
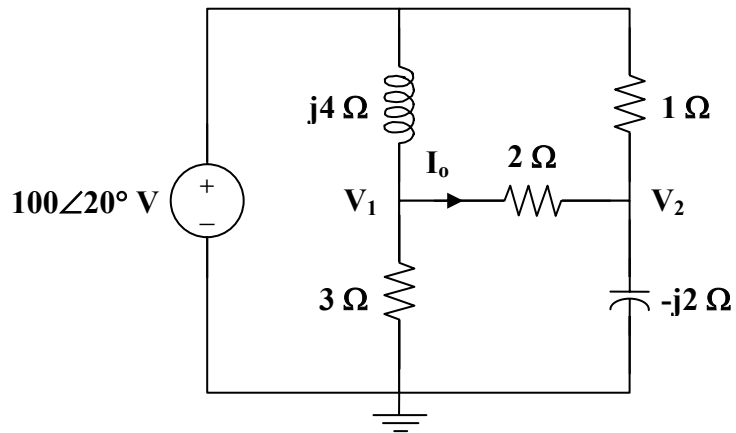


Figure 10.66

For Prob. 10.17.

Chapter 10, Solution 17.

Consider the circuit below.



At node 1,

$$\frac{100\angle 20^\circ - \mathbf{V}_1}{j4} = \frac{\mathbf{V}_1}{3} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{2}$$

$$100\angle 20^\circ = \frac{\mathbf{V}_1}{3}(3 + j10) - j2\mathbf{V}_2$$

(1)

At node 2,

$$\frac{100\angle 20^\circ - \mathbf{V}_2}{1} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{2} = \frac{\mathbf{V}_2}{-j2}$$

$$100\angle 20^\circ = -0.5\mathbf{V}_1 + (1.5 + j0.5)\mathbf{V}_2$$

(2)

From (1) and (2),

$$\begin{bmatrix} 100\angle 20^\circ \\ 100\angle 20^\circ \end{bmatrix} = \begin{bmatrix} -0.5 & 0.5(3 + j) \\ 1 + j10/3 & -j2 \end{bmatrix} \begin{bmatrix} \mathbf{V}_1 \\ \mathbf{V}_2 \end{bmatrix}$$

$$\Delta = \begin{vmatrix} -0.5 & 1.5 + j0.5 \\ 1 + j10/3 & -j2 \end{vmatrix} = 0.1667 - j4.5$$

$$\Delta_1 = \begin{vmatrix} 100\angle 20^\circ & 1.5 + j0.5 \\ 100\angle 20^\circ & -j2 \end{vmatrix} = -55.45 - j286.2$$

$$\Delta_2 = \begin{vmatrix} -0.5 & 100\angle 20^\circ \\ 1 + j10/3 & 100\angle 20^\circ \end{vmatrix} = -26.95 - j364.5$$

$$\mathbf{V}_1 = \frac{\Delta_1}{\Delta} = 64.74\angle -13.08^\circ$$

$$\mathbf{V}_2 = \frac{\Delta_2}{\Delta} = 81.17\angle -6.35^\circ$$

$$\mathbf{I}_o = \frac{\mathbf{V}_1 - \mathbf{V}_2}{2} = \frac{\Delta_1 - \Delta_2}{2\Delta} = \frac{-28.5 + j78.31}{0.3333 - j9}$$

$$\mathbf{I}_o = \underline{\underline{9.25\angle -162.12^\circ \text{ A}}}$$

Chapter 10, Problem 18.



Use nodal analysis to obtain V_o in the circuit of Fig. 10.67 below.

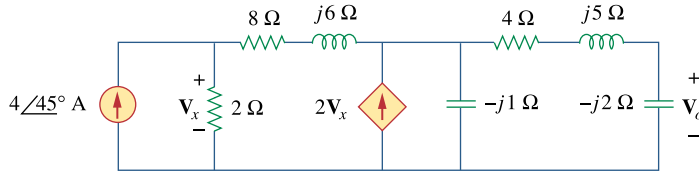
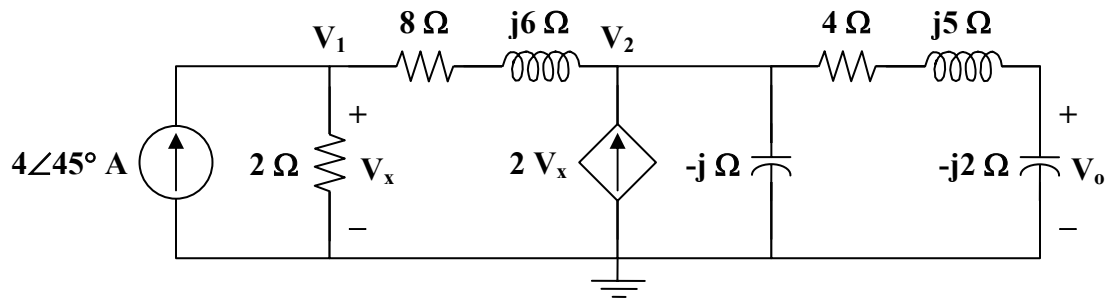


Figure 10.67

For Prob. 10.18.

Chapter 10, Solution 18.

Consider the circuit shown below.



At node 1,

$$4\angle 45^\circ = \frac{\mathbf{V}_1}{2} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{8 + j6}$$
$$200\angle 45^\circ = (29 - j3)\mathbf{V}_1 - (4 - j3)\mathbf{V}_2$$

(1)

At node 2,

$$\frac{\mathbf{V}_1 - \mathbf{V}_2}{8 + j6} + 2\mathbf{V}_x = \frac{\mathbf{V}_2}{-j} + \frac{\mathbf{V}_2}{4 + j5 - j2}, \quad \text{where } \mathbf{V}_x = \mathbf{V}_1$$
$$(104 - j3)\mathbf{V}_1 = (12 + j41)\mathbf{V}_2$$
$$\mathbf{V}_1 = \frac{12 + j41}{104 - j3}\mathbf{V}_2$$

(2)

Substituting (2) into (1),

$$200\angle 45^\circ = (29 - j3)\frac{(12 + j41)}{104 - j3}\mathbf{V}_2 - (4 - j3)\mathbf{V}_2$$
$$200\angle 45^\circ = (14.21\angle 89.17^\circ)\mathbf{V}_2$$
$$\mathbf{V}_2 = \frac{200\angle 45^\circ}{14.21\angle 89.17^\circ}$$
$$\mathbf{V}_o = \frac{-j2}{4 + j5 - j2}\mathbf{V}_2 = \frac{-j2}{4 + j3}\mathbf{V}_2 = \frac{-6 - j8}{25}\mathbf{V}_2$$
$$\mathbf{V}_o = \frac{10\angle 233.13^\circ}{25} \cdot \frac{200\angle 45^\circ}{14.21\angle 89.17^\circ}$$
$$\mathbf{V}_o = \underline{\underline{5.63\angle 189^\circ \text{ V}}}$$

Chapter 10, Problem 19.



Obtain V_o in Fig. 10.68 using nodal analysis.

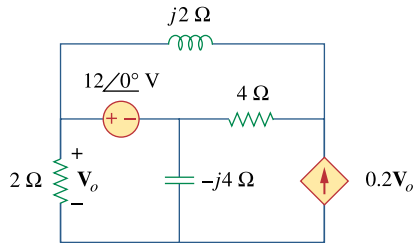
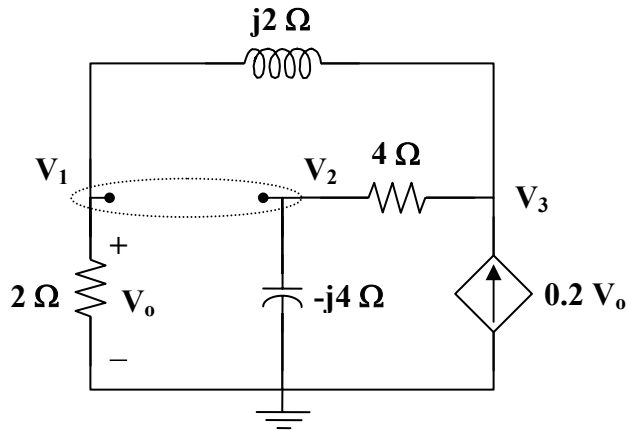


Figure 10.68

For Prob. 10.19.

Chapter 10, Solution 19.

We have a supernode as shown in the circuit below.



Notice that $V_o = V_1$.

At the supernode,

$$\begin{aligned} \frac{V_3 - V_2}{4} &= \frac{V_2}{-j4} + \frac{V_1}{2} + \frac{V_1 - V_3}{j2} \\ 0 &= (2 - j2)V_1 + (1 + j)V_2 + (-1 + j2)V_3 \end{aligned} \quad (1)$$

At node 3,

$$\begin{aligned} 0.2V_1 + \frac{V_1 - V_3}{j2} &= \frac{V_3 - V_2}{4} \\ (0.8 - j2)V_1 + V_2 + (-1 + j2)V_3 &= 0 \end{aligned} \quad (2)$$

Subtracting (2) from (1),

$$0 = 1.2V_1 + jV_2 \quad (3)$$

But at the supernode,

$$V_1 = 12\angle 0^\circ + V_2$$

$$\text{or} \quad V_2 = V_1 - 12 \quad (4)$$

Substituting (4) into (3),

$$\begin{aligned} 0 &= 1.2V_1 + j(V_1 - 12) \\ V_1 &= \frac{j12}{1.2 + j} = V_o \end{aligned}$$

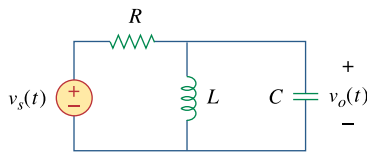
$$V_o = \frac{12\angle 90^\circ}{1.562\angle 39.81^\circ}$$

$$V_o = \underline{7.682\angle 50.19^\circ \text{ V}}$$

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Chapter 10, Problem 20.

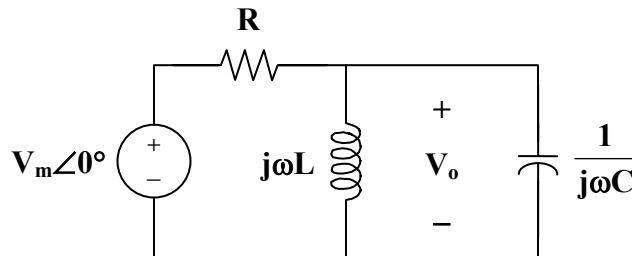
Refer to Fig. 10.69. If $v_s(t) = V_m \sin \omega t$ and $v_o(t) = A \sin(\omega t + \phi)$ derive the expressions for A and ϕ

**Figure 10.69**

For Prob. 10.20.

Chapter 10, Solution 20.

The circuit is converted to its frequency-domain equivalent circuit as shown below.



$$\text{Let } Z = j\omega L \parallel \frac{1}{j\omega C} = \frac{\frac{L}{C}}{j\omega L + \frac{1}{j\omega C}} = \frac{j\omega L}{1 - \omega^2 LC}$$

$$V_o = \frac{Z}{R + Z} V_m = \frac{\frac{j\omega L}{1 - \omega^2 LC}}{R + \frac{j\omega L}{1 - \omega^2 LC}} V_m = \frac{j\omega L}{R(1 - \omega^2 LC) + j\omega L} V_m$$

$$V_o = \frac{\omega L V_m}{\sqrt{R^2 (1 - \omega^2 LC)^2 + \omega^2 L^2}} \angle \left(90^\circ - \tan^{-1} \frac{\omega L}{R(1 - \omega^2 LC)} \right)$$

If $V_o = A \angle \phi$, then

$$A = \frac{\omega L V_m}{\sqrt{R^2 (1 - \omega^2 LC)^2 + \omega^2 L^2}}$$

$$\text{and } \phi = \underline{\underline{90^\circ - \tan^{-1} \frac{\omega L}{R(1 - \omega^2 LC)}}}$$

Chapter 10, Problem 21.

For each of the circuits in Fig. 10.70, find V_o/V_i for $\omega = 0$, $\omega \rightarrow \infty$, and $\omega^2 = 1/LC$.

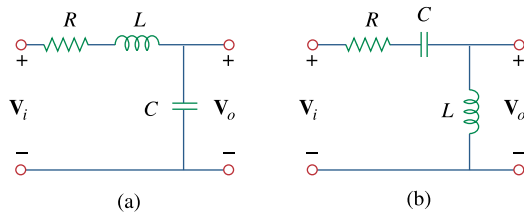


Figure 10.70

For Prob. 10.21.

Chapter 10, Solution 21.

$$(a) \quad \frac{V_o}{V_i} = \frac{\frac{1}{j\omega C}}{R + j\omega L + \frac{1}{j\omega C}} = \frac{1}{1 - \omega^2 LC + j\omega RC}$$

At $\omega = 0$, $\frac{V_o}{V_i} = \frac{1}{1} = \underline{1}$

As $\omega \rightarrow \infty$, $\frac{V_o}{V_i} = \underline{0}$

At $\omega = \frac{1}{\sqrt{LC}}$, $\frac{V_o}{V_i} = \frac{1}{jRC \cdot \frac{1}{\sqrt{LC}}} = \underline{\frac{-j}{R} \sqrt{\frac{L}{C}}}$

$$(b) \quad \frac{V_o}{V_i} = \frac{j\omega L}{R + j\omega L + \frac{1}{j\omega C}} = \frac{-\omega^2 LC}{1 - \omega^2 LC + j\omega RC}$$

At $\omega = 0$, $\frac{V_o}{V_i} = \underline{0}$

As $\omega \rightarrow \infty$, $\frac{V_o}{V_i} = \frac{1}{1} = \underline{1}$

At $\omega = \frac{1}{\sqrt{LC}}$, $\frac{V_o}{V_i} = \frac{-1}{jRC \cdot \frac{1}{\sqrt{LC}}} = \underline{\frac{j}{R} \sqrt{\frac{L}{C}}}$

Chapter 10, Problem 22.

For the circuit in Fig. 10.71, determine V_o/V_s .

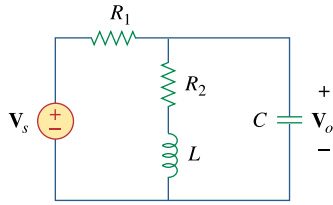
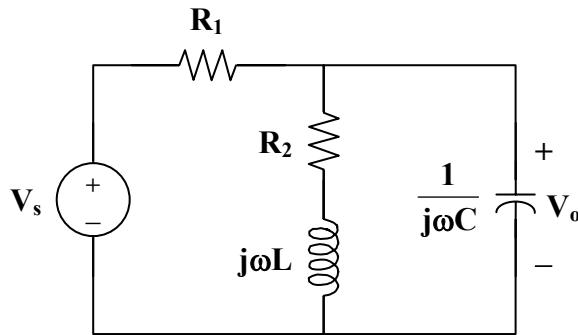


Figure 10.71

For Prob. 10.22.

Chapter 10, Solution 22.

Consider the circuit in the frequency domain as shown below.



$$\text{Let } Z = (R_2 + j\omega L) \parallel \frac{1}{j\omega C}$$

$$Z = \frac{\frac{1}{j\omega C}(R_2 + j\omega L)}{R_2 + j\omega L + \frac{1}{j\omega C}} = \frac{R_2 + j\omega L}{1 + j\omega R_2 - \omega^2 LC}$$

$$\frac{V_o}{V_s} = \frac{Z}{Z + R_1} = \frac{\frac{R_2 + j\omega L}{1 - \omega^2 LC + j\omega R_2 C}}{R_1 + \frac{R_2 + j\omega L}{1 - \omega^2 LC + j\omega R_2 C}}$$

$$\frac{V_o}{V_s} = \frac{R_2 + j\omega L}{R_1 + R_2 - \omega^2 LCR_1 + j\omega(L + R_1 R_2 C)}$$

Chapter 10, Problem 23.

Using nodal analysis obtain V in the circuit of Fig. 10.72.

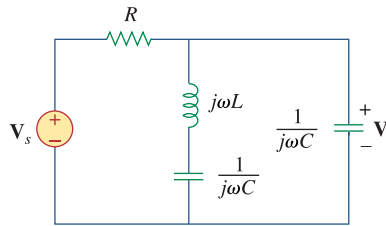


Figure 10.72

For Prob. 10.23.

Chapter 10, Solution 23.

$$\frac{V - V_s}{R} + \frac{V}{j\omega L + \frac{1}{j\omega C}} + j\omega CV = 0$$

$$V + \frac{j\omega RCV}{-\omega^2 LC + 1} + j\omega RCV = V_s$$

$$\left(\frac{1 - \omega^2 LC + j\omega RC + j\omega RC - j\omega^3 RLC^2}{1 - \omega^2 LC} \right) V = V_s$$

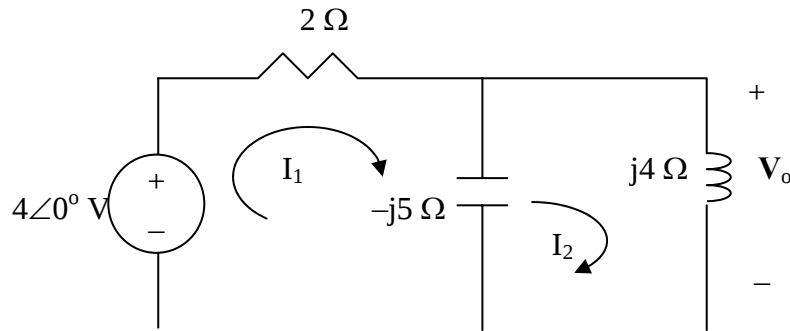
$$V = \frac{(1 - \omega^2 LC)V_s}{1 - \omega^2 LC + j\omega RC(2 - \omega^2 LC)}$$

Chapter 10, Problem 24.

Use mesh analysis to find V_o in the circuit of Prob. 10.2.

Chapter 10, Solution 24.

Consider the circuit as shown below.



For mesh 1,

$$4 = (2 - j5)I_1 + j5I_2 \quad (1)$$

For mesh 2,

$$0 = j5I_1 + (j4 - j5)I_2 \quad \longrightarrow \quad I_1 = \frac{1}{5}I_2 \quad (2)$$

Substituting (2) into (1),

$$4 = (2 - j5)\frac{1}{5}I_2 + j5I_2 \quad \longrightarrow \quad I_2 = \frac{1}{0.1 + j}$$

$$V_o = j4I_2 = \frac{j4}{0.1 + j} = \underline{3.98 \angle 5.71^\circ \text{ V}}$$

Chapter 10, Problem 25.



Solve for i_o in Fig. 10.73 using mesh analysis.

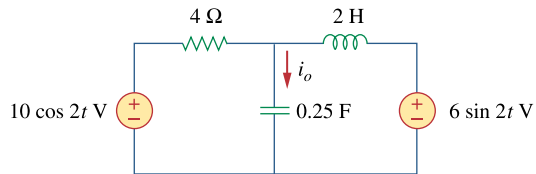


Figure 10.73

For Prob. 10.25.

Chapter 10, Solution 25.

$$\omega = 2$$

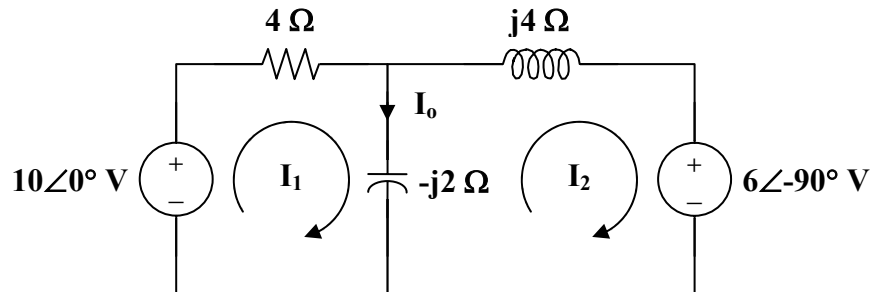
$$10 \cos(2t) \longrightarrow 10 \angle 0^\circ$$

$$6 \sin(2t) \longrightarrow 6 \angle -90^\circ = -j6$$

$$2 \text{ H} \longrightarrow j\omega L = j4$$

$$0.25 \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/4)} = -j2$$

The circuit is shown below.



For loop 1,

$$-10 + (4 - j2)I_1 + j2I_2 = 0$$

$$5 = (2 - j)I_1 + jI_2 \quad (1)$$

For loop 2,

$$j2I_1 + (j4 - j2)I_2 + (-j6) = 0$$

$$I_1 + I_2 = 3 \quad (2)$$

In matrix form (1) and (2) become

$$\begin{bmatrix} 2-j & j \\ 1 & 1 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} 5 \\ 3 \end{bmatrix}$$

$$\Delta = 2(1-j), \quad \Delta_1 = 5-j3, \quad \Delta_2 = 1-j3$$

$$I_o = I_1 - I_2 = \frac{\Delta_1 - \Delta_2}{\Delta} = \frac{4}{2(1-j)} = 1+j = 1.414 \angle 45^\circ$$

Therefore, $i_o(t) = \underline{\underline{1.4142 \cos(2t + 45^\circ) \text{ A}}}$

Chapter 10, Problem 26.

Use mesh analysis to find current i_o in the circuit of Fig. 10.74.

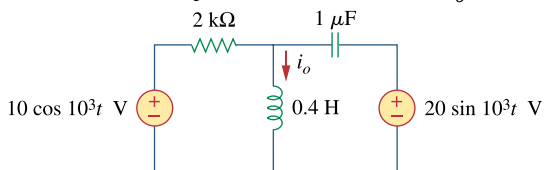


Figure 10.74

For Prob. 10.26.

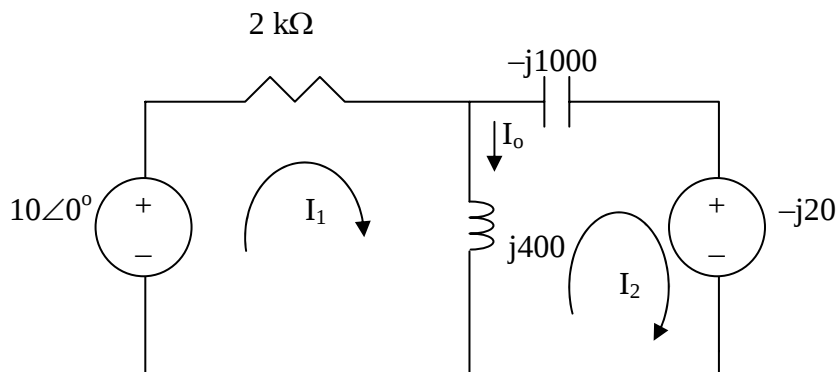
Chapter 10, Solution 26.

$$0.4\text{ H} \longrightarrow j\omega L = j10^3 \times 0.4 = j400$$

$$1\mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j10^3 \times 10^{-6}} = -j1000$$

$$20 \sin 10^3 t = 20 \cos(10^3 t - 90^\circ) \longrightarrow 20 \angle -90 = -j20$$

The circuit becomes that shown below.



For loop 1,

$$-10 + (12000 + j400)I_1 - j400I_2 = 0 \longrightarrow 1 = (200 + j40)I_1 - j40I_2 \quad (1)$$

For loop 2,

$$-j20 + (j400 - j1000)I_2 - j400I_1 = 0 \longrightarrow -12 = 40I_1 + 60I_2 \quad (2)$$

(2)

In matrix form, (1) and (2) become

$$\begin{bmatrix} 1 \\ -12 \end{bmatrix} = \begin{bmatrix} 200 + j40 & -j40 \\ 40 & 60 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

Solving this leads to

$$I_1 = 0.0025 - j0.0075, \quad I_2 = -0.035 + j0.005$$

$$I_o = I_1 - I_2 = 0.0375 - j0.0125 = 39.5 \angle -18.43^\circ \text{ mA}$$

$$i_o = 39.5 \cos(10^3 t - 18.43^\circ) \text{ mA}$$

Chapter 10, Problem 27.



Using mesh analysis, find $\mathbf{I}_1$ and $\mathbf{I}_2$ in the circuit of Fig. 10.75.

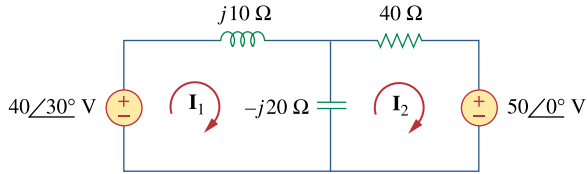


Figure 10.75

For Prob. 10.27.

Chapter 10, Solution 27.

For mesh 1,

$$\begin{aligned} -40\angle 30^\circ + (j10 - j20)\mathbf{I}_1 + j20\mathbf{I}_2 &= 0 \\ 4\angle 30^\circ &= -j\mathbf{I}_1 + j2\mathbf{I}_2 \end{aligned} \quad (1)$$

For mesh 2,

$$\begin{aligned} 50\angle 0^\circ + (40 - j20)\mathbf{I}_2 + j20\mathbf{I}_1 &= 0 \\ 5 &= -j2\mathbf{I}_1 - (4 - j2)\mathbf{I}_2 \end{aligned} \quad (2)$$

From (1) and (2),

$$\begin{bmatrix} 4\angle 30^\circ \\ 5 \end{bmatrix} = \begin{bmatrix} -j & j2 \\ -j2 & -(4 - j2) \end{bmatrix} \begin{bmatrix} \mathbf{I}_1 \\ \mathbf{I}_2 \end{bmatrix}$$

$$\Delta = -2 + 4j = 4.472\angle 116.56^\circ$$

$$\Delta_1 = -(4\angle 30^\circ)(4 - j2) - j10 = 21.01\angle 211.8^\circ$$

$$\Delta_2 = -j5 + 8\angle 120^\circ = 4.44\angle 154.27^\circ$$

$$\mathbf{I}_1 = \frac{\Delta_1}{\Delta} = \underline{\underline{4.698\angle 95.24^\circ \text{ A}}}$$

$$\mathbf{I}_2 = \frac{\Delta_2}{\Delta} = \underline{\underline{0.9928\angle 37.71^\circ \text{ A}}}$$

Chapter 10, Problem 28.



In the circuit of Fig. 10.76, determine the mesh currents i_1 and i_2 . Let $v_1 = 10 \cos 4t \text{ V}$ and $v_2 = 20 \cos(4t - 30^\circ) \text{ V}$.

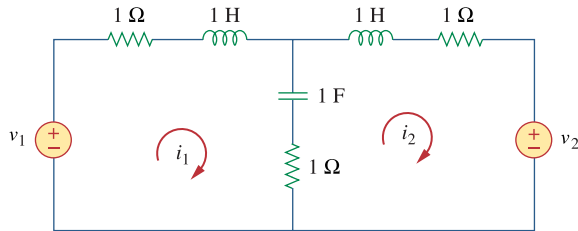


Figure 10.76

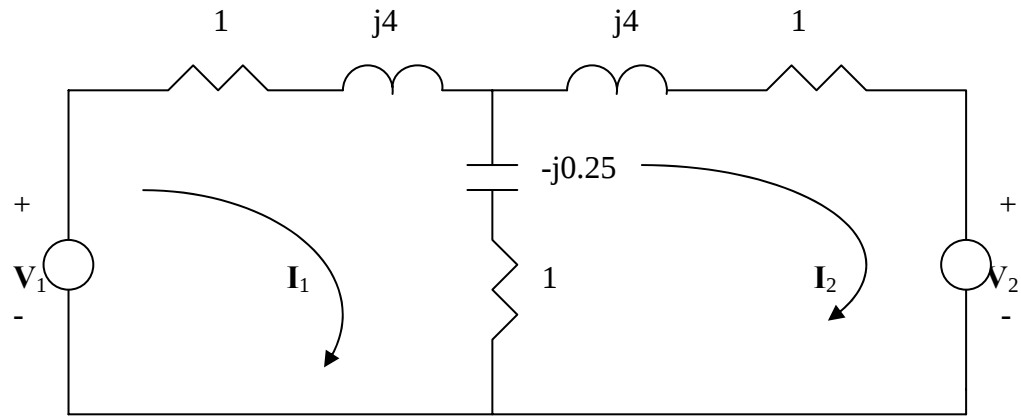
For Prob. 10.28.

Chapter 10, Solution 28.

$$1\text{H} \longrightarrow j\omega L = j4, \quad 1\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j1 \times 4} = -j0.25$$

The frequency-domain version of the circuit is shown below, where

$$V_1 = 10\angle 0^\circ, \quad V_2 = 20\angle -30^\circ.$$



$$V_1 = 10\angle 0^\circ, \quad V_2 = 20\angle -30^\circ$$

Applying mesh analysis,

$$10 = (2 + j3.75)I_1 - (1 - j0.25)I_2 \quad (1)$$

$$-20\angle -30^\circ = -(1 - j0.25)I_1 + (2 + j3.75)I_2 \quad (2)$$

From (1) and (2), we obtain

$$\begin{pmatrix} 10 \\ -17.32 + j10 \end{pmatrix} = \begin{pmatrix} 2 + j3.75 & -1 + j0.25 \\ -1 + j0.25 & 2 + j3.75 \end{pmatrix} \begin{pmatrix} I_1 \\ I_2 \end{pmatrix}$$

Solving this leads to

$$I_1 = 2.741\angle -41.07^\circ, \quad I_2 = 4.114\angle 92^\circ$$

Hence,

$$i_1(t) = \underline{2.741\cos(4t-41.07^\circ)\text{A}}, \quad i_2(t) = \underline{4.114\cos(4t+92^\circ)\text{A}}.$$

Chapter 10, Problem 29.



By using mesh analysis, find $\mathbf{I}_1$ and $\mathbf{I}_2$ in the circuit depicted in Fig. 10.77.

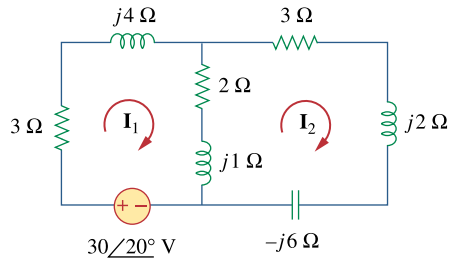


Figure 10.77

For Prob. 10.29.

Chapter 10, Solution 29.

For mesh 1,

$$\begin{aligned}(5 + j5)\mathbf{I}_1 - (2 + j)\mathbf{I}_2 - 30\angle 20^\circ &= 0 \\ 30\angle 20^\circ &= (5 + j5)\mathbf{I}_1 - (2 + j)\mathbf{I}_2 \\ (1)\end{aligned}$$

For mesh 2,

$$\begin{aligned}(5 + j3 - j6)\mathbf{I}_2 - (2 + j)\mathbf{I}_1 &= 0 \\ 0 &= -(2 + j)\mathbf{I}_1 + (5 - j3)\mathbf{I}_2 \\ (2)\end{aligned}$$

From (1) and (2),

$$\begin{bmatrix} 30\angle 20^\circ \\ 0 \end{bmatrix} = \begin{bmatrix} 5 + j5 & -(2 + j) \\ -(2 + j) & 5 - j3 \end{bmatrix} \begin{bmatrix} \mathbf{I}_1 \\ \mathbf{I}_2 \end{bmatrix}$$

$$\Delta = 37 + j6 = 37.48\angle 9.21^\circ$$

$$\Delta_1 = (30\angle 20^\circ)(5.831\angle -30.96^\circ) = 175\angle -10.96^\circ$$

$$\Delta_2 = (30\angle 20^\circ)(2.356\angle 26.56^\circ) = 67.08\angle 46.56^\circ$$

$$\mathbf{I}_1 = \frac{\Delta_1}{\Delta} = \underline{\underline{4.67\angle -20.17^\circ \text{ A}}}$$

$$\mathbf{I}_2 = \frac{\Delta_2}{\Delta} = \underline{\underline{1.79\angle 37.35^\circ \text{ A}}}$$

Chapter 10, Problem 30.



Use mesh analysis to find v_o in the circuit of Fig. 10.78. Let $v_{s1} = 120 \cos(100t + 90^\circ)$ V, $v_{s2} = 80 \cos 100t$ V.

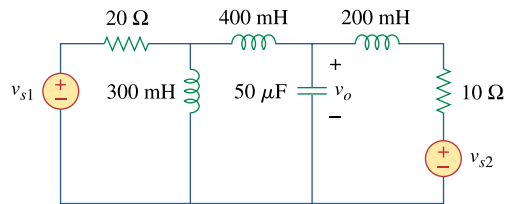


Figure 10.78

For Prob. 10.30.

Chapter 10, Solution 30.

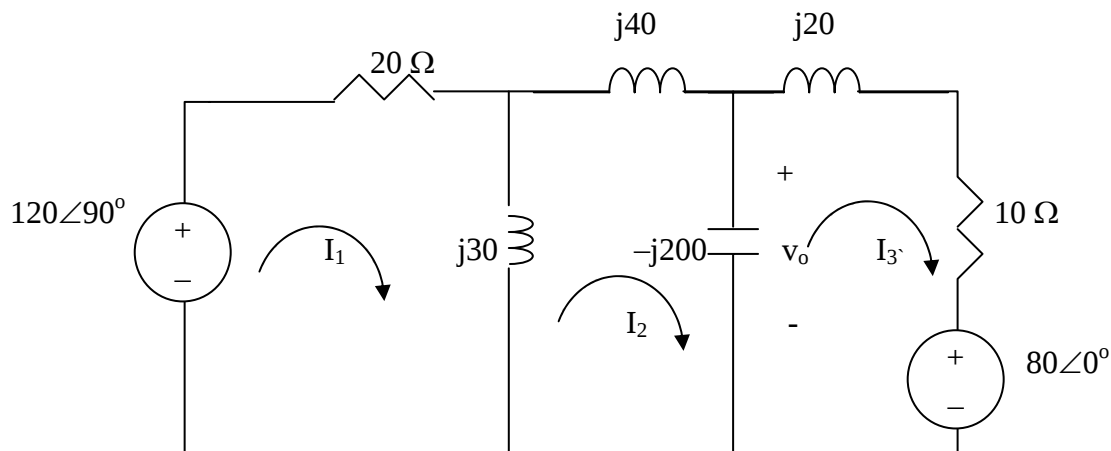
$$300 \text{ mH} \longrightarrow j\omega L = j100 \times 300 \times 10^{-3} = j30$$

$$200 \text{ mH} \longrightarrow j\omega L = j100 \times 200 \times 10^{-3} = j20$$

$$400 \text{ mH} \longrightarrow j\omega L = j100 \times 400 \times 10^{-3} = j40$$

$$50 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j100 \times 50 \times 10^{-6}} = -j200$$

The circuit becomes that shown below.



For mesh 1,

$$-120 \angle 90^\circ + (20 + j30)I_1 - j30I_2 = 0 \longrightarrow j120 = (20 + j30)I_1 - j30I_2 \quad (1)$$

For mesh 2,

$$-j30I_1 + (j30 + j40 - j200)I_2 + j200I_3 = 0 \longrightarrow 0 = -3I_1 - 13I_2 + 20I_3 \quad (2)$$

For mesh 3,

$$80 + j200I_2 + (10 - j180)I_3 = 0 \rightarrow -8 = j20I_2 + (1 - j18)I_3 \quad (3)$$

We put (1) to (3) in matrix form.

$$\begin{bmatrix} 2 + j3 & -j3 & 0 \\ -3 & -13 & 20 \\ 0 & j20 & 1 - j18 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} j12 \\ 0 \\ -8 \end{bmatrix}$$

This is an excellent candidate for MATLAB.

```
>> Z=[(2+3i),-3i,0;-3,-13,20;0,20i,(1-18i)]
```

Z =

```
2.0000 + 3.0000i    0 - 3.0000i    0
-3.0000    -13.0000    20.0000
0    0 + 20.0000i    1.0000 - 18.0000i
```

```
>> V=[12i;0;-8]
```

V =

```
0 + 12.0000i
0
-8.0000
```

```
>> I=inv(Z)*V
```

I =

```
2.0557 + 3.5651i
0.4324 + 2.1946i
0.5894 + 1.9612i
```

$$V_o = -j200(I_2 - I_3) = -j200(-0.157 + j0.2334) = 46.68 + j31.4 = 56.26 \angle 33.93^\circ$$

$$v_o = \underline{\underline{56.26 \cos(100t + 33.93^\circ) \text{ V.}}}$$

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Chapter 10, Problem 31.



Use mesh analysis to determine current $\mathbf{I}_o$ in the circuit of Fig. 10.79 below.

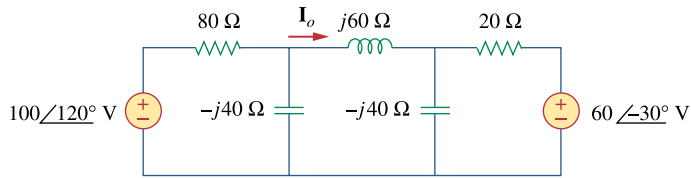
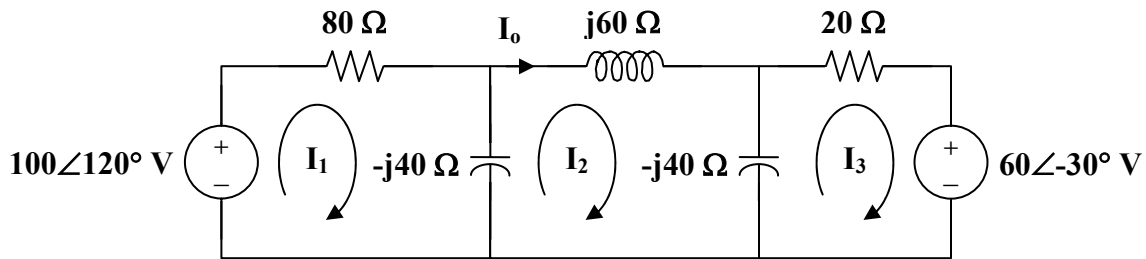


Figure 10.79

For Prob. 10.31.

Chapter 10, Solution 31.

Consider the network shown below.



For loop 1,

$$\begin{aligned} -100\angle 120^\circ + (80 - j40)\mathbf{I}_1 + j40\mathbf{I}_2 &= 0 \\ 10\angle 20^\circ &= 4(2 - j)\mathbf{I}_1 + j4\mathbf{I}_2 \end{aligned} \quad (1)$$

For loop 2,

$$\begin{aligned} j40\mathbf{I}_1 + (j60 - j80)\mathbf{I}_2 + j40\mathbf{I}_3 &= 0 \\ 0 &= 2\mathbf{I}_1 - \mathbf{I}_2 + 2\mathbf{I}_3 \end{aligned} \quad (2)$$

For loop 3,

$$\begin{aligned} 60\angle -30^\circ + (20 - j40)\mathbf{I}_3 + j40\mathbf{I}_2 &= 0 \\ -6\angle -30^\circ &= j4\mathbf{I}_2 + 2(1 - j2)\mathbf{I}_3 \end{aligned} \quad (3)$$

From (2),

$$2\mathbf{I}_3 = \mathbf{I}_2 - 2\mathbf{I}_1$$

Substituting this equation into (3),

$$-6\angle -30^\circ = -2(1 - j2)\mathbf{I}_1 + (1 + j2)\mathbf{I}_2 \quad (4)$$

From (1) and (4),

$$\begin{bmatrix} 10\angle 120^\circ \\ -6\angle -30^\circ \end{bmatrix} = \begin{bmatrix} 4(2 - j) & j4 \\ -2(1 - j2) & 1 + j2 \end{bmatrix} \begin{bmatrix} \mathbf{I}_1 \\ \mathbf{I}_2 \end{bmatrix}$$

$$\Delta = \begin{vmatrix} 8 - j4 & -j4 \\ -2 + j4 & 1 + j2 \end{vmatrix} = 32 + j20 = 37.74\angle 32^\circ$$

$$\Delta_2 = \begin{vmatrix} 8 - j4 & 10\angle 120^\circ \\ -2 + j4 & -6\angle -30^\circ \end{vmatrix} = -4.928 + j82.11 = 82.25\angle 93.44^\circ$$

$$\mathbf{I}_o = \mathbf{I}_2 = \frac{\Delta_2}{\Delta} = \underline{\underline{2.179\angle 61.44^\circ \text{ A}}}$$

Chapter 10, Problem 32.



Determine V_o and I_o in the circuit of Fig. 10.80 using mesh analysis.

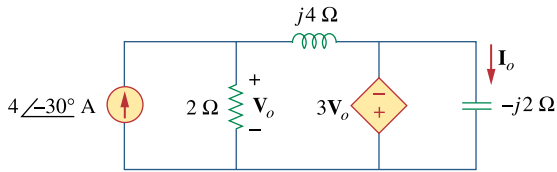
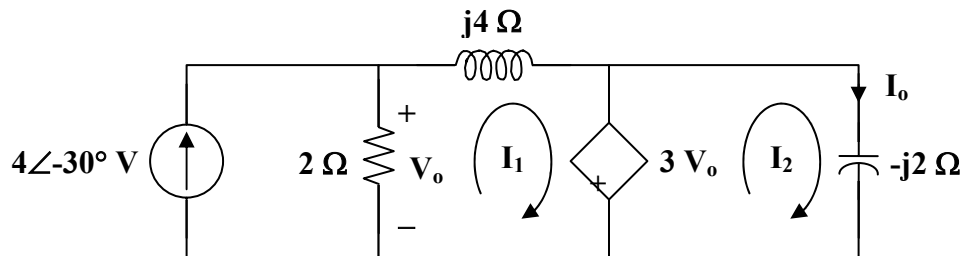


Figure 10.80

For Prob. 10.32.

Chapter 10, Solution 32.

Consider the circuit below.



For mesh 1,

$$(2 + j4)I_1 - 2(4\angle -30^\circ) + 3V_o = 0$$

where

$$V_o = 2(4\angle -30^\circ - I_1)$$

Hence,

$$(2 + j4)I_1 - 8\angle -30^\circ + 6(4\angle -30^\circ - I_1) = 0$$

$$4\angle -30^\circ = (1 - j)I_1$$

or

$$I_1 = 2\sqrt{2}\angle 15^\circ$$

$$I_o = \frac{3V_o}{-j2} = \frac{3}{-j2}(2)(4\angle -30^\circ - I_1)$$

$$I_o = j3(4\angle -30^\circ - 2\sqrt{2}\angle 15^\circ)$$

$$I_o = \underline{8.485\angle 15^\circ \text{ A}}$$

$$V_o = \frac{-j2I_o}{3} = \underline{5.657\angle -75^\circ \text{ V}}$$

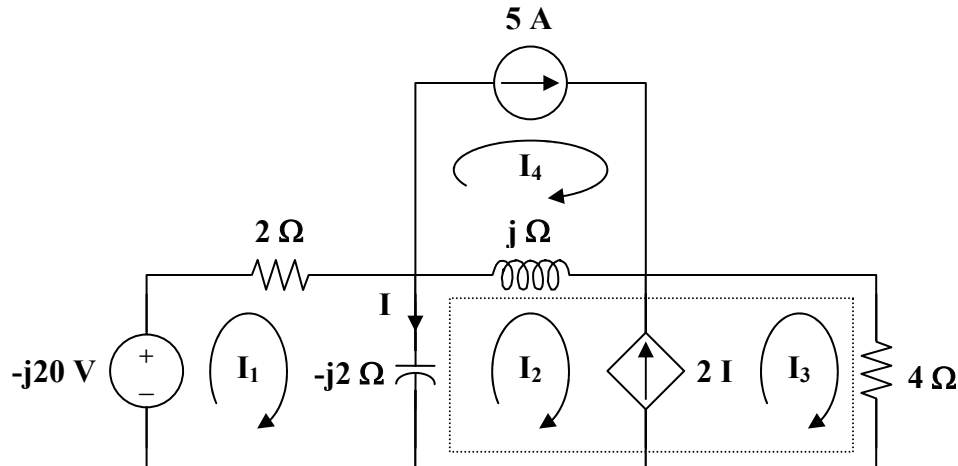
Chapter 10, Problem 33.



Compute $\mathbf{I}$ in Prob. 10.15 using mesh analysis.

Chapter 10, Solution 33.

Consider the circuit shown below.



For mesh 1,

$$\begin{aligned} j20 + (2 - j2)\mathbf{I}_1 + j2\mathbf{I}_2 &= 0 \\ (1 - j)\mathbf{I}_1 + j\mathbf{I}_2 &= -j10 \end{aligned} \quad (1)$$

For the supermesh,

$$(j - j2)\mathbf{I}_2 + j2\mathbf{I}_1 + 4\mathbf{I}_3 - j\mathbf{I}_4 = 0 \quad (2)$$

Also,

$$\begin{aligned} \mathbf{I}_3 - \mathbf{I}_2 &= 2\mathbf{I} = 2(\mathbf{I}_1 - \mathbf{I}_2) \\ \mathbf{I}_3 &= 2\mathbf{I}_1 - \mathbf{I}_2 \end{aligned} \quad (3)$$

For mesh 4,

$$\mathbf{I}_4 = 5 \quad (4)$$

Substituting (3) and (4) into (2),

$$(8 + j2)\mathbf{I}_1 - (-4 + j)\mathbf{I}_2 = j5 \quad (5)$$

Putting (1) and (5) in matrix form,

$$\begin{bmatrix} 1 - j & j \\ 8 + j2 & -4 - j \end{bmatrix} \begin{bmatrix} \mathbf{I}_1 \\ \mathbf{I}_2 \end{bmatrix} = \begin{bmatrix} -j10 \\ j5 \end{bmatrix}$$

$$\Delta = -3 - j5, \quad \Delta_1 = -5 + j40, \quad \Delta_2 = -15 + j85$$

$$\mathbf{I} = \mathbf{I}_1 - \mathbf{I}_2 = \frac{\Delta_1 - \Delta_2}{\Delta} = \frac{10 - j45}{-3 - j5} = \underline{\underline{7.906 \angle 43.49^\circ \text{ A}}}$$

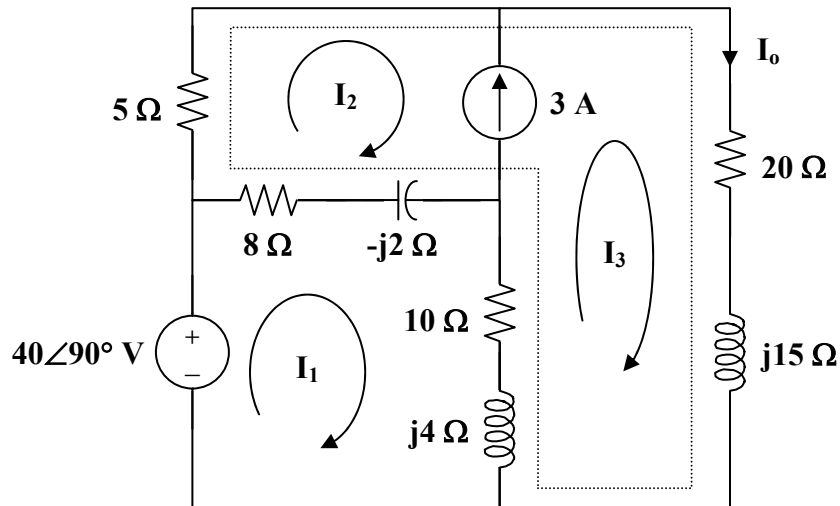
Chapter 10, Problem 34.



Use mesh analysis to find $\mathbf{I}_o$ in Fig. 10.28 (for Example 10.10).

Chapter 10, Solution 34.

The circuit is shown below.



For mesh 1,

$$-j40 + (18 + j2)\mathbf{I}_1 - (8 - j2)\mathbf{I}_2 - (10 + j4)\mathbf{I}_3 = 0 \quad (1)$$

For the supermesh,

$$(13 - j2)\mathbf{I}_2 + (30 + j19)\mathbf{I}_3 - (18 + j2)\mathbf{I}_1 = 0 \quad (2)$$

Also,

$$\mathbf{I}_2 = \mathbf{I}_3 - 3 \quad (3)$$

Adding (1) and (2) and incorporating (3),

$$-j40 + 5(\mathbf{I}_3 - 3) + (20 + j15)\mathbf{I}_3 = 0$$

$$\mathbf{I}_3 = \frac{3 + j8}{5 + j3} = 1.465 \angle 38.48^\circ$$

$$\mathbf{I}_o = \mathbf{I}_3 = \underline{\underline{1.465 \angle 38.48^\circ \text{ A}}}$$

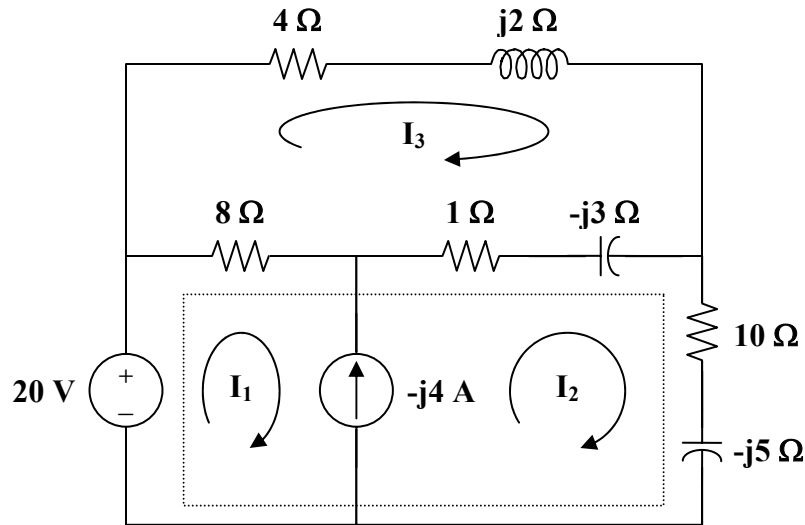
Chapter 10, Problem 35.



Calculate I_o in Fig. 10.30 (for Practice Prob. 10.10) using mesh analysis.

Chapter 10, Solution 35.

Consider the circuit shown below.



For the supermesh,

$$-20 + 8I_1 + (11 - j8)I_2 - (9 - j3)I_3 = 0 \quad (1)$$

Also,

$$I_1 = I_2 + j4 \quad (2)$$

For mesh 3,

$$(13 - j)I_3 - 8I_1 - (1 - j3)I_2 = 0 \quad (3)$$

Substituting (2) into (1),

$$(19 - j8)I_2 - (9 - j3)I_3 = 20 - j32 \quad (4)$$

Substituting (2) into (3),

$$-(9 - j3)I_2 + (13 - j)I_3 = j32 \quad (5)$$

From (4) and (5),

$$\begin{bmatrix} 19 - j8 & -(9 - j3) \\ -(9 - j3) & 13 - j \end{bmatrix} \begin{bmatrix} I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} 20 - j32 \\ j32 \end{bmatrix}$$

$$\Delta = 167 - j69,$$

$$\Delta_2 = 324 - j148$$

$$I_2 = \frac{\Delta_2}{\Delta} = \frac{324 - j148}{167 - j69} = \frac{356.2 \angle -24.55^\circ}{180.69 \angle -22.45^\circ}$$

$$I_2 = \underline{\underline{1.971 \angle -2.1^\circ \text{ A}}}$$

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Chapter 10, Problem 36.



Compute V_o in the circuit of Fig. 10.81 using mesh analysis.

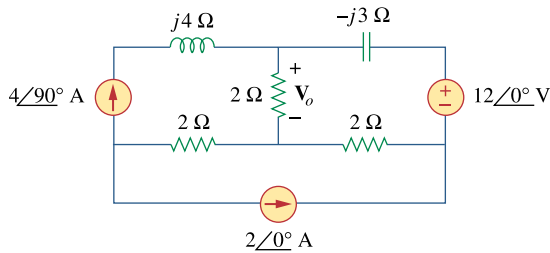
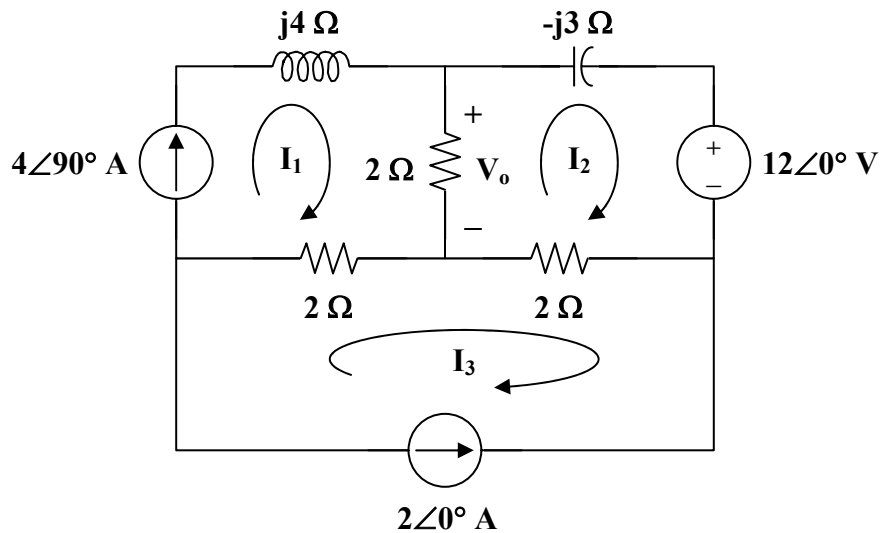


Figure 10.81

For Prob. 10.36.

Chapter 10, Solution 36.

Consider the circuit below.



Clearly,

$$\mathbf{I_1 = 4\angle 90^\circ = j4 \quad \text{and} \quad \mathbf{I_3 = -2}}$$

For mesh 2,

$$(4 - j3)\mathbf{I_2} - 2\mathbf{I_1} - 2\mathbf{I_3} + 12 = 0$$

$$(4 - j3)\mathbf{I_2} - j8 + 4 + 12 = 0$$

$$\mathbf{I_2 = \frac{-16 + j8}{4 - j3} = -3.52 - j0.64}$$

Thus,

$$\mathbf{V_o = 2(I_1 - I_2) = (2)(3.52 + j4.64) = 7.04 + j9.28}$$

$$\mathbf{V_o = 11.648\angle 52.82^\circ \text{ V}}$$

Chapter 10, Problem 37.



Use mesh analysis to find currents $\mathbf{I}_1$, $\mathbf{I}_2$, and $\mathbf{I}_3$ in the circuit of Fig. 10.82.

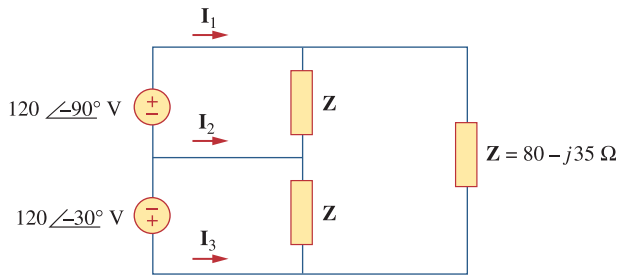
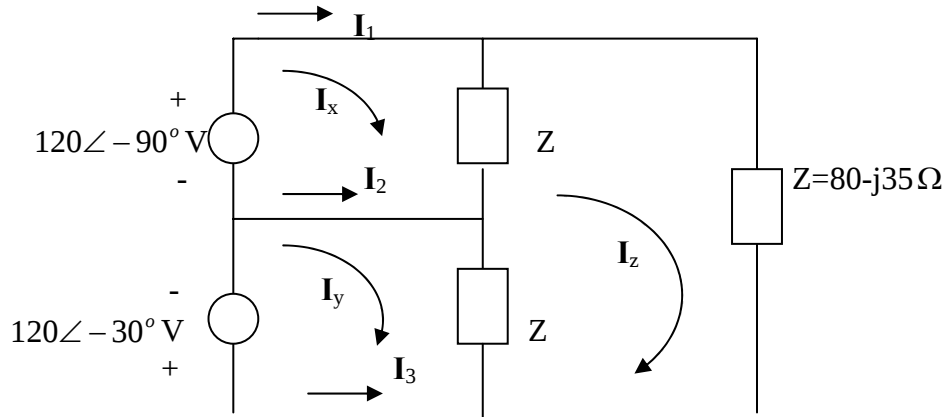


Figure 10.82

For Prob. 10.37.

Chapter 10, Solution 37.



For mesh x,

$$ZI_x - ZI_z = -j120 \quad (1)$$

For mesh y,

$$ZI_y - ZI_z = -120\angle 30^\circ = -103.92 + j60 \quad (2)$$

For mesh z,

$$-ZI_x - ZI_y + 3ZI_z = 0 \quad (3)$$

Putting (1) to (3) together leads to the following matrix equation:

$$\begin{pmatrix} (80 - j35) & 0 & (-80 + j35) \\ 0 & (80 - j35) & (-80 + j35) \\ (-80 + j35) & (-80 + j35) & (240 - j105) \end{pmatrix} \begin{pmatrix} I_x \\ I_y \\ I_z \end{pmatrix} = \begin{pmatrix} -j120 \\ -103.92 + j60 \\ 0 \end{pmatrix} \longrightarrow AI = B$$

Using MATLAB, we obtain

$$I = \text{inv}(A) * B = \begin{pmatrix} -0.2641 - j2.366 \\ -2.181 - j0.954 \\ -0.815 - j1.1066 \end{pmatrix}$$

$$I_1 = I_x = -0.2641 - j2.366 = \underline{2.38\angle -96.37^\circ} \text{ A}$$

$$I_2 = I_y - I_x = -1.9167 + j1.4116 = \underline{2.38\angle 143.63^\circ} \text{ A}$$

$$I_3 = -I_y = 2.181 + j0.954 = \underline{2.38\angle 23.63^\circ} \text{ A}$$

Chapter 10, Problem 38.



Using mesh analysis, obtain $\mathbf{I}_o$ in the circuit shown in Fig. 10.83.

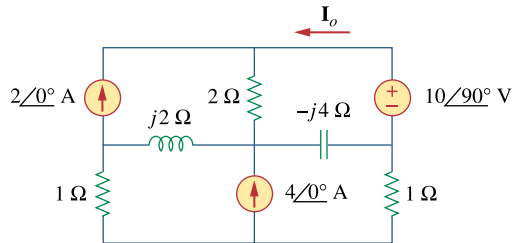
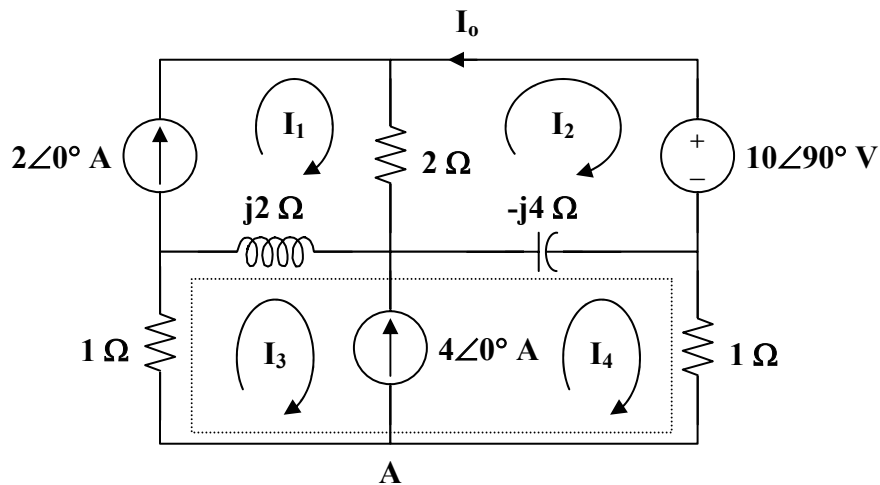


Figure 10.83

For Prob. 10.38.

Chapter 10, Solution 38.

Consider the circuit below.



Clearly,

$$\mathbf{I_1 = 2} \quad (1)$$

For mesh 2,

$$(2 - j4)\mathbf{I_2} - 2\mathbf{I_1} + j4\mathbf{I_4} + 10\angle 90^\circ = 0 \quad (2)$$

Substitute (1) into (2) to get

$$(1 - j2)\mathbf{I_2} + j2\mathbf{I_4} = 2 - j5$$

For the supermesh,

$$\begin{aligned} (1 + j2)\mathbf{I_3} - j2\mathbf{I_1} + (1 - j4)\mathbf{I_4} + j4\mathbf{I_2} &= 0 \\ j4\mathbf{I_2} + (1 + j2)\mathbf{I_3} + (1 - j4)\mathbf{I_4} &= j4 \end{aligned} \quad (3)$$

At node A,

$$\mathbf{I_3 = I_4 - 4} \quad (4)$$

Substituting (4) into (3) gives

$$j2\mathbf{I_2} + (1 - j)\mathbf{I_4} = 2(1 + j3) \quad (5)$$

From (2) and (5),

$$\begin{bmatrix} 1 - j2 & j2 \\ j2 & 1 - j \end{bmatrix} \begin{bmatrix} \mathbf{I_2} \\ \mathbf{I_4} \end{bmatrix} = \begin{bmatrix} 2 - j5 \\ 2 + j6 \end{bmatrix}$$

$$\Delta = 3 - j3, \quad \Delta_1 = 9 - j11$$

$$\mathbf{I_o = -I_2 = \frac{-\Delta_1}{\Delta} = \frac{-(9 - j11)}{3 - j3} = \frac{1}{3}(-10 + j)}$$

$$\mathbf{I_o = 3.35\angle 174.3^\circ A}$$

Chapter 10, Problem 39.



Find I_1 , I_2 , I_3 , and I_x in the circuit of Fig. 10.84.

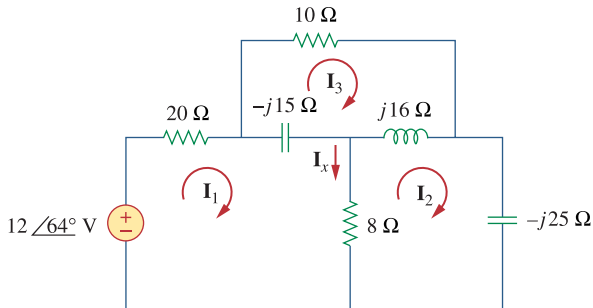


Figure 10.84

For Prob. 10.39.

Chapter 10, Solution 39.

For mesh 1,

$$(28 - j15)I_1 - 8I_2 + j15I_3 = 12\angle 64^\circ \quad (1)$$

For mesh 2,

$$-8I_1 + (8 - j9)I_2 - j16I_3 = 0 \quad (2)$$

For mesh 3,

$$j15I_1 - j16I_2 + (10 + j)I_3 = 0 \quad (3)$$

In matrix form, (1) to (3) can be cast as

$$\begin{pmatrix} (28 - j15) & -8 & j15 \\ -8 & (8 - j9) & -j16 \\ j15 & -j16 & (10 + j) \end{pmatrix} \begin{pmatrix} I_1 \\ I_2 \\ I_3 \end{pmatrix} = \begin{pmatrix} 12\angle 64^\circ \\ 0 \\ 0 \end{pmatrix} \quad \text{or} \quad \mathbf{AI} = \mathbf{B}$$

Using MATLAB,

$$\mathbf{I} = \text{inv}(\mathbf{A}) * \mathbf{B}$$

$$I_1 = -0.128 + j0.3593 = \underline{0.3814\angle 109.6^\circ \text{ A}}$$

$$I_2 = -0.1946 + j0.2841 = \underline{0.3443\angle 124.4^\circ \text{ A}}$$

$$I_3 = 0.0718 - j0.1265 = \underline{0.1455\angle -60.42^\circ \text{ A}}$$

$$I_x = I_1 - I_2 = 0.0666 + j0.0752 = \underline{0.1005\angle 48.5^\circ \text{ A}}$$

Chapter 10, Problem 40.

Find i_o in the circuit shown in Fig. 10.85 using superposition.

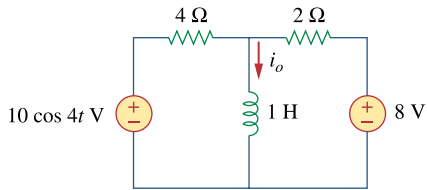
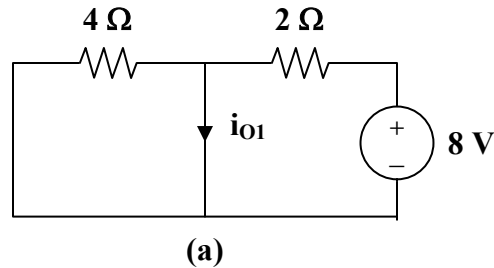


Figure 10.85
For Prob. 10.40.

Chapter 10, Solution 40.

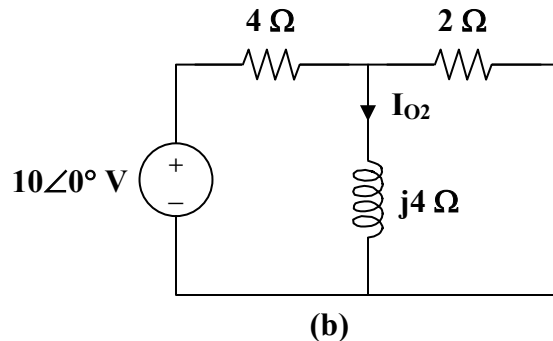
Let $i_o = i_{o1} + i_{o2}$, where i_{o1} is due to the dc source and i_{o2} is due to the ac source. For i_{o1} , consider the circuit in Fig. (a).



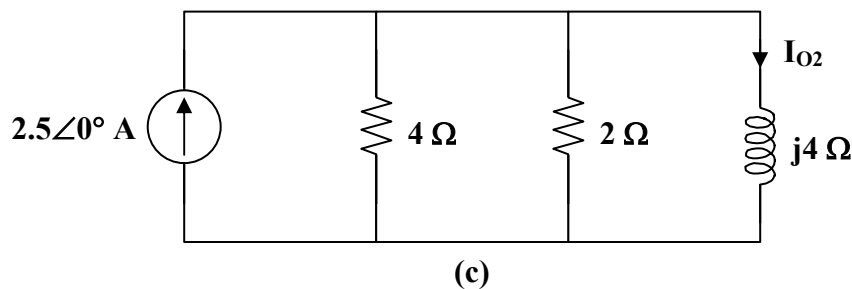
Clearly,

$$i_{o1} = 8/2 = 4 \text{ A}$$

For i_{o2} , consider the circuit in Fig. (b).



If we transform the voltage source, we have the circuit in Fig. (c), where $4 \parallel 2 = 4/3 \Omega$.



By the current division principle,

$$I_{o2} = \frac{4/3}{4/3 + j4} (2.5\angle 0^\circ)$$

$$I_{o2} = 0.25 - j0.75 = 0.79 \angle -71.56^\circ$$

Thus, $i_{o2} = 0.79 \cos(4t - 71.56^\circ) \text{ A}$

Therefore,

$$i_o = i_{o1} + i_{o2} = \underline{\underline{4 + 0.79 \cos(4t - 71.56^\circ) \text{ A}}}$$

Chapter 10, Problem 41.

Find v_o for the circuit in Fig. 10.86, assuming that $v_s = 6 \cos 2t + 4 \sin 4t$ V.

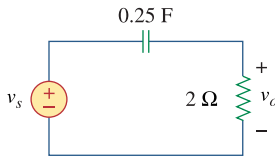


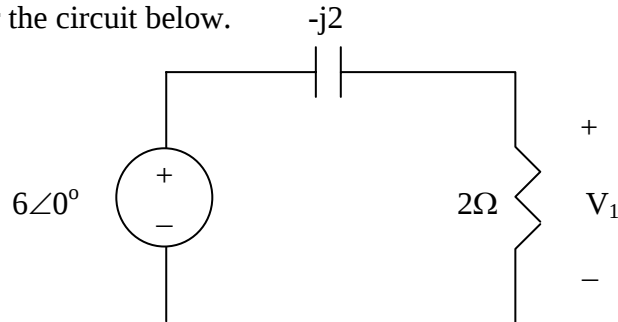
Figure 10.86
For Prob. 10.41.

Chapter 10, Solution 41.

We apply superposition principle. We let

$$v_o = v_1 + v_2$$

where v_1 and v_2 are due to the sources $6\cos 2t$ and $4\sin 4t$ respectively. To find v_1 , consider the circuit below.



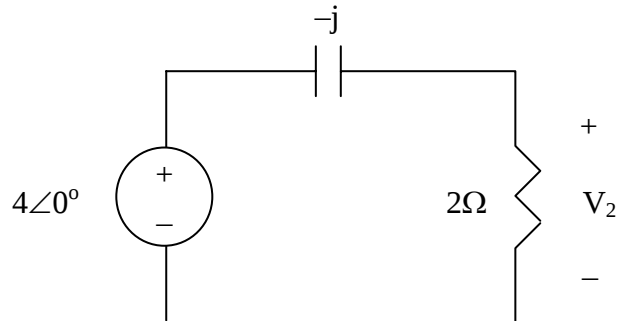
$$1/4F \longrightarrow \frac{1}{j\omega C} = \frac{1}{j2 \times 1/4} = -j2$$

$$V_1 = \frac{2}{2-j2}(6) = 3 + j3 = 4.2426 \angle 45^\circ$$

Thus,

$$v_1 = 4.2426 \cos(2t + 45^\circ)$$

To get v_2 , consider the circuit below



$$1/4F \longrightarrow \frac{1}{j\omega C} = \frac{1}{j4 \times 1/4} = -j1$$

$$V_2 = \frac{2}{2-j}(4) = 3.2 + j1.6 = 3.578 \angle 26.56^\circ$$

$$v_2 = 3.578 \sin(4t + 26.56^\circ)$$

Hence,

$$v_o = \underline{4.243\cos(2t + 45^\circ) + 3.578\sin(4t + 25.56^\circ) \text{ V.}}$$

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Chapter 10, Problem 42.

Solve for I_o in the circuit of Fig. 10.87.

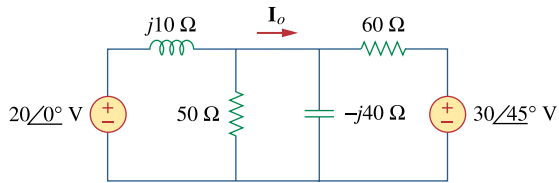


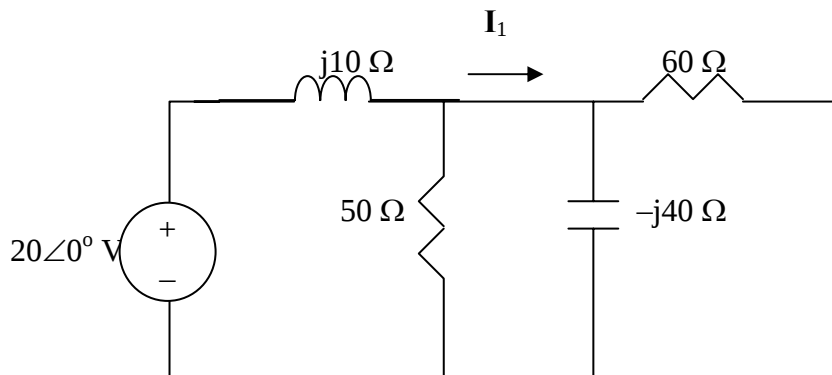
Figure 10.87

For Prob. 10.42.

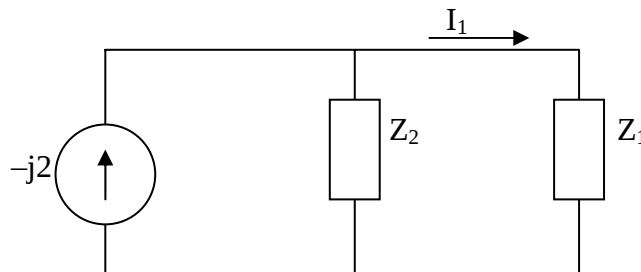
Chapter 10, Solution 42.

$$\text{Let } I_o = I_1 + I_2$$

where I_1 and I_2 are due to $20\angle 0^\circ$ and $30\angle 45^\circ$ sources respectively. To get I_1 , we use the circuit below.



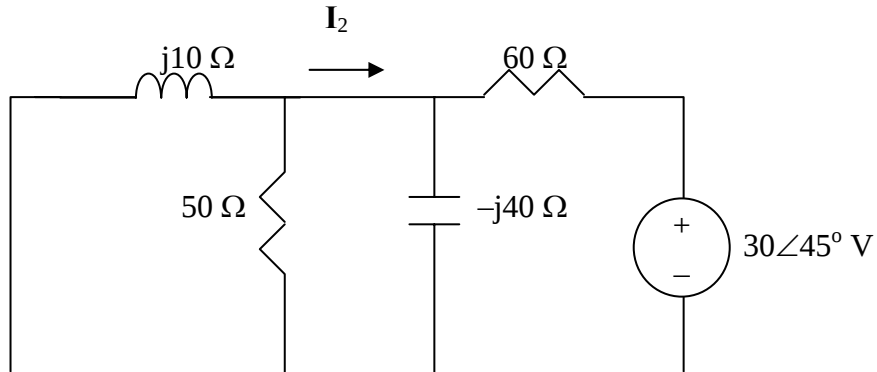
Let $Z_1 = -j40//60 = 18.4615 - j27.6927$, $Z_2 = j10//50 = 1.9231 + j9.615$
Transforming the voltage source to a current source leads to the circuit below.



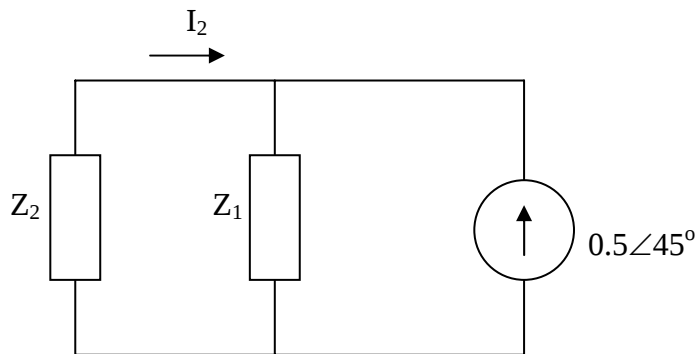
Using current division,

$$I_1 = \frac{Z_2}{Z_1 + Z_2}(-j2) = 0.6217 + j0.3626$$

To get I_2 , we use the circuit below.



After transforming the voltage source, we obtain the circuit below.



Using current division,

$$I_2 = \frac{-Z_1}{Z_1 + Z_2}(0.5 \angle 45^\circ) = -0.5275 - j0.3077$$

Hence,

$$I_o = I_1 + I_2 = 0.0942 + j0.0509 = \underline{0.109 \angle 30^\circ \text{ A}}$$

Chapter 10, Problem 43.

Using the superposition principle, find i_x in the circuit of Fig. 10.88.

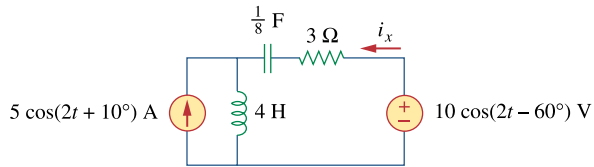


Figure 10.88

For Prob. 10.43.

Chapter 10, Solution 43.

Let $\mathbf{I}_x = \mathbf{I}_1 + \mathbf{I}_2$, where $\mathbf{I}_1$ is due to the voltage source and $\mathbf{I}_2$ is due to the current source.

$$\omega = 2$$

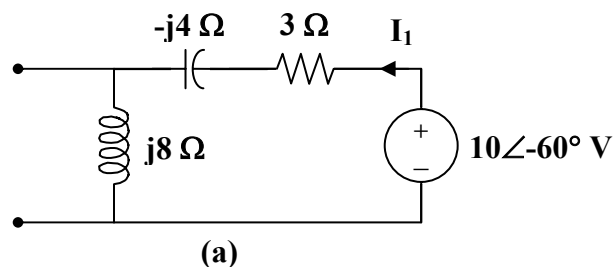
$$5 \cos(2t + 10^\circ) \longrightarrow 5 \angle 10^\circ$$

$$10 \cos(2t - 60^\circ) \longrightarrow 10 \angle -60^\circ$$

$$4 \text{ H} \longrightarrow j\omega L = j8$$

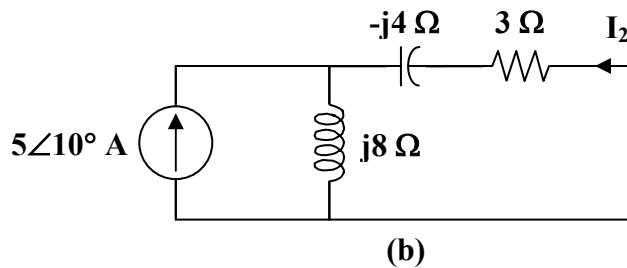
$$\frac{1}{8} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/8)} = -j4$$

For $\mathbf{I}_1$, consider the circuit in Fig. (a).



$$\mathbf{I}_1 = \frac{10 \angle -60^\circ}{3 + j8 - j4} = \frac{10 \angle -60^\circ}{3 + j4}$$

For $\mathbf{I}_2$, consider the circuit in Fig. (b).



$$\mathbf{I}_2 = \frac{-j8}{3 + j8 - j4} (5 \angle 10^\circ) = \frac{-j40 \angle 10^\circ}{3 + j4}$$

$$\mathbf{I}_x = \mathbf{I}_1 + \mathbf{I}_2 = \frac{1}{3 + j4} (10 \angle -60^\circ - j40 \angle 10^\circ)$$

$$\mathbf{I}_x = \frac{49.51 \angle -76.04^\circ}{5 \angle 53.13^\circ} = 9.902 \angle -129.17^\circ$$

Therefore, $i_x = \underline{\underline{9.902 \cos(2t - 129.17^\circ) \text{ A}}}$

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Chapter 10, Problem 44.

Use the superposition principle to obtain v_x in the circuit of Fig. 10.89. Let $v_s = 50 \sin 2t$ V and $i_s = 12 \cos(6t + 10^\circ)$ A.

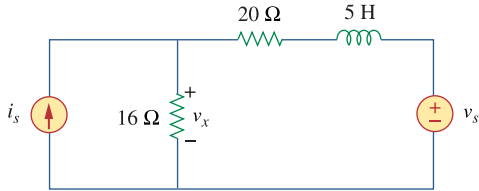


Figure 10.89

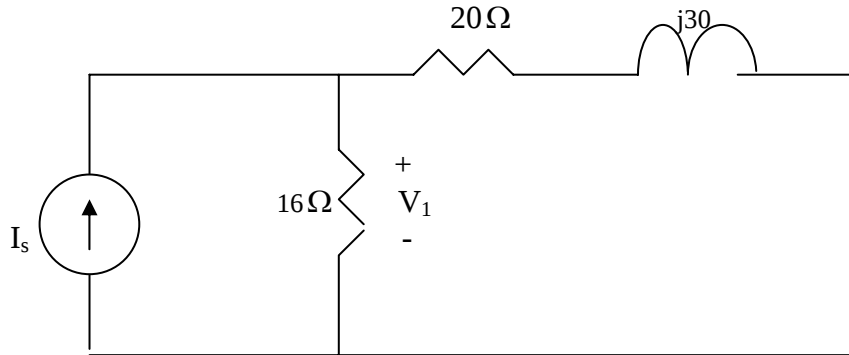
For Prob. 10.44.

Chapter 10, Solution 44.

Let $v_x = v_1 + v_2$, where v_1 and v_2 are due to the current source and voltage source respectively.

For v_1 , $\omega = 6$, $5 \text{ H} \longrightarrow j\omega L = j30$

The frequency-domain circuit is shown below.

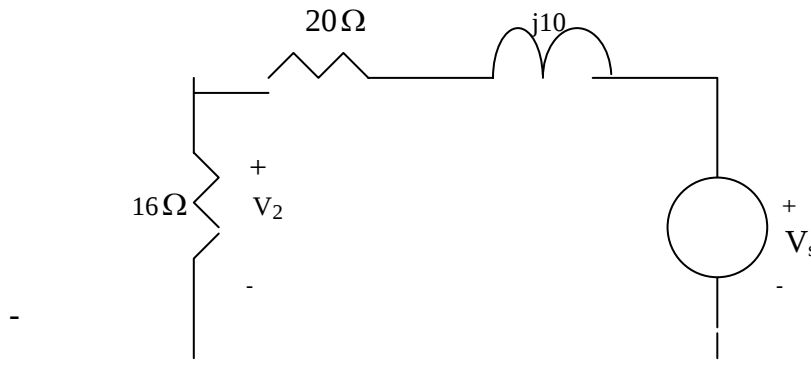


$$\text{Let } Z = 16 \parallel (20 + j30) = \frac{16(20 + j30)}{36 + j30} = 11.8 + j3.497 = 12.31 \angle 16.5^\circ$$

$$V_1 = I_s Z = (12 \angle 10^\circ)(12.31 \angle 16.5^\circ) = 147.7 \angle 26.5^\circ \longrightarrow v_1 = 147.7 \cos(6t + 26.5^\circ) \text{ V}$$

For v_2 , $\omega = 2$, $5 \text{ H} \longrightarrow j\omega L = j10$

The frequency-domain circuit is shown below.



Using voltage division,

$$V_2 = \frac{16}{16 + 20 + j10} V_s = \frac{16(50 \angle 0^\circ)}{36 + j10} = 21.41 \angle -15.52^\circ \longrightarrow v_2 = 21.41 \sin(2t - 15.52^\circ) \text{ V}$$

Thus,

$$v_x = 147.7 \cos(6t + 26.5^\circ) + 21.41 \sin(2t - 15.52^\circ) \text{ V}$$

Chapter 10, Problem 45.

Use superposition to find $i(t)$ in the circuit of Fig. 10.90.

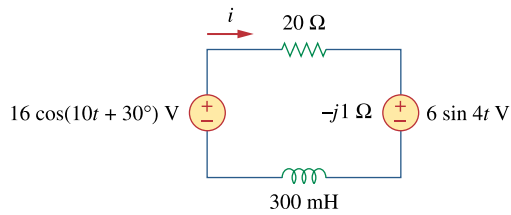
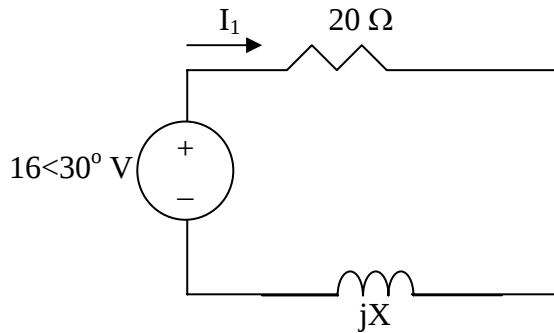


Figure 10.90
For Prob. 10.45.

Chapter 10, Solution 45.

Let $i = i_1 + i_2$, where i_1 and i_2 are due to $16\cos(10t + 30^\circ)$ and $6\sin 4t$ sources respectively. To find i_1 , consider the circuit below.

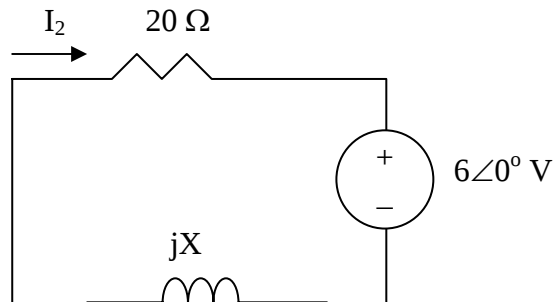


$$X = \omega L = 10 \times 300 \times 10^{-3} = 3$$

$$I_1 = \frac{16 \angle 30^\circ}{20 + j3} = 0.7911$$

$$i_1 = 0.7911 \cos(10t + 21.47^\circ) \text{ A}$$

To find i_2 , consider the circuit below.



$$X = \omega L = 4 \times 300 \times 10^{-3} = 1.2$$

$$I_2 = -\frac{6 \angle 0^\circ}{20 + j1.2} = 0.2995 \angle 176.6^\circ$$

$$i_2 = 0.2995 \sin(4t + 176.6^\circ) \text{ A}$$

Thus,

$$\begin{aligned} i &= i_1 + i_2 = 0.7911 \cos(10t + 21.47^\circ) + 0.2995 \sin(4t + 176.6^\circ) \text{ A} \\ &= \underline{\underline{791.1 \cos(10t + 21.47^\circ) + 299.5 \sin(4t + 176.6^\circ) \text{ mA}}} \end{aligned}$$

Chapter 10, Problem 46.

Solve for $v_o(t)$ in the circuit of Fig. 10.91 using the superposition principle.

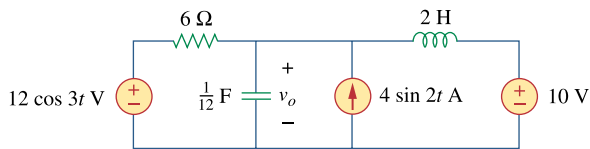
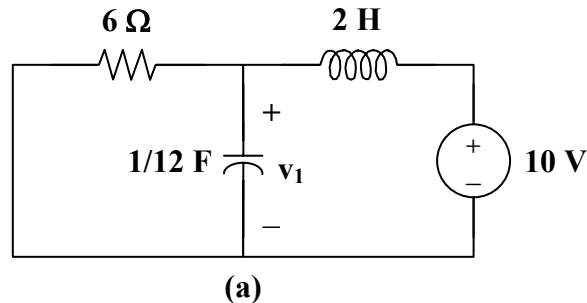


Figure 10.91

For Prob. 10.46.

Chapter 10, Solution 46.

Let $v_o = v_1 + v_2 + v_3$, where v_1 , v_2 , and v_3 are respectively due to the 10-V dc source, the ac current source, and the ac voltage source. For v_1 consider the circuit in Fig. (a).



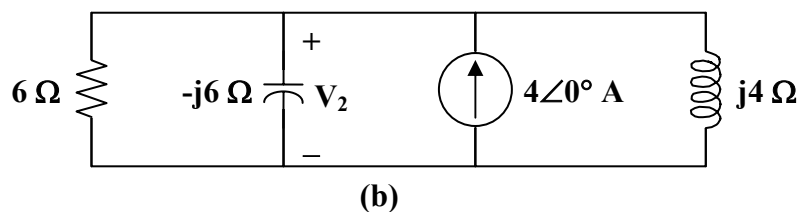
The capacitor is open to dc, while the inductor is a short circuit. Hence,
 $v_1 = 10 \text{ V}$

For v_2 , consider the circuit in Fig. (b).

$$\omega = 2$$

$$2 \text{ H} \longrightarrow j\omega L = j4$$

$$\frac{1}{12} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/12)} = -j6$$



Applying nodal analysis,

$$4 = \frac{\mathbf{V}_2}{6} + \frac{\mathbf{V}_2}{-j6} + \frac{\mathbf{V}_2}{j4} = \left(\frac{1}{6} + \frac{j}{6} - \frac{j}{4} \right) \mathbf{V}_2$$

$$\mathbf{V}_2 = \frac{24}{1 - j0.5} = 21.45 \angle 26.56^\circ$$

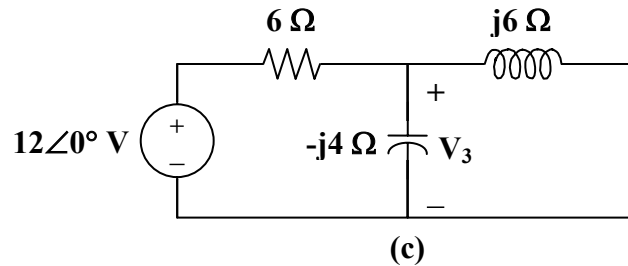
Hence, $v_2 = 21.45 \sin(2t + 26.56^\circ) \text{ V}$

For v_3 , consider the circuit in Fig. (c).

$$\omega = 3$$

$$2 \text{ H} \longrightarrow j\omega L = j6$$

$$\frac{1}{12} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(3)(1/12)} = -j4$$



At the non-reference node,

$$\frac{12 - \mathbf{V}_3}{6} = \frac{\mathbf{V}_3}{-j4} + \frac{\mathbf{V}_3}{j6}$$

$$\mathbf{V}_3 = \frac{12}{1 + j0.5} = 10.73 \angle -26.56^\circ$$

Hence, $v_3 = 10.73 \cos(3t - 26.56^\circ) \text{ V}$

Therefore, $v_o = \underline{\underline{10 + 21.45 \sin(2t + 26.56^\circ) + 10.73 \cos(3t - 26.56^\circ) \text{ V}}}$

Chapter 10, Problem 47.



Determine i_o in the circuit of Fig. 10.92, using the superposition principle.

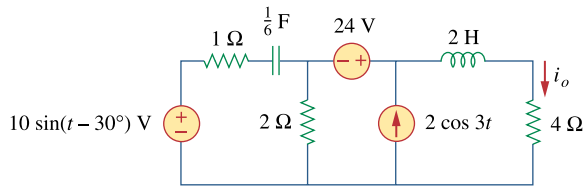
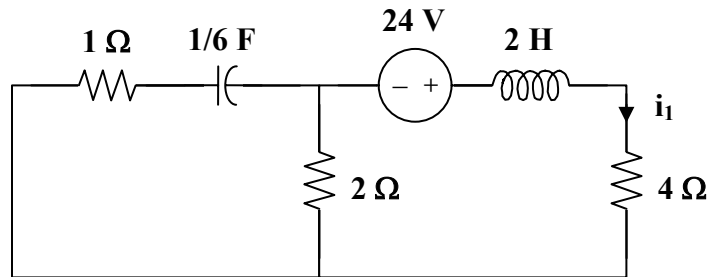


Figure 10.92

For Prob. 10.47.

Chapter 10, Solution 47.

Let $i_o = i_1 + i_2 + i_3$, where i_1 , i_2 , and i_3 are respectively due to the 24-V dc source, the ac voltage source, and the ac current source. For i_1 , consider the circuit in Fig. (a).



Since the capacitor is an open circuit to dc,

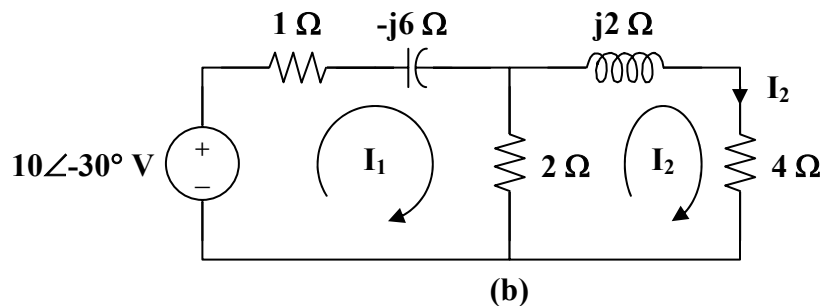
$$i_1 = \frac{24}{4+2} = 4 \text{ A}$$

For i_2 , consider the circuit in Fig. (b).

$$\omega = 1$$

$$2 \text{ H} \longrightarrow j\omega L = j2$$

$$\frac{1}{6} \text{ F} \longrightarrow \frac{1}{j\omega C} = -j6$$



For mesh 1,

$$\begin{aligned} -10\angle -30^\circ + (3 - j6)I_1 - 2I_2 &= 0 \\ 10\angle -30^\circ &= 3(1 - 2j)I_1 - 2I_2 \end{aligned} \quad (1)$$

For mesh 2,

$$\begin{aligned} 0 &= -2I_1 + (6 + j2)I_2 \\ I_1 &= (3 + j)I_2 \end{aligned} \quad (2)$$

Substituting (2) into (1)

$$10 \angle -30^\circ = 13 - j15 \mathbf{I}_2$$

$$\mathbf{I}_2 = 0.504 \angle 19.1^\circ$$

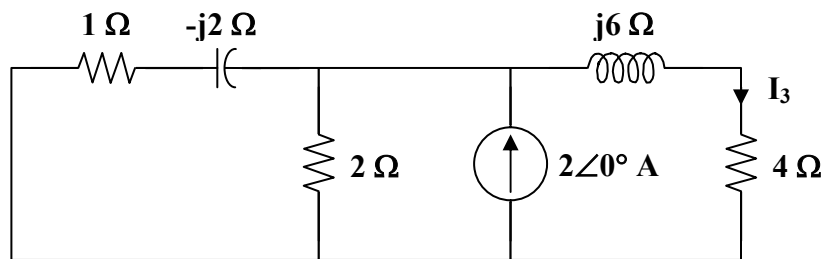
Hence, $i_2 = 0.504 \sin(t + 19.1^\circ) \text{ A}$

For i_3 , consider the circuit in Fig. (c).

$$\omega = 3$$

$$2 \text{ H} \longrightarrow j\omega L = j6$$

$$\frac{1}{6} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(3)(1/6)} = -j2$$



(c)

$$2 \parallel (1 - j2) = \frac{2(1 - j2)}{3 - j2}$$

Using current division,

$$\mathbf{I}_3 = \frac{\frac{2(1 - j2)}{3 - j2} \cdot (2 \angle 0^\circ)}{4 + j6 + \frac{2(1 - j2)}{3 - j2}} = \frac{2(1 - j2)}{13 + j3}$$

$$\mathbf{I}_3 = 0.3352 \angle -76.43^\circ$$

Hence $i_3 = 0.3352 \cos(3t - 76.43^\circ) \text{ A}$

Therefore, $i_o = \underline{4 + 0.504 \sin(t + 19.1^\circ) + 0.3352 \cos(3t - 76.43^\circ) \text{ A}}$

Chapter 10, Problem 48.



Find i_o in the circuit of Fig. 10.93 using superposition.

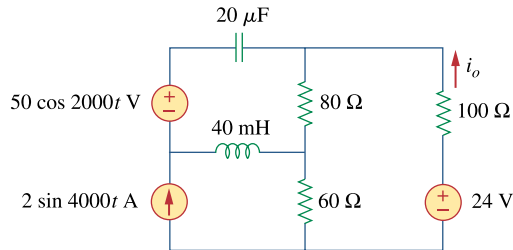


Figure 10.93

For Prob. 10.48.

Chapter 10, Solution 48.

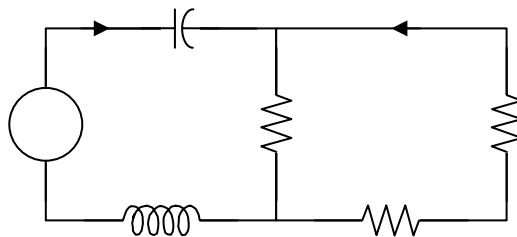
Let $i_o = i_{o1} + i_{o2} + i_{o3}$, where i_{o1} is due to the ac voltage source, i_{o2} is due to the dc voltage source, and i_{o3} is due to the ac current source. For i_{o1} , consider the circuit in Fig. (a).

$$\omega = 2000$$

$$50 \cos(2000t) \longrightarrow 50 \angle 0^\circ$$

$$40 \text{ mH} \longrightarrow j\omega L = j(2000)(40 \times 10^{-3}) = j80$$

$$20 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2000)(20 \times 10^{-6})} = -j25$$



$$80 \parallel (60 + 100) = 160/3$$

$$\mathbf{I} = \frac{50}{160/3 + j80 - j25} = \frac{30}{32 + j33}$$

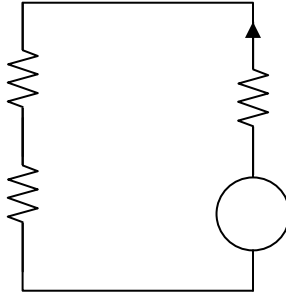
Using current division,

$$\mathbf{I}_{O1} = \frac{-80\mathbf{I}}{80+160} = \frac{-1}{3}\mathbf{I} = \frac{10\angle 180^\circ}{46\angle 45.9^\circ}$$

$$\mathbf{I}_{O1} = 0.217\angle 134.1^\circ$$

Hence, $i_{O1} = 0.217 \cos(2000t + 134.1^\circ) \text{ A}$

For i_{O2} , consider the circuit in Fig. (b).



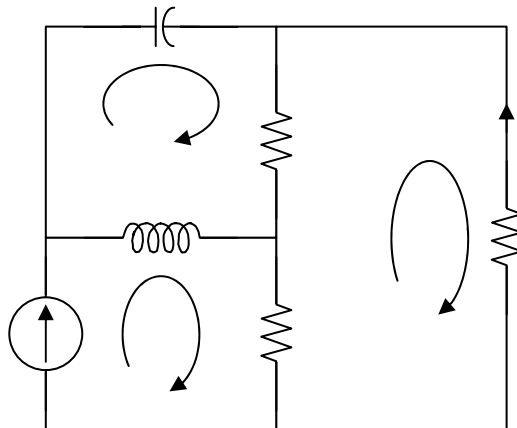
$$i_{O2} = \frac{24}{80+60+100} = 0.1 \text{ A}$$

For i_{O3} , consider the circuit in Fig. (c).

$$\omega = 4000$$

$$2 \cos(4000t) \longrightarrow 2\angle 0^\circ$$

$$40 \text{ mH} \longrightarrow j\omega L = j(4000)(40 \times 10^{-3}) = j160$$



$$20 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(4000)(20 \times 10^{-6})} = -j12.5$$

For mesh 1,

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$$\mathbf{I}_1 = 2 \quad (1)$$

For mesh 2,

$$(80 + j160 - j12.5)\mathbf{I}_2 - j160\mathbf{I}_1 - 80\mathbf{I}_3 = 0$$

Simplifying and substituting (1) into this equation yields

$$(8 + j14.75)\mathbf{I}_2 - 8\mathbf{I}_3 = j32 \quad (2)$$

For mesh 3,

$$240\mathbf{I}_3 - 60\mathbf{I}_1 - 80\mathbf{I}_2 = 0$$

Simplifying and substituting (1) into this equation yields

$$\mathbf{I}_2 = 3\mathbf{I}_3 - 1.5 \quad (3)$$

Substituting (3) into (2) yields

$$(16 + j44.25)\mathbf{I}_3 = 12 + j54.125$$

$$\mathbf{I}_3 = \frac{12 + j54.125}{16 + j44.25} = 1.1782 \angle 7.38^\circ$$

$$\mathbf{I}_{O3} = -\mathbf{I}_3 = -1.1782 \angle 7.38^\circ$$

Hence, $i_{O3} = -1.1782 \sin(4000t + 7.38^\circ) \text{ A}$

Therefore, $i_O = \underline{\underline{0.1 + 0.217 \cos(2000t + 134.1^\circ) - 1.1782 \sin(4000t + 7.38^\circ) \text{ A}}}$

Chapter 10, Problem 49.

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Using source transformation, find i in the circuit of Fig. 10.94.

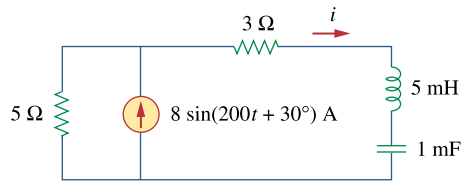


Figure 10.94

For Prob. 10.49.

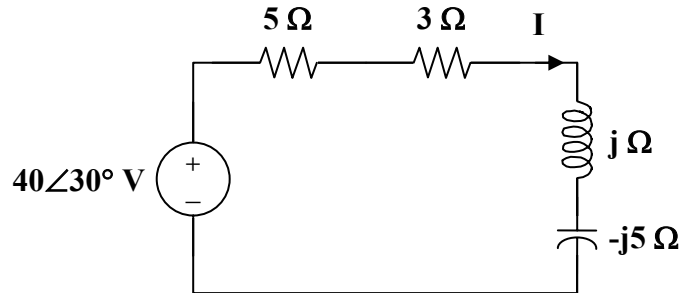
Chapter 10, Solution 49.

$$8 \sin(200t + 30^\circ) \longrightarrow 8 \angle 30^\circ, \quad \omega = 200$$

$$5 \text{ mH} \longrightarrow j\omega L = j(200)(5 \times 10^{-3}) = j$$

$$1 \text{ mF} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(200)(1 \times 10^{-3})} = -j5$$

After transforming the current source, the circuit becomes that shown in the figure below.



$$\mathbf{I} = \frac{40 \angle 30^\circ}{5 + 3 + j - j5} = \frac{40 \angle 30^\circ}{8 - j4} = 4.472 \angle 56.56^\circ$$

$$i = \underline{\underline{4.472 \sin(200t + 56.56^\circ) \text{ A}}}$$

Chapter 10, Problem 50.

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Use source transformation to find v_o in the circuit of Fig. 10.95.

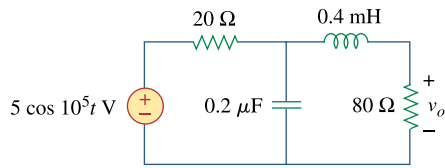


Figure 10.95
For Prob. 10.50.

Chapter 10, Solution 50.

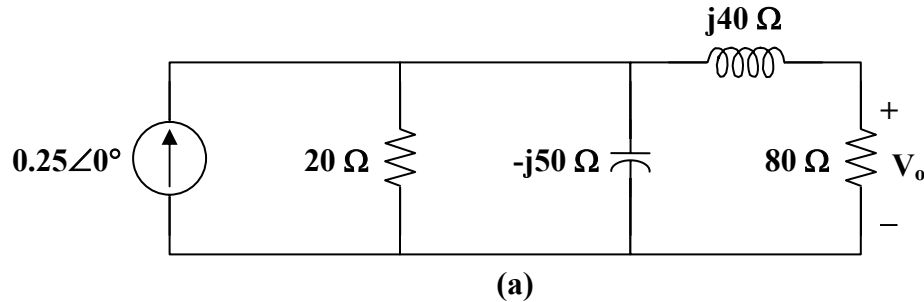
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$$5 \cos(10^5 t) \longrightarrow 5 \angle 0^\circ, \quad \omega = 10^5$$

$$0.4 \text{ mH} \longrightarrow j\omega L = j(10^5)(0.4 \times 10^{-3}) = j40$$

$$0.2 \text{ } \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10^5)(0.2 \times 10^{-6})} = -j50$$

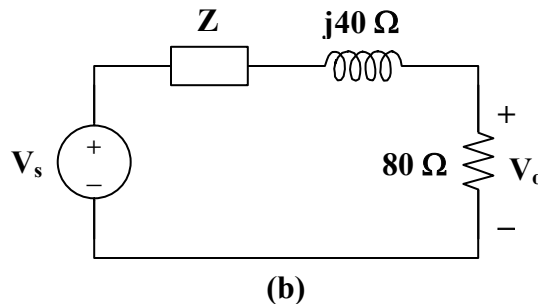
After transforming the voltage source, we get the circuit in Fig. (a).



$$\text{Let } Z = 20 \parallel -j50 = \frac{-j100}{2 - j5}$$

$$\text{and } V_s = (0.25 \angle 0^\circ) Z = \frac{-j25}{2 - j5}$$

With these, the current source is transformed to obtain the circuit in Fig.(b).



By voltage division,

$$V_o = \frac{80}{Z + 80 + j40} V_s = \frac{80}{\frac{-j100}{2 - j5} + 80 + j40} \cdot \frac{-j25}{2 - j5}$$

$$V_o = \frac{8(-j25)}{36 - j42} = 3.615 \angle -40.6^\circ$$

$$\text{Therefore, } v_o = \underline{\underline{3.615 \cos(10^5 t - 40.6^\circ) \text{ V}}}$$

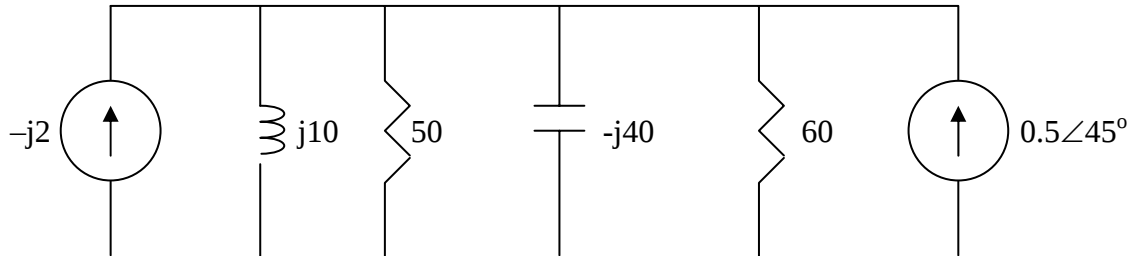
Chapter 10, Problem 51.

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Use source transformation to find I_o in the circuit of Prob. 10.42.

Chapter 10, Solution 51.

Transforming the voltage sources into current sources, we have the circuit as shown below.



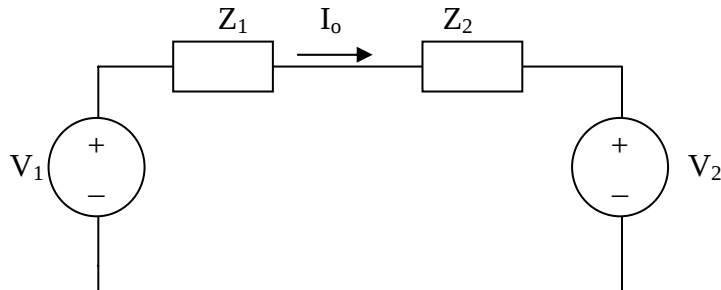
$$\text{Let } Z_1 = j10 // 50 = \frac{j10 \times 50}{50 + j10} = 1.9231 + j9.615$$

$$V_1 = -j2Z_1 = 19.231 - j3.846$$

$$\text{Let } Z_2 = -j40 // 60 = \frac{-j40 \times 60}{60 - j40} = 18.4615 - j27.6923$$

$$V_2 = Z_2 \times 0.5 \angle 45^\circ = 16.315 - j3.263$$

Transforming the current sources to voltage sources leads to the circuit below.



Applying KVL to the loop gives

$$-V_1 + I_o(Z_1 + Z_2) + V_2 = 0 \quad \longrightarrow \quad I_o = \frac{V_1 - V_2}{Z_1 + Z_2}$$

$$I_o = \frac{19.231 - j3.846 - 16.315 + j3.263}{1.9231 + j9.615 + 18.4615 - j27.6923} = \underline{0.1093 \angle 30^\circ \text{ A}} = \underline{\underline{109.3 \angle 30^\circ \text{ mA}}}$$

Chapter 10, Problem 52.

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Use the method of source transformation to find $\mathbf{I}_x$ in the circuit of Fig. 10.96.

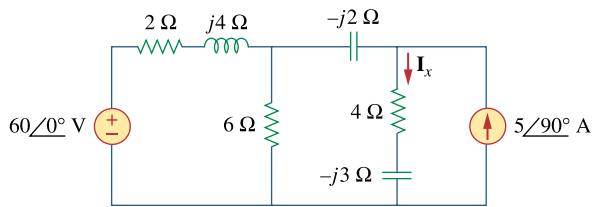


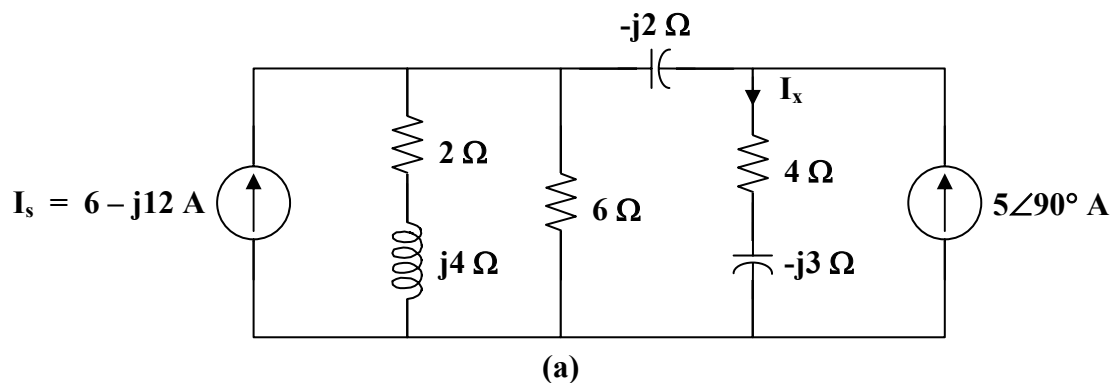
Figure 10.96
For Prob. 10.52.

Chapter 10, Solution 52.

We transform the voltage source to a current source.

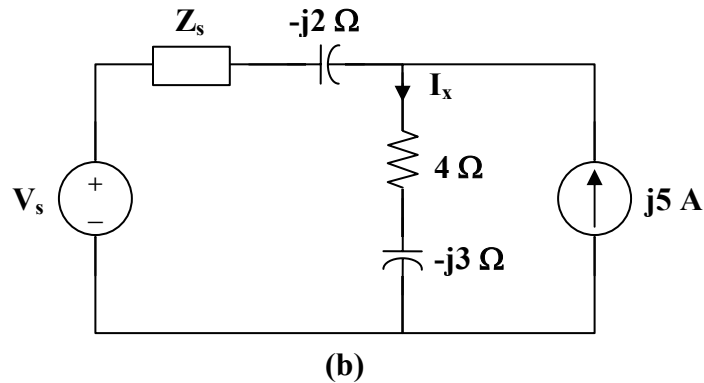
$$\mathbf{I}_s = \frac{60\angle 0^\circ}{2 + j4} = 6 - j12$$

The new circuit is shown in Fig. (a).



$$\begin{aligned} \text{Let } \mathbf{Z}_s &= 6 \parallel (2 + j4) = \frac{6(2 + j4)}{8 + j4} = 2.4 + j1.8 \\ \mathbf{V}_s &= \mathbf{I}_s \mathbf{Z}_s = (6 - j12)(2.4 + j1.8) = 36 - j18 = 18(2 - j) \end{aligned}$$

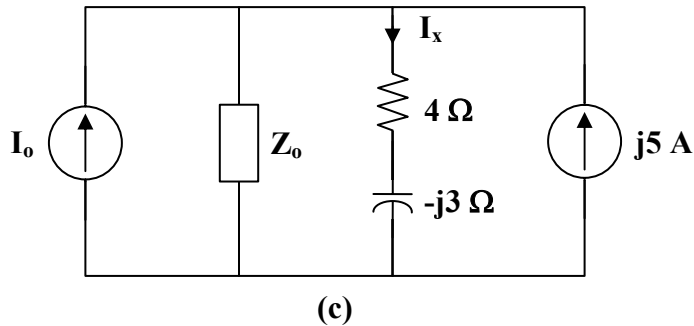
With these, we transform the current source on the left hand side of the circuit to a voltage source. We obtain the circuit in Fig. (b).



Let $Z_o = Z_s - j2 = 2.4 - j0.2 = 0.2(12 - j)$

$$I_o = \frac{V_s}{Z_o} = \frac{18(2 - j)}{0.2(12 - j)} = 15.517 - j6.207$$

With these, we transform the voltage source in Fig. (b) to a current source. We obtain the circuit in Fig. (c).



Using current division,

$$I_x = \frac{Z_o}{Z_o + 4 - j3} (I_o + j5) = \frac{2.4 - j0.2}{6.4 - j3.2} (15.517 - j1.207)$$

$$I_x = 5 + j1.5625 = \underline{\underline{5.238 \angle 17.35^\circ \text{ A}}}$$

Chapter 10, Problem 53.



Use the concept of source transformation to find V_o in the circuit of Fig. 10.97.

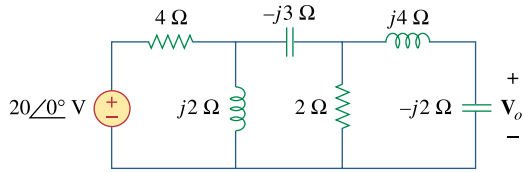
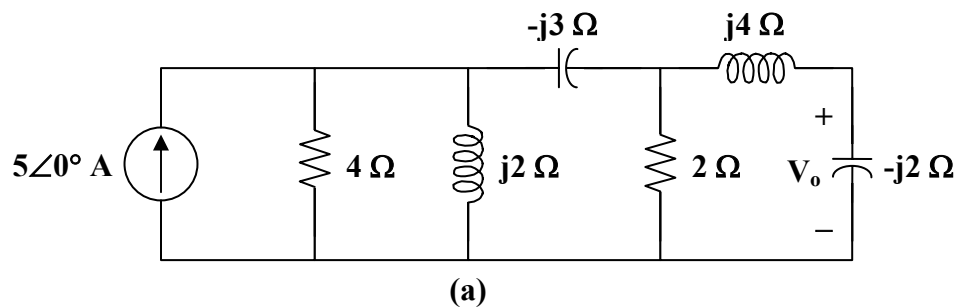


Figure 10.97

For Prob. 10.53.

Chapter 10, Solution 53.

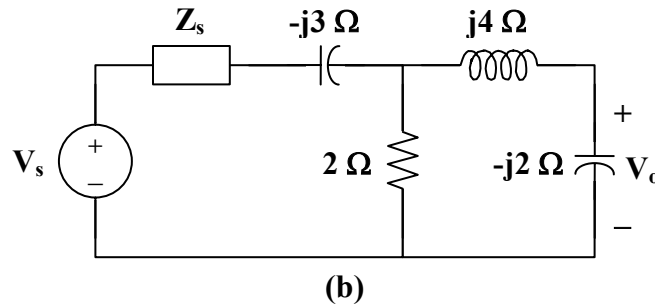
We transform the voltage source to a current source to obtain the circuit in Fig. (a).



$$\text{Let } \mathbf{Z}_s = 4 \parallel j2 = \frac{j8}{4 + j2} = 0.8 + j1.6$$

$$\mathbf{V}_s = (5\angle 0^\circ) \mathbf{Z}_s = (5)(0.8 + j1.6) = 4 + j8$$

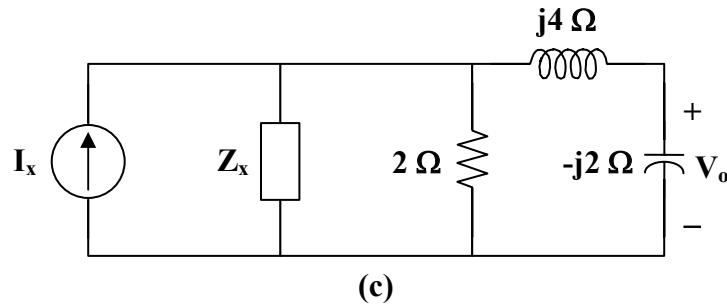
With these, the current source is transformed so that the circuit becomes that shown in Fig. (b).



Let $Z_x = Z_s - j3 = 0.8 - j1.4$

$$I_x = \frac{V_s}{Z_s} = \frac{4 + j8}{0.8 - j1.4} = -3.0769 + j4.6154$$

With these, we transform the voltage source in Fig. (b) to obtain the circuit in Fig. (c).

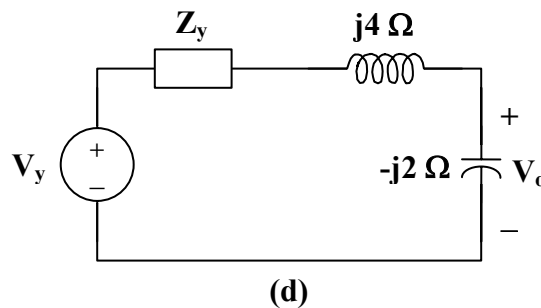


Let $Z_y = 2 \parallel Z_x = \frac{1.6 - j2.8}{2.8 - j1.4} = 0.8571 - j0.5714$

$$V_y = I_x Z_y = (-3.0769 + j4.6154) \cdot (0.8571 - j0.5714) = j5.7143$$

With these, we transform the current source to obtain the circuit in Fig. (d).

Using current division,



$$V_o = \frac{-j2}{Z_y + j4 - j2} V_y = \frac{-j2(j5.7143)}{0.8571 - j0.5714 + j4 - j2} = \underline{\underline{(3.529 - j5.883) \text{ V}}}$$

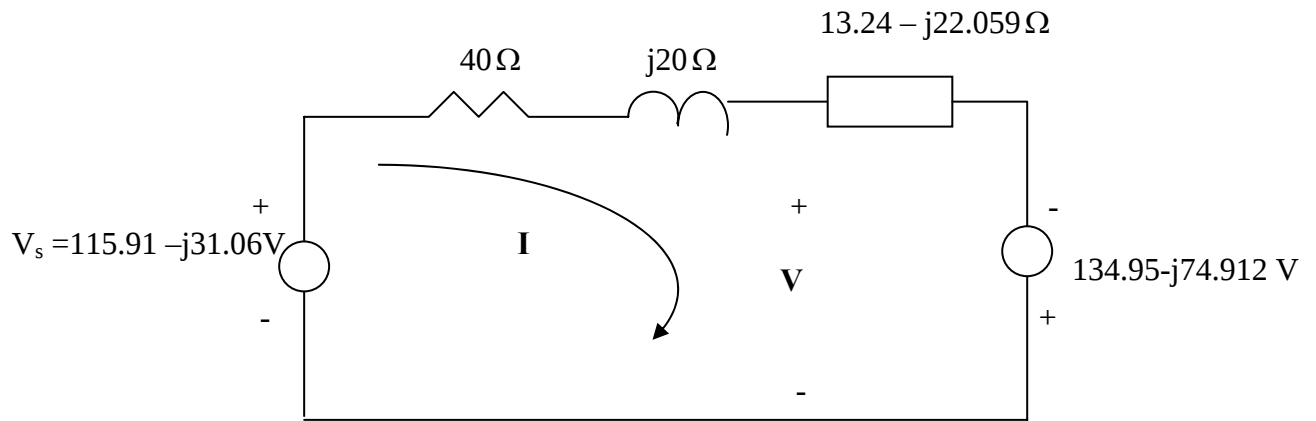
Chapter 10, Problem 54.

Rework Prob. 10.7 using source transformation.

Chapter 10, Solution 54.

$$50 // (-j30) = \frac{50 \times (-j30)}{50 - j30} = 13.24 - j22.059$$

We convert the current source to voltage source and obtain the circuit below.



Applying KVL gives

$$-115.91 + j31.058 + (53.24 - j2.059)I - 134.95 + j74.912 = 0$$

$$\text{or } I = \frac{-250.86 + j105.97}{53.24 - j2.059} = -4.7817 + j1.8055$$

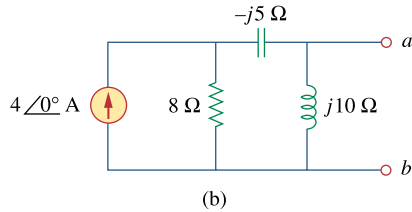
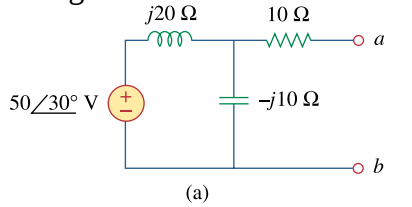
$$\text{But } -V_s + (40 + j20)I + V = 0 \quad \longrightarrow \quad V = V_s - (40 + j20)I$$

$$V = 115.91 - j31.05 - (40 + j20)(-4.7817 + j1.8055) = \underline{124.06 \angle -154^\circ \text{ V}}$$

which agrees with the result in Prob. 10.7.

Chapter 10, Problem 55.

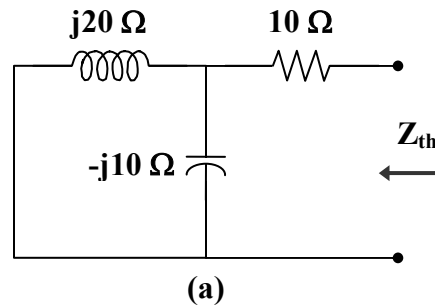
Find the Thevenin and Norton equivalent circuits at terminals a - b for each of the circuits in Fig. 10.98.

**Figure 10.98**

For Prob. 10.55.

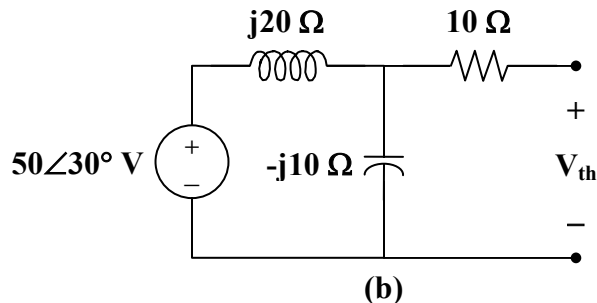
Chapter 10, Solution 55.

(a) To find Z_{th} , consider the circuit in Fig. (a).



$$\begin{aligned} Z_N = Z_{th} &= 10 + j20 \parallel (-j10) = 10 + \frac{(j20)(-j10)}{j20 - j10} \\ &= 10 - j20 = \underline{22.36\angle -63.43^\circ \Omega} \end{aligned}$$

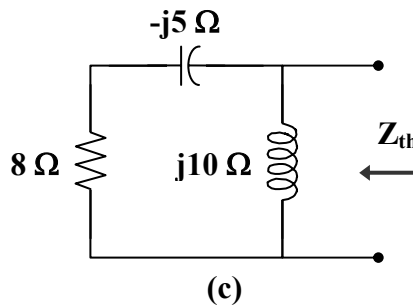
To find V_{th} , consider the circuit in Fig. (b).



$$V_{th} = \frac{-j10}{j20 - j10} (50 \angle 30^\circ) = \underline{\underline{-50 \angle 30^\circ \text{ V}}}$$

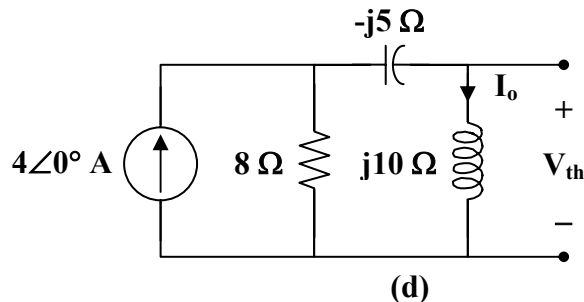
$$I_N = \frac{V_{th}}{Z_{th}} = \frac{-50 \angle 30^\circ}{22.36 \angle -63.43^\circ} = \underline{\underline{2.236 \angle 273.4^\circ \text{ A}}}$$

(b) To find Z_{th} , consider the circuit in Fig. (c).



$$Z_N = Z_{th} = j10 \parallel (8 - j5) = \frac{(j10)(8 - j5)}{j10 + 8 - j5} = \underline{\underline{10 \angle 26^\circ \Omega}}$$

To obtain V_{th} , consider the circuit in Fig. (d).



By current division,

$$I_o = \frac{8}{8 + j10 - j5} (4 \angle 0^\circ) = \frac{32}{8 + j5}$$

$$V_{th} = j10 I_o = \frac{j320}{8 + j5} = \underline{\underline{33.92 \angle 58^\circ \text{ V}}}$$

$$I_N = \frac{V_{th}}{Z_{th}} = \frac{33.92 \angle 58^\circ}{10 \angle 26^\circ} = \underline{\underline{3.392 \angle 32^\circ \text{ A}}}$$

Chapter 10, Problem 56.

For each of the circuits in Fig. 10.99, obtain Thevenin and Norton equivalent circuits at terminals a - b .

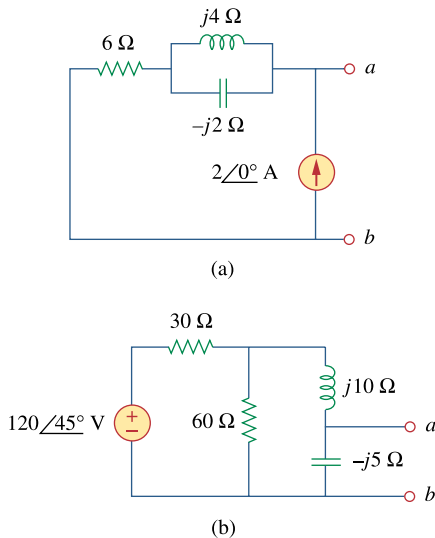
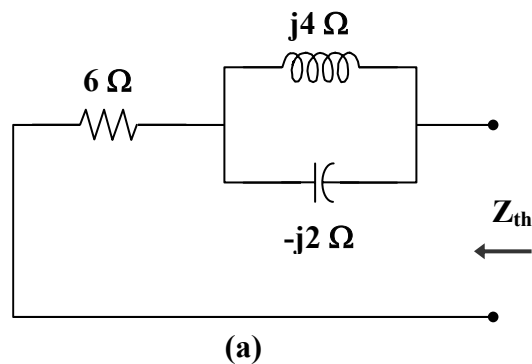


Figure 10.99

For Prob. 10.56.

Chapter 10, Solution 56.

(a) To find $\mathbf{Z}_{th}$, consider the circuit in Fig. (a).



$$\begin{aligned}\mathbf{Z}_N = \mathbf{Z}_{th} &= 6 + j4 \parallel (-j2) = 6 + \frac{(j4)(-j2)}{j4 - j2} = 6 - j4 \\ &= \underline{\underline{7.211 \angle -33.69^\circ \Omega}}\end{aligned}$$

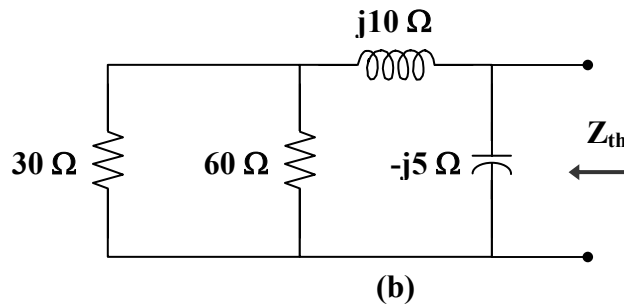
By placing short circuit at terminals a - b , we obtain,

$$\mathbf{I}_N = \underline{\underline{2 \angle 0^\circ \text{ A}}}$$

$$\mathbf{V}_{th} = \mathbf{Z}_{th} \mathbf{I}_{th} = (7.211 \angle -33.69^\circ)(2 \angle 0^\circ) = \underline{\underline{14.422 \angle -33.69^\circ \text{ V}}}$$

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(b) To find Z_{th} , consider the circuit in Fig. (b).

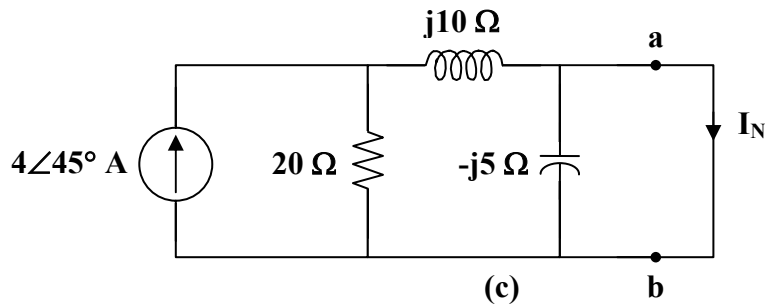


$$30 \parallel 60 = 20$$

$$Z_N = Z_{th} = -j5 \parallel (20 + j10) = \frac{(-j5)(20 + j10)}{20 + j5}$$

$$= \underline{5.423 \angle -77.47^\circ \Omega}$$

To find V_{th} and I_N , we transform the voltage source and combine the 30Ω and 60Ω resistors. The result is shown in Fig. (c).



$$I_N = \frac{20}{20 + j10} (4 \angle 45^\circ) = \frac{2}{5} (2 - j)(4 \angle 45^\circ)$$

$$= \underline{3.578 \angle 18.43^\circ \text{ A}}$$

$$V_{th} = Z_{th} I_N = (5.423 \angle -77.47^\circ) (3.578 \angle 18.43^\circ)$$

$$= \underline{19.4 \angle -59^\circ \text{ V}}$$

Chapter 10, Problem 57.

Find the Thevenin and Norton equivalent circuits for the circuit shown in Fig. 10.100.

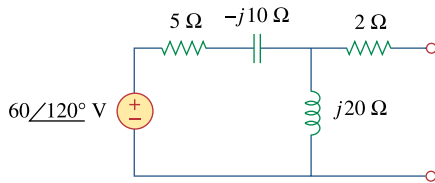
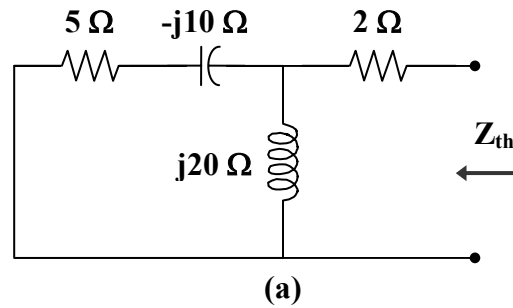


Figure 10.100
For Prob. 10.57.

Chapter 10, Solution 57.

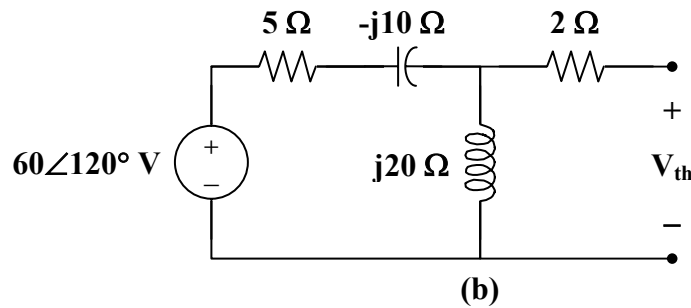
To find Z_{th} , consider the circuit in Fig. (a).



$$Z_N = Z_{th} = 2 + j20 \parallel (5 - j10) = 2 + \frac{(j20)(5 - j10)}{5 + j10}$$

$$= 18 - j12 = \underline{21.63 \angle -33.7^\circ \Omega}$$

To find V_{th} , consider the circuit in Fig. (b).



$$V_{th} = \frac{j20}{5 - j10 + j20} (60 \angle 120^\circ) = \frac{j4}{1 + j2} (60 \angle 120^\circ)$$

$$= \underline{107.3 \angle 146.56^\circ \text{ V}}$$

$$I_N = \frac{V_{th}}{Z_{th}} = \frac{107.3 \angle 146.56^\circ}{21.633 \angle -33.7^\circ} = \underline{4.961 \angle -179.7^\circ \text{ A}}$$

Chapter 10, Problem 58.

For the circuit depicted in Fig. 10.101, find the Thevenin equivalent circuit at terminals a - b .

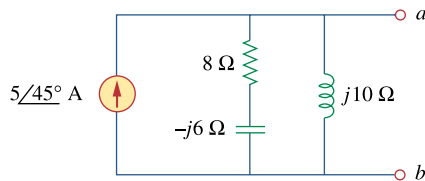
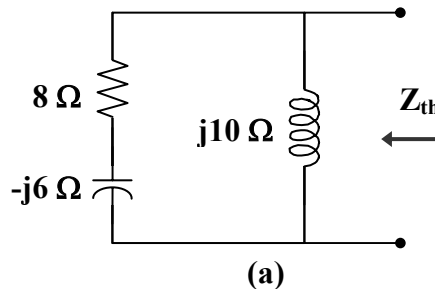


Figure 10.101

For Prob. 10.58.

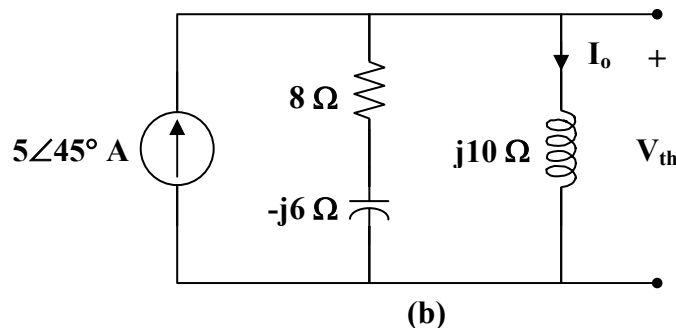
Chapter 10, Solution 58.

Consider the circuit in Fig. (a) to find $\mathbf{Z}_{th}$.



$$\begin{aligned}\mathbf{Z}_{th} &= j10 \parallel (8 - j6) = \frac{(j10)(8 - j6)}{8 + j4} = 5(2 + j) \\ &= \underline{\underline{11.18\angle 26.56^\circ\ \Omega}}\end{aligned}$$

Consider the circuit in Fig. (b) to find $\mathbf{V}_{th}$.



$$\mathbf{I}_o = \frac{8 - j6}{8 - j6 + j10} (5\angle 45^\circ) = \frac{4 - j3}{4 + j2} (5\angle 45^\circ)$$

$$\mathbf{V}_{th} = j10\mathbf{I}_o = \frac{(j10)(4 - j3)(5\angle 45^\circ)}{(2)(2 + j)} = \underline{\underline{55.9\angle 71.56^\circ\ \text{V}}}$$

Chapter 10, Problem 59.

Calculate the output impedance of the circuit shown in Fig. 10.102.

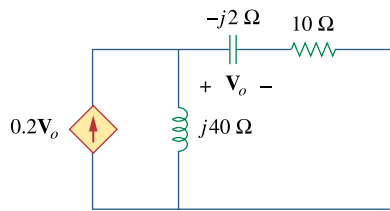
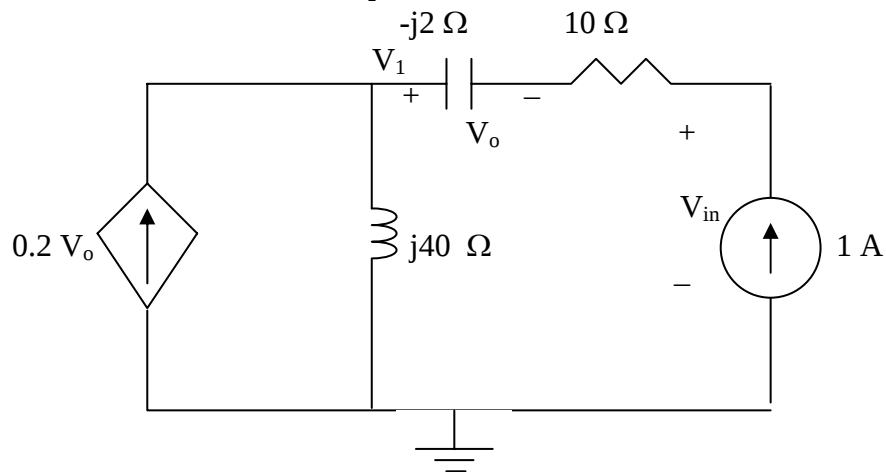


Figure 10.102
For Prob. 10.59.

Chapter 10, Solution 59.

Insert a 1-A current source at the output as shown below.



$$0.2v_o + 1 = \frac{V_1}{j40}$$

But $v_o = -1(-j2) = j2$

$$j2 \times 0.2 + 1 = \frac{V_1}{j40} \quad \longrightarrow \quad V_1 = -16 + j40$$

$$V_{in} = V_1 - V_o + 10 = -6 + j38 = 1 \times Z_{in}$$

$$Z_{in} = \underline{\underline{-6 + j38 \, \Omega.}}$$

Chapter 10, Problem 60.



Find the Thevenin equivalent of the circuit in Fig. 10.103 as seen from:

- (a) terminals a - b (b) terminals c - d

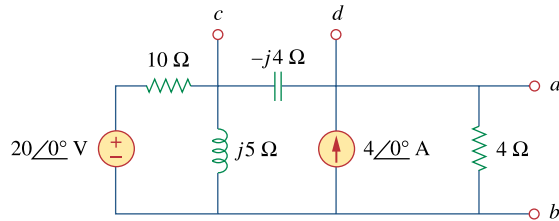
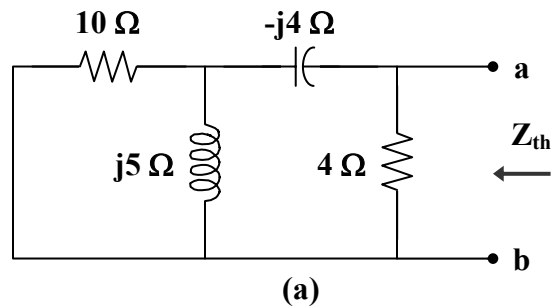


Figure 10.103

For Prob. 10.60.

Chapter 10, Solution 60.

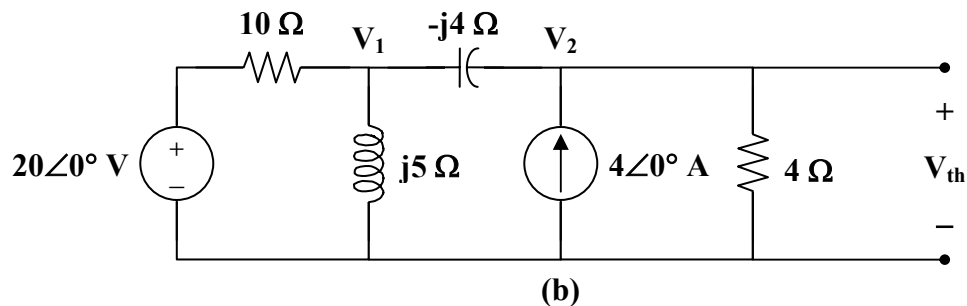
- (a) To find Z_{th} , consider the circuit in Fig. (a).



$$Z_{th} = 4 \parallel (-j4 + 10 \parallel j5) = 4 \parallel (-j4 + 2 + j4)$$

$$Z_{th} = 4 \parallel 2 = \underline{1.333 \Omega}$$

- To find V_{th} , consider the circuit in Fig. (b).



At node 1,

$$\frac{20 - V_1}{10} = \frac{V_1}{j5} + \frac{V_1 - V_2}{-j4}$$

$$(1 + j0.5)V_1 - j2.5V_2 = 20 \quad (1)$$

At node 2,

$$4 + \frac{V_1 - V_2}{-j4} = \frac{V_2}{4}$$

$$V_1 = (1 - j)V_2 + j16 \quad (2)$$

Substituting (2) into (1) leads to

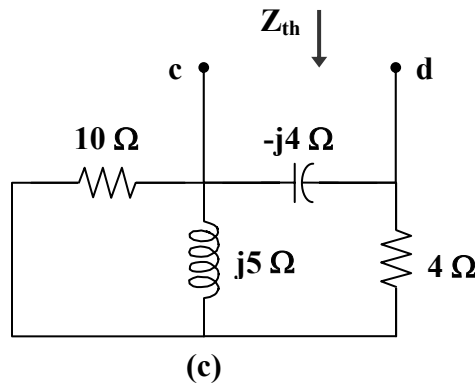
$$28 - j16 = (1.5 - j3)V_2$$

$$V_2 = \frac{28 - j16}{1.5 - j3} = 8 + j5.333$$

Therefore,

$$V_{th} = V_2 = \underline{\underline{9.615 \angle 33.69^\circ \text{ V}}}$$

(b) To find Z_{th} , consider the circuit in Fig. (c).



$$Z_{th} = -j4 \parallel (4 + 10 \parallel j5) = -j4 \parallel \left(4 + \frac{j10}{2 + j} \right)$$

$$Z_{th} = -j4 \parallel (6 + j4) = \frac{-j4}{6} (6 + j4) = \underline{\underline{2.667 - j4 \Omega}}$$

To find V_{th} , we will make use of the result in part (a).

$$V_2 = 8 + j5.333 = (8/3)(3 + j2)$$

$$V_1 = (1 - j)V_2 + j16 = j16 + (8/3)(5 - j)$$

$$V_{th} = V_1 - V_2 = 16/3 + j8 = \underline{\underline{9.614 \angle 56.31^\circ \text{ V}}}$$

Chapter 10, Problem 61.



Find the Thevenin equivalent at terminals a - b of the circuit in Fig. 10.104.

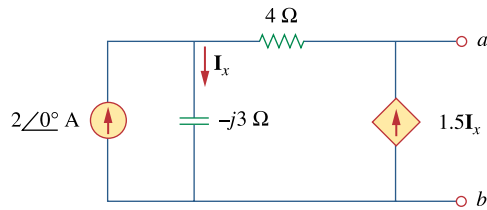
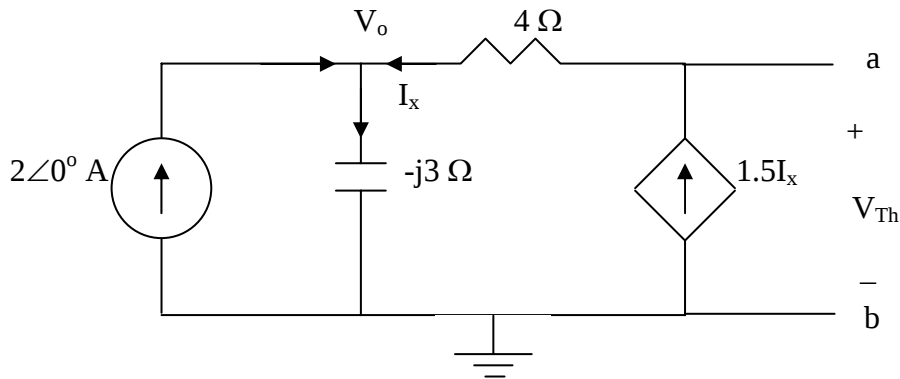


Figure 10.104

For Prob. 10.61.

Chapter 10, Solution 61.

To find V_{Th} , consider the circuit below

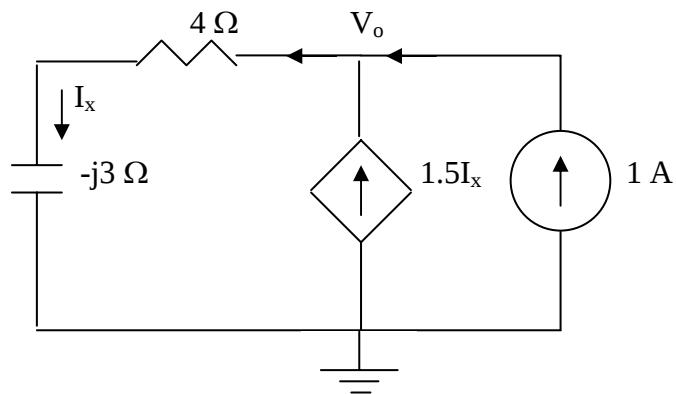


$$2 + 1.5I_x = I_x \longrightarrow I_x = -4$$

$$\text{But } V_o = -j3I_x = j12$$

$$V_{Th} = V_o + 6I_x = \underline{j12 - 24\text{ V}}$$

To find Z_{Th} , consider the circuit shown below.



$$1 + 1.5I_x = I_x \Rightarrow I_x = -2$$

$$-V_o + I_x(4 - j3) = 0 \longrightarrow V_o = -8 + j6$$

$$Z_{Th} = \frac{V_o}{1} = \underline{-8 + j6\ \Omega}$$

Chapter 10, Problem 62.



Using Thevenin's theorem, find v_o in the circuit of Fig. 10.105.

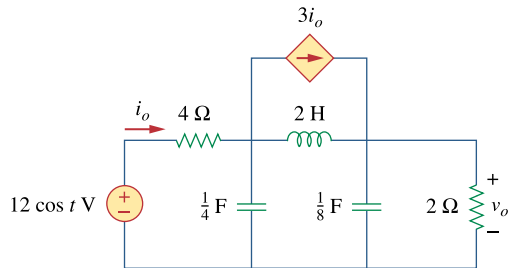


Figure 10.105

For Prob. 10.62.

Chapter 10, Solution 62.

First, we transform the circuit to the frequency domain.

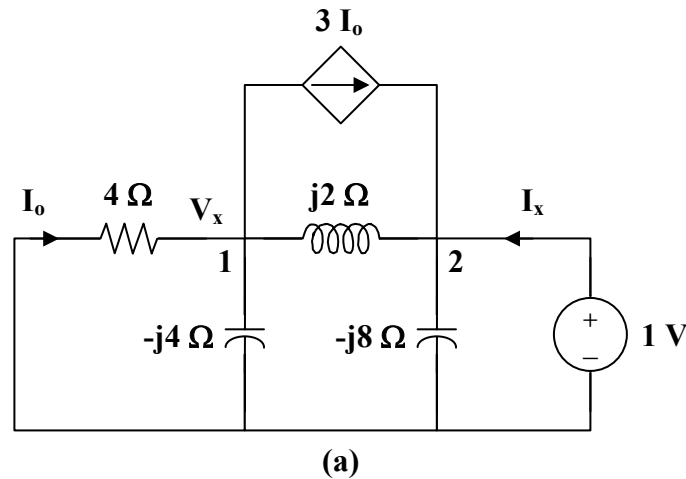
$$12 \cos(t) \longrightarrow 12 \angle 0^\circ, \quad \omega = 1$$

$$2 \text{ H} \longrightarrow j\omega L = j2$$

$$\frac{1}{4} \text{ F} \longrightarrow \frac{1}{j\omega C} = -j4$$

$$\frac{1}{8} \text{ F} \longrightarrow \frac{1}{j\omega C} = -j8$$

To find $\mathbf{Z}_{th}$, consider the circuit in Fig. (a).



At node 1,

$$\frac{\mathbf{V}_x}{4} + \frac{\mathbf{V}_x}{-j4} + 3\mathbf{I}_o = \frac{1 - \mathbf{V}_x}{j2}, \quad \text{where } \mathbf{I}_o = \frac{-\mathbf{V}_x}{4}$$

Thus,

$$\frac{\mathbf{V}_x}{-j4} - \frac{2\mathbf{V}_x}{4} = \frac{1 - \mathbf{V}_x}{j2}$$

$$\mathbf{V}_x = 0.4 + j0.8$$

At node 2,

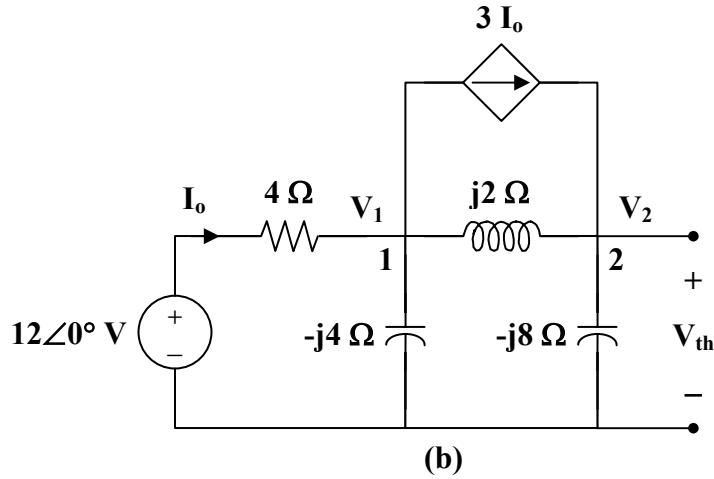
$$\mathbf{I}_x + 3\mathbf{I}_o = \frac{1}{-j8} + \frac{1 - \mathbf{V}_x}{j2}$$

$$\mathbf{I}_x = (0.75 + j0.5)\mathbf{V}_x - j\frac{3}{8}$$

$$\mathbf{I}_x = -0.1 + j0.425$$

$$\mathbf{Z}_{th} = \frac{1}{\mathbf{I}_x} = -0.5246 - j2.229 = 2.29 \angle -103.24^\circ \Omega$$

To find V_{th} , consider the circuit in Fig. (b).



At node 1,

$$\frac{12 - V_1}{4} = 3I_o + \frac{V_1}{-j4} + \frac{V_1 - V_2}{j2}, \quad \text{where } I_o = \frac{12 - V_1}{4}$$

$$24 = (2 + j)V_1 - j2V_2 \quad (1)$$

At node 2,

$$\frac{V_1 - V_2}{j2} + 3I_o = \frac{V_2}{-j8}$$

$$72 = (6 + j4)V_1 - j3V_2 \quad (2)$$

From (1) and (2),

$$\begin{bmatrix} 24 \\ 72 \end{bmatrix} = \begin{bmatrix} 2 + j & -j2 \\ 6 + j4 & -j3 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$

$$\Delta = -5 + j6,$$

$$\Delta_2 = -j24$$

$$V_{th} = V_2 = \frac{\Delta_2}{\Delta} = 3.073 \angle -219.8^\circ$$

Thus,

$$V_o = \frac{2}{2 + Z_{th}} V_{th} = \frac{(2)(3.073 \angle -219.8^\circ)}{1.4754 - j2.229}$$

$$V_o = \frac{6.146 \angle -219.8^\circ}{2.673 \angle -56.5^\circ} = 2.3 \angle -163.3^\circ$$

Therefore, $v_o = \underline{\underline{2.3 \cos(t - 163.3^\circ) \text{ V}}}$

Chapter 10, Problem 63.



Obtain the Norton equivalent of the circuit depicted in Fig. 10.106 at terminals a - b .

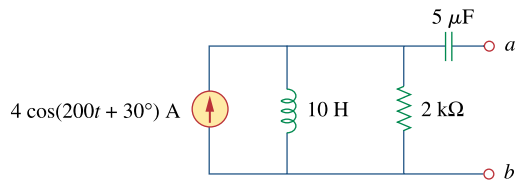


Figure 10.106

For Prob. 10.63.

Chapter 10, Solution 63.

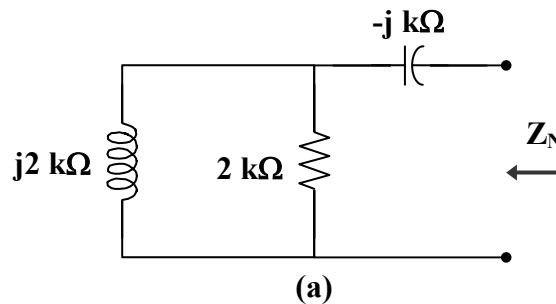
Transform the circuit to the frequency domain.

$$4 \cos(200t + 30^\circ) \longrightarrow 4 \angle 30^\circ, \quad \omega = 200$$

$$10 \text{ H} \longrightarrow j\omega L = j(200)(10) = j2 \text{ k}\Omega$$

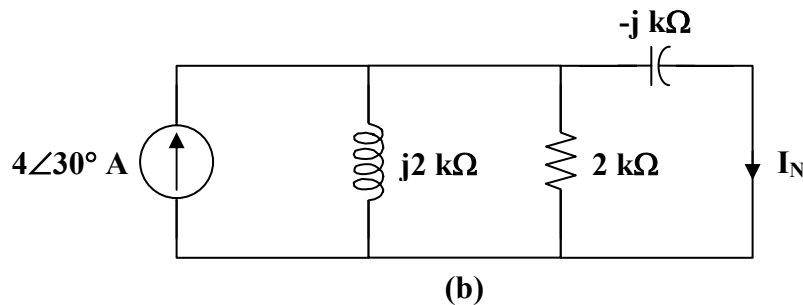
$$5 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(200)(5 \times 10^{-6})} = -j \text{ k}\Omega$$

Z_N is found using the circuit in Fig. (a).



$$Z_N = -j + 2 \parallel j2 = -j + 1 + j = 1 \text{ k}\Omega$$

We find I_N using the circuit in Fig. (b).



$$j2 \parallel 2 = 1 + j$$

By the current division principle,

$$I_N = \frac{1+j}{1+j-j} (4 \angle 30^\circ) = 5.657 \angle 75^\circ$$

Therefore,

$$i_N = \underline{5.657 \cos(200t + 75^\circ) \text{ A}}$$

$$Z_N = \underline{1 \text{ k}\Omega}$$

Chapter 10, Problem 64.



For the circuit shown in Fig. 10.107, find the Norton equivalent circuit at terminals a - b .

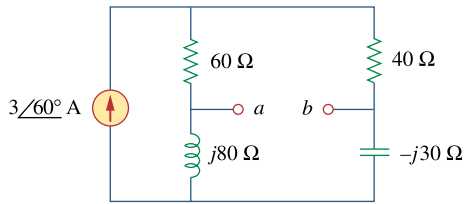
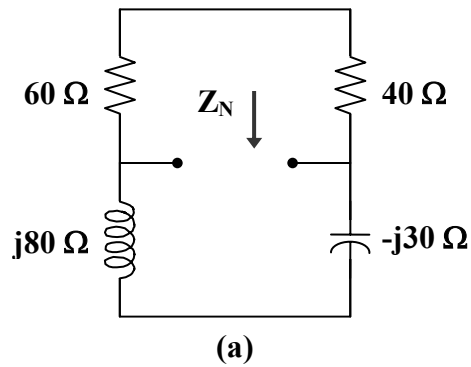


Figure 10.107

For Prob. 10.64.

Chapter 10, Solution 64.

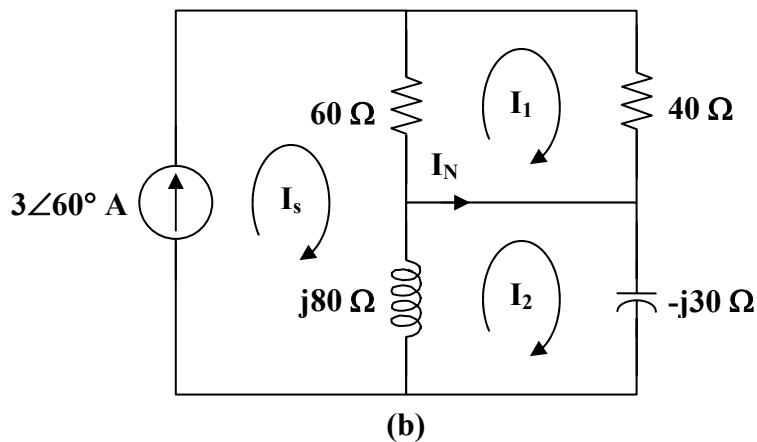
Z_N is obtained from the circuit in Fig. (a).



$$Z_N = (60 + 40) \parallel (j80 - j30) = 100 \parallel j50 = \frac{(100)(j50)}{100 + j50}$$

$$Z_N = 20 + j40 = \underline{\underline{44.72\angle 63.43^\circ \Omega}}$$

To find I_N , consider the circuit in Fig. (b).



$$I_s = 3\angle 60^\circ$$

For mesh 1,

$$100I_1 - 60I_s = 0$$

$$I_1 = 1.8\angle 60^\circ$$

For mesh 2,

$$(j80 - j30)I_2 - j80I_s = 0$$

$$I_2 = 4.8\angle 60^\circ$$

$$I_N = I_2 - I_1 = \underline{\underline{3\angle 60^\circ \text{ A}}}$$

Chapter 10, Problem 65.

Compute i_o in Fig. 10.108 using Norton's theorem.

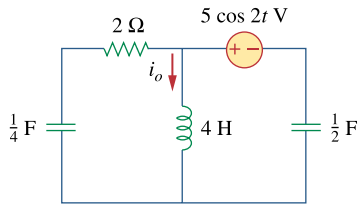
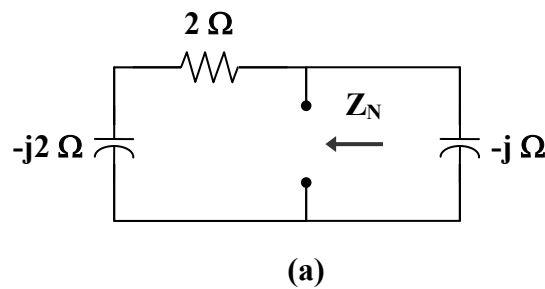


Figure 10.108
For Prob. 10.65.

Chapter 10, Solution 65.

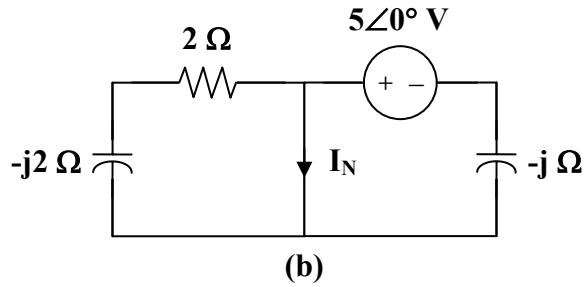
$$\begin{aligned} 5 \cos(2t) &\longrightarrow 5\angle 0^\circ, \quad \omega = 2 \\ 4 \text{ H} &\longrightarrow j\omega L = j(2)(4) = j8 \\ \frac{1}{4} \text{ F} &\longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/4)} = -j2 \\ \frac{1}{2} \text{ F} &\longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/2)} = -j \end{aligned}$$

To find $\mathbf{Z}_N$, consider the circuit in Fig. (a).



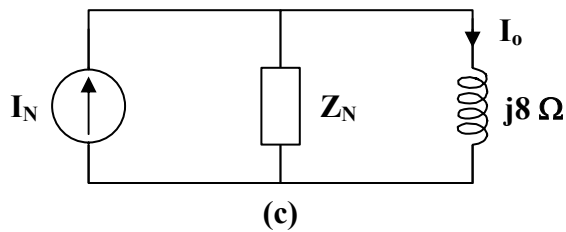
$$\mathbf{Z}_N = -j \parallel (2 - j2) = \frac{-j(2 - j2)}{2 - j3} = \frac{1}{13}(2 - j10)$$

To find $\mathbf{I}_N$, consider the circuit in Fig. (b).



$$\mathbf{I}_N = \frac{5\angle 0^\circ}{-j} = j5$$

The Norton equivalent of the circuit is shown in Fig. (c).



Using current division,

$$\mathbf{I}_o = \frac{\mathbf{Z}_N}{\mathbf{Z}_N + j8} \mathbf{I}_N = \frac{(1/13)(2 - j10)(j5)}{(1/13)(2 - j10) + j8} = \frac{50 + j10}{2 + j94}$$

$$\mathbf{I}_o = 0.1176 - j0.5294 = 0.542 \angle -77.47^\circ$$

Therefore, $i_o = \underline{\underline{542 \cos(2t - 77.47^\circ) \text{ mA}}}$

Chapter 10, Problem 66.



At terminals a - b , obtain Thevenin and Norton equivalent circuits for the network depicted in Fig. 10.109. Take $\omega = 10$ rad/s.

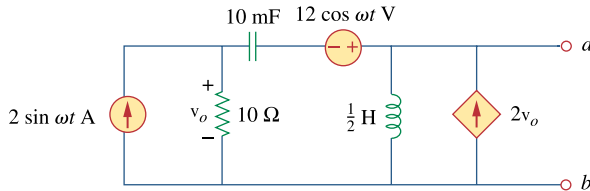


Figure 10.109

For Prob. 10.66.

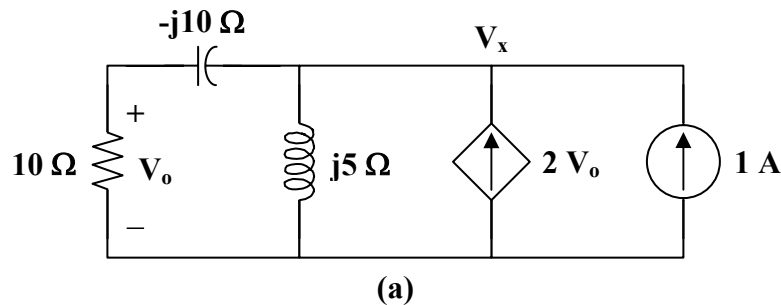
Chapter 10, Solution 66.

$$\omega = 10$$

$$0.5 \text{ H} \longrightarrow j\omega L = j(10)(0.5) = j5$$

$$10 \text{ mF} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10)(10 \times 10^{-3})} = -j10$$

To find Z_{th} , consider the circuit in Fig. (a).

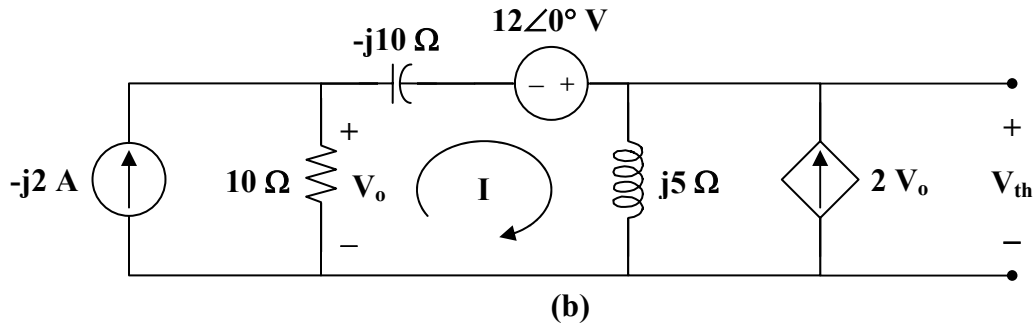


$$1 + 2V_o = \frac{V_x}{j5} + \frac{V_x}{10 - j10}, \quad \text{where } V_o = \frac{10V_x}{10 - j10}$$

$$1 + \frac{19V_x}{10 - j10} = \frac{V_x}{j5} \longrightarrow V_x = \frac{-10 + j10}{21 + j2}$$

$$Z_N = Z_{th} = \frac{V_x}{1} = \frac{14.142 \angle 135^\circ}{21.095 \angle 5.44^\circ} = \underline{\underline{0.67 \angle 129.56^\circ \Omega}}$$

To find V_{th} and I_N , consider the circuit in Fig. (b).



$$(10 - j10 + j5)I - (10)(-j2) + j5(2V_o) - 12 = 0$$

where $V_o = (10)(-j2 - I)$

Thus,

$$(10 - j105)I = -188 - j20$$

$$I = \frac{188 + j20}{-10 + j105}$$

$$V_{th} = j5(I + 2V_o) = j5(-19I - j40) = -j95I + 200$$

$$V_{th} = \frac{-j95(188 + j20)}{-10 + j105} + 200 = 29.73 + j1.8723$$

$$V_{th} = \underline{\underline{29.79\angle 3.6^\circ \text{ V}}}$$

$$I_N = \frac{V_{th}}{Z_{th}} = \frac{29.79\angle 3.6^\circ}{0.67\angle 129.56^\circ} = \underline{\underline{44.46\angle -125.96^\circ \text{ A}}}$$

Chapter 10, Problem 67.



Find the Thevenin and Norton equivalent circuits at terminals a - b in the circuit of Fig. 10.110.

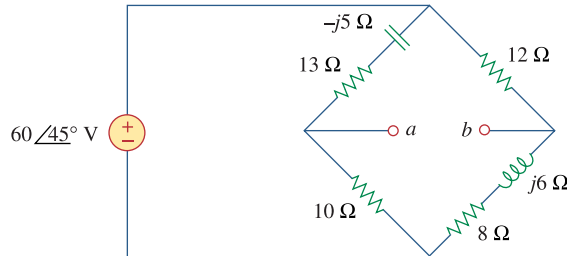


Figure 10.110
For Prob. 10.67.

Chapter 10, Solution 67.

$$Z_N = Z_{Th} = 10 \parallel (13 - j5) + 12 \parallel (8 + j6) = \frac{10(13 - j5)}{23 - j5} + \frac{12(8 + j6)}{20 + j6} = \underline{11.243 + j1.079 \Omega}$$

$$V_a = \frac{10}{23 - j5} (60 \angle 45^\circ) = 13.78 + j21.44, \quad V_b = \frac{(8 + j6)}{20 + j6} (60 \angle 45^\circ) = 12.069 + j26.08 \Omega$$

$$V_{Th} = V_a - V_b = 1.711 - j4.64 = \underline{4.945 \angle -69.76^\circ \text{ V}},$$

$$I_N = \frac{V_{Th}}{Z_{Th}} = \frac{4.945 \angle -69.76^\circ}{11.295 \angle 5.48^\circ} = \underline{0.4378 \angle -75.24^\circ \text{ A}}$$

Chapter 10, Problem 68.



Find the Thevenin equivalent at terminals $a-b$ in the circuit of Fig. 10.111.

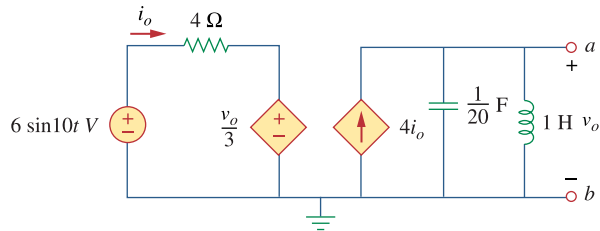
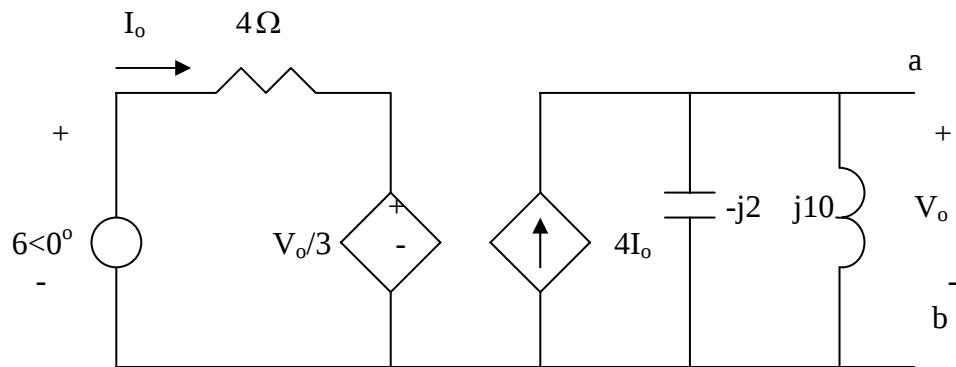


Figure 10.111
For Prob. 10.68.

Chapter 10, Solution 68.

$$\begin{aligned} 1\text{H} &\longrightarrow j\omega L = j10 \times 1 = j10 \\ \frac{1}{20}\text{F} &\longrightarrow \frac{1}{j\omega C} = \frac{1}{j10 \times \frac{1}{20}} = -j2 \end{aligned}$$

We obtain V_{Th} using the circuit below.



$$j10 // (-j2) = \frac{j10(-j2)}{j10 - j2} = -j2.5$$

$$V_o = 4I_o \times (-j2.5) = -j10I_o \quad (1)$$

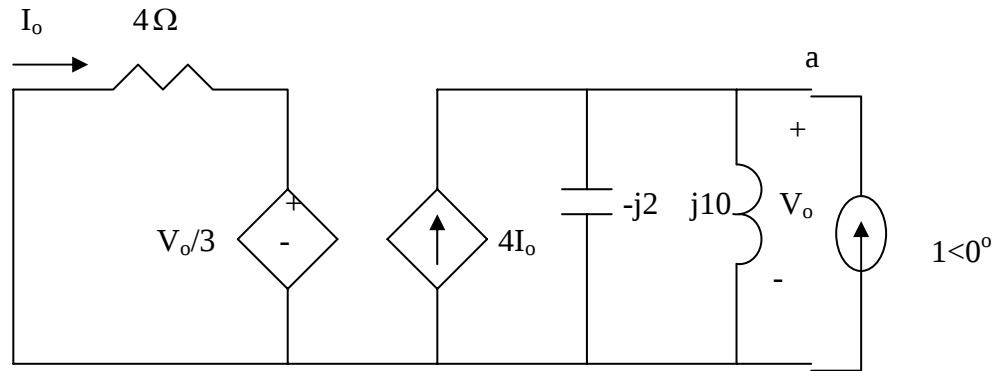
$$-6 + 4I_o + \frac{1}{3}V_o = 0 \quad (2)$$

Combining (1) and (2) gives

$$I_o = \frac{6}{4 - j10/3}, \quad V_{Th} = V_o = -j10I_o = \frac{-j60}{4 - j10/3} = 11.52 \angle -50.19^\circ$$

$$\underline{v_{Th} = 11.52 \sin(10t - 50.19^\circ)}$$

To find R_{Th} , we insert a 1-A source at terminals a-b, as shown below.



$$4I_o + \frac{1}{3}V_o = 0 \quad \longrightarrow \quad I_o = -\frac{V_o}{12}$$

$$1 + 4I_o = \frac{V_o}{-j2} + \frac{V_o}{j10}$$

Combining the two equations leads to

$$V_o = \frac{1}{0.333 + j0.4} = 1.2293 - j1.4766$$

$$Z_{Th} = \frac{V_o}{1} = \underline{1.2293 - j1.477\Omega}$$

Chapter 10, Problem 69.

For the differentiator shown in Fig. 10.112, obtain $\mathbf{V}_o/\mathbf{V}_s$. Find $v_o(t)$ when $v_s(t) = V_m \sin \omega t$ and $\omega = 1/RC$.

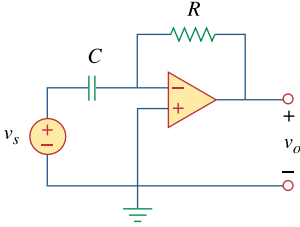


Figure 10.112
For Prob. 10.69.

Chapter 10, Solution 69.

This is an inverting op amp so that

$$\frac{\mathbf{V}_o}{\mathbf{V}_s} = \frac{-\mathbf{Z}_f}{\mathbf{Z}_i} = \frac{-R}{1/j\omega C} = \underline{\underline{-j\omega RC}}$$

When $\mathbf{V}_s = V_m$ and $\omega = 1/RC$,

$$\mathbf{V}_o = -j \cdot \frac{1}{RC} \cdot RC \cdot V_m = -jV_m = V_m \angle -90^\circ$$

Therefore,

$$v_o(t) = V_m \sin(\omega t - 90^\circ) = \underline{\underline{-V_m \cos(\omega t)}}$$

Chapter 10, Problem 70.

The circuit in Fig. 10.113 is an integrator with a feedback resistor. Calculate $v_o(t)$ if $v_s = 2 \cos 4 \times 10^4 t$ V.

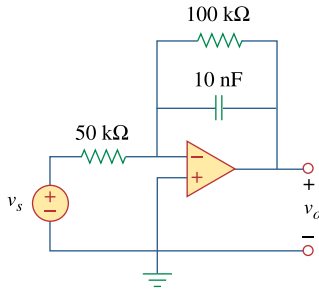


Figure 10.113
For Prob. 10.70.

Chapter 10, Solution 70.

This may also be regarded as an inverting amplifier.

$$2 \cos(4 \times 10^4 t) \longrightarrow 2 \angle 0^\circ, \quad \omega = 4 \times 10^4$$

$$10 \text{ nF} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(4 \times 10^4)(10 \times 10^{-9})} = -j2.5 \text{ k}\Omega$$

$$\frac{V_o}{V_s} = \frac{-Z_f}{Z_i}$$

$$\text{where } Z_i = 50 \text{ k}\Omega \text{ and } Z_f = 100 \text{ k} \parallel (-j2.5 \text{ k}) = \frac{-j100}{40 - j} \text{ k}\Omega.$$

$$\text{Thus, } \frac{V_o}{V_s} = \frac{j2}{40 - j}$$

$$\text{If } V_s = 2 \angle 0^\circ,$$

$$V_o = \frac{j4}{40 - j} = \frac{4 \angle 90^\circ}{40.01 \angle -1.43^\circ} = 0.1 \angle 91.43^\circ$$

Therefore,

$$v_o(t) = \underline{\underline{0.1 \cos(4 \times 10^4 t + 91.43^\circ) \text{ V}}}$$

Chapter 10, Problem 71.

Find v_o in the op amp circuit of Fig. 10.114.

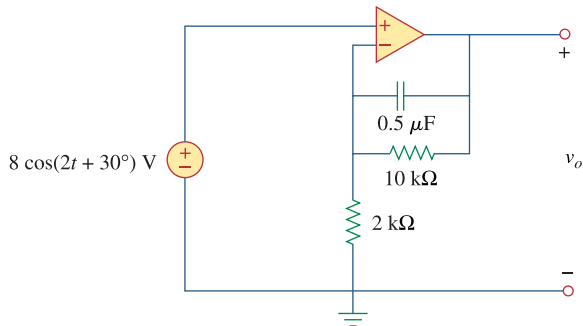


Figure 10.114
For Prob. 10.71.

Chapter 10, Solution 71.

$$8 \cos(2t + 30^\circ) \longrightarrow 8 \angle 30^\circ$$

$$0.5 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j2 \times 0.5 \times 10^{-6}} = -j1 \text{ M}\Omega$$

At the inverting terminal,

$$\frac{V_o - 8 \angle 30^\circ}{-j1000\text{k}} + \frac{V_o - 8 \angle 30^\circ}{10\text{k}} = \frac{8 \angle 30^\circ}{2\text{k}} \longrightarrow$$

$$V_o(1 - j100) = 8 \angle 30^\circ + 800 \angle -60^\circ + 4000 \angle -60^\circ$$

$$V_o = \frac{6.928 + j4 + 2400 - j4157}{1 - j100} = \frac{4800 \angle -59.9^\circ}{100 \angle -89.43^\circ} = 48 \angle 29.53^\circ$$

$$v_o(t) = \underline{\underline{48 \cos(2t + 29.53^\circ) \text{ V}}}$$

Chapter 10, Problem 72.

Compute $i_o(t)$ in the op amp circuit in Fig. 10.115 if $v_s = 4\cos 10^4 t$ V.

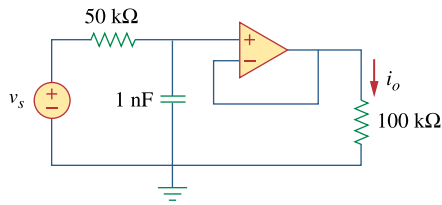


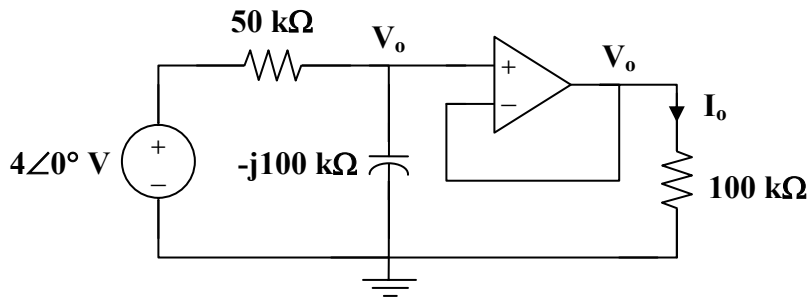
Figure 10.115
For Prob. 10.72.

Chapter 10, Solution 72.

$$4\cos(10^4 t) \longrightarrow 4\angle 0^\circ, \quad \omega = 10^4$$

$$1 \text{ nF} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10^4)(10^{-9})} = -j100 \text{ k}\Omega$$

Consider the circuit as shown below.



At the noninverting node,

$$\frac{4 - V_o}{50} = \frac{V_o}{-j100} \longrightarrow V_o = \frac{4}{1 + j0.5}$$

$$I_o = \frac{V_o}{100\text{k}} = \frac{4}{(100)(1 + j0.5)} \text{ mA} = 35.78\angle -26.56^\circ \mu\text{A}$$

Therefore,

$$i_o(t) = \underline{\underline{35.78 \cos(10^4 t - 26.56^\circ) \mu\text{A}}}$$

Chapter 10, Problem 73.

If the input impedance is defined as $Z_{in} = V_s / I_s$ find the input impedance of the op amp circuit in Fig. 10.116 when $R_1 = 10 \text{ k}\Omega$, $R_2 = 20 \text{ k}\Omega$, $C_1 = 10 \text{ nF}$, and $\omega = 5000 \text{ rad/s}$.

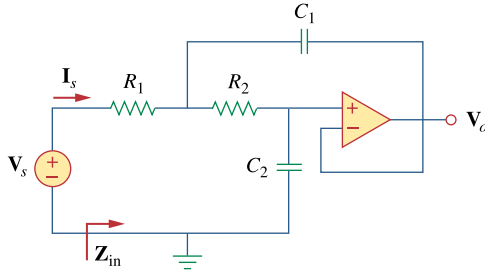


Figure 10.116
For Prob. 10.73.

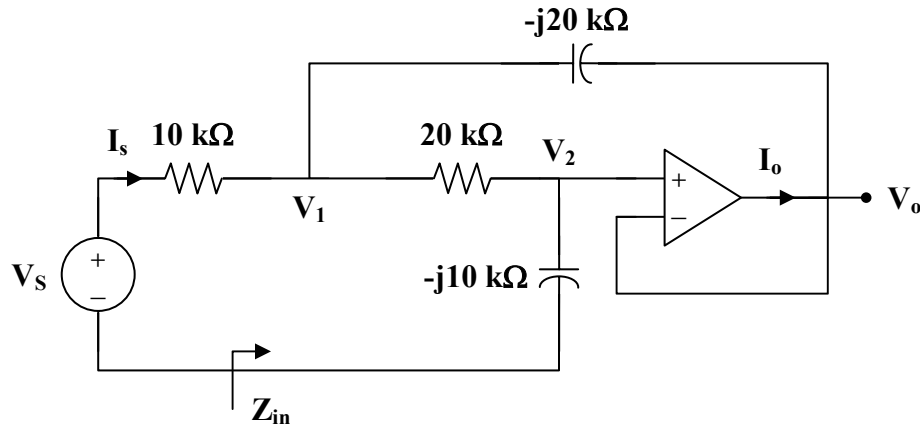
Chapter 10, Solution 73.

As a voltage follower, $V_2 = V_o$

$$C_1 = 10 \text{ nF} \longrightarrow \frac{1}{j\omega C_1} = \frac{1}{j(5 \times 10^3)(10 \times 10^{-9})} = -j20 \text{ k}\Omega$$

$$C_2 = 20 \text{ nF} \longrightarrow \frac{1}{j\omega C_2} = \frac{1}{j(5 \times 10^3)(20 \times 10^{-9})} = -j10 \text{ k}\Omega$$

Consider the circuit in the frequency domain as shown below.



At node 1,

$$\begin{aligned}\frac{V_s - V_1}{10} &= \frac{V_1 - V_o}{-j20} + \frac{V_1 - V_o}{20} \\ 2V_s &= (3 + j)V_1 - (1 + j)V_o\end{aligned}\quad (1)$$

At node 2,

$$\begin{aligned}\frac{V_1 - V_o}{20} &= \frac{V_o - 0}{-j10} \\ V_1 &= (1 + j2)V_o\end{aligned}\quad (2)$$

Substituting (2) into (1) gives

$$2V_s = j6V_o \quad \text{or} \quad V_o = -j\frac{1}{3}V_s$$

$$V_1 = (1 + j2)V_o = \left(\frac{2}{3} - j\frac{1}{3}\right)V_s$$

$$I_s = \frac{V_s - V_1}{10k} = \frac{(1/3)(1 + j)}{10k} V_s$$

$$\frac{I_s}{V_s} = \frac{1 + j}{30k}$$

$$Z_{in} = \frac{V_s}{I_s} = \frac{30k}{1 + j} = 15(1 - j)k$$

$$Z_{in} = \underline{\underline{21.21\angle -45^\circ \text{ k}\Omega}}$$

Chapter 10, Problem 74.

Evaluate the voltage gain $A_v = V_o/V_s$ in the op amp circuit of Fig. 10.117. Find A_v at $\omega = 0$, $\omega \rightarrow \infty$, $\omega = 1/R_1C_1$, and $\omega = 1/R_2C_2$.

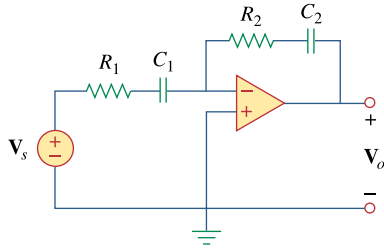


Figure 10.117
For Prob. 10.74.

Chapter 10, Solution 74.

$$Z_i = R_1 + \frac{1}{j\omega C_1},$$

$$Z_f = R_2 + \frac{1}{j\omega C_2}$$

$$A_v = \frac{V_o}{V_s} = \frac{-Z_f}{Z_i} = -\frac{R_2 + \frac{1}{j\omega C_2}}{R_1 + \frac{1}{j\omega C_1}} = -\left(\frac{C_1}{C_2}\right) \left(\frac{1 + j\omega R_2 C_2}{1 + j\omega R_1 C_1} \right)$$

$$\text{At } \omega = 0, \quad A_v = -\frac{C_1}{C_2}$$

$$\text{As } \omega \rightarrow \infty, \quad A_v = -\frac{R_2}{R_1}$$

$$\text{At } \omega = \frac{1}{R_1 C_1}, \quad A_v = -\left(\frac{C_1}{C_2}\right) \left(\frac{1 + j R_2 C_2 / R_1 C_1}{1 + j} \right)$$

$$\text{At } \omega = \frac{1}{R_2 C_2}, \quad A_v = -\left(\frac{C_1}{C_2}\right) \left(\frac{1 + j}{1 + j R_1 C_1 / R_2 C_2} \right)$$

Chapter 10, Problem 75.



In the op amp circuit of Fig. 10.118, find the closed-loop gain and phase shift of the output voltage with respect to the input voltage if $C_1 = C_2 = 1 \text{ nF}$, $R_1 = R_2 = 100 \text{ k}\Omega$, $R_3 = 20 \text{ k}\Omega$, $R_4 = 40 \text{ k}\Omega$, and $\omega = 2000 \text{ rad/s}$.

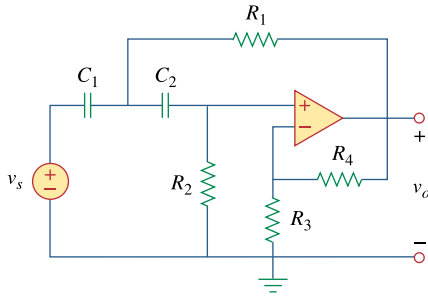


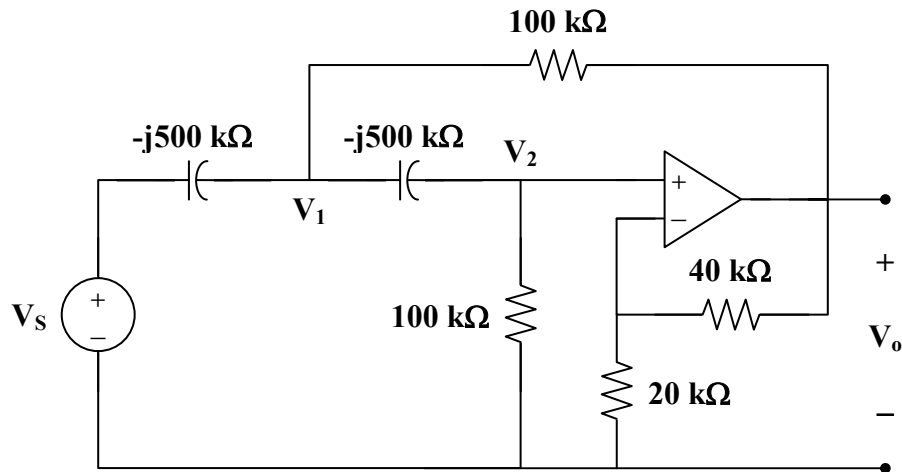
Figure 10.118
For Prob. 10.75.

Chapter 10, Solution 75.

$$\omega = 2 \times 10^3$$

$$C_1 = C_2 = 1 \text{ nF} \longrightarrow \frac{1}{j\omega C_1} = \frac{1}{j(2 \times 10^3)(1 \times 10^{-9})} = -j500 \text{ k}\Omega$$

Consider the circuit shown below.



Let $V_s = 10\text{V}$.

At node 1,

$$\begin{aligned} &[(V_1 - 10)/(-j500\text{k})] + [(V_1 - V_o)/10^5] + [(V_1 - V_2)/(-j500\text{k})] = 0 \\ &\text{or } (1 + j0.4)V_1 - j0.2V_2 - V_o = j2 \end{aligned} \quad (1)$$

At node 2,

$$\begin{aligned} &[(V_2 - V_1)/(-j5)] + (V_2 - 0) = 0 \\ &\text{or } -j0.2V_1 + (1 + j0.2)V_2 = 0 \text{ or } V_1 = (1 - j5)V_2 \end{aligned} \quad (2)$$

But

$$V_2 = \frac{R_3}{R_3 + R_4} V_o = \frac{V_o}{3} \quad (3)$$

From (2) and (3),

$$V_1 = (0.3333 - j1.6667)V_o \quad (4)$$

Substituting (3) and (4) into (1),

$$(1+j0.4)(0.3333-j1.6667)V_o - j0.06667V_o - V_o = j2$$

$$(1.077\angle 21.8^\circ)(1.6997\angle -78.69^\circ) = 1.8306\angle -56.89^\circ = 1 - j1.5334$$

Thus,

$$(1-j1.5334)V_o - j0.06667V_o - V_o = j2$$

$$\text{and, } V_o = j2/(-j1.6601) = -1.2499 = 1.2499\angle 180^\circ \text{ V}$$

Since $V_s = 10$,

$$V_o/V_s = \underline{\underline{0.12499\angle 180^\circ}}.$$

Checking with MATLAB.

```
>> Y=[1+0.4i,-0.2i,-1;1,-1+5i,0;0,-3,1]
```

Y =

```
1.0000 + 0.4000i    0 - 0.2000i -1.0000
1.0000    -1.0000 + 5.0000i    0
0    -3.0000    1.0000
```

```
>> I=[2i;0;0]
```

I =

```
0 + 2.0000i
0
0
```

```
>> V=inv(Y)*I
```

V =

```
-0.4167 + 2.0833i
-0.4167
-1.2500 + 0.0000i (this last term is v_o)
```

and, the answer checks.

Chapter 10, Problem 76.



Determine V_o and I_o in the op amp circuit of Fig. 10.119.

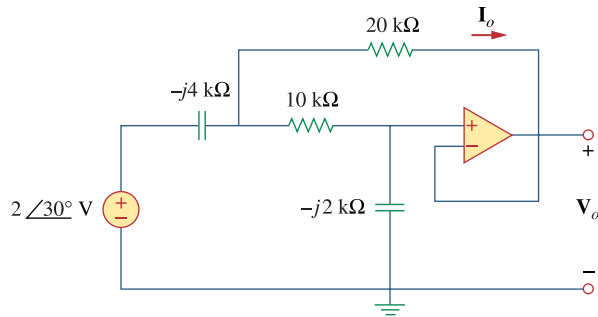


Figure 10.119
For Prob. 10.76.

Chapter 10, Solution 76.

Let the voltage between the $-jk\Omega$ capacitor and the $10k\Omega$ resistor be V_1 .

$$\begin{aligned}\frac{2\angle 30^\circ - V_1}{-j4k} &= \frac{V_1 - V_o}{10k} + \frac{V_1 - V_o}{20k} \longrightarrow \\ 2\angle 30^\circ &= (1 - j0.6)V_1 + j0.6V_o \\ &= 1.7321 + j1\end{aligned}\quad (1)$$

Also,

$$\frac{V_1 - V_o}{10k} = \frac{V_o}{-j2k} \longrightarrow V_1 = (1 + j5)V_o \quad (2)$$

Solving (2) into (1) yields

$$\begin{aligned}2\angle 30^\circ &= (1 - j0.6)(1 + j5)V_o + j0.6V_o = (1 + 3 - j0.6 + j5 + j6)V_o \\ &= (4 + j5)V_o \\ V_o &= \frac{2\angle 30^\circ}{6.403\angle 51.34^\circ} = \underline{0.3124\angle -21.34^\circ \text{ V}}\end{aligned}$$

```
>> Y=[1-0.6i,0.6i;1,-1-0.5i]
```

Y =

$$\begin{bmatrix} 1.0000 - 0.6000i & 0 + 0.6000i \\ 1.0000 & -1.0000 - 5.0000i \end{bmatrix}$$

```
>> I=[1.7321+1i;0]
```

I =

$$\begin{bmatrix} 1.7321 + 1.0000i \\ 0 \end{bmatrix}$$

```
>> V=inv(Y)*I
```

V =

$$\begin{bmatrix} 0.8593 + 1.3410i \\ 0.2909 - 0.1137i \end{bmatrix} = V_o = 0.3123\angle -21.35^\circ \text{ V. Answer checks.}$$

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Chapter 10, Problem 77.



Compute the closed-loop gain V_o/V_s for the op amp circuit of Fig. 10.120.

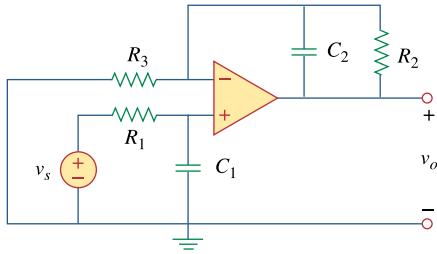
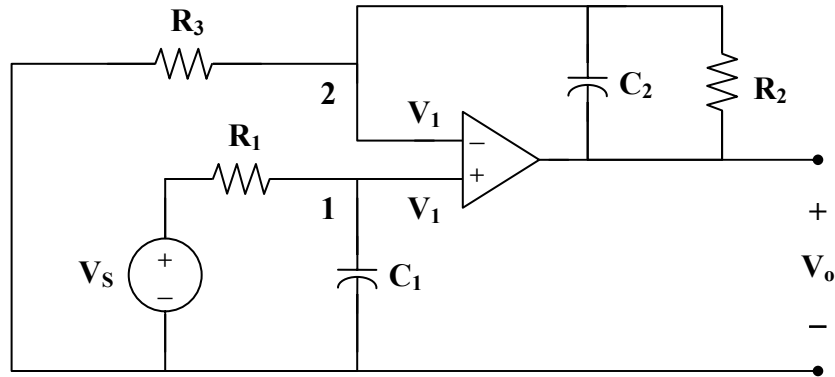


Figure 10.120
For Prob. 10.77.

Chapter 10, Solution 77.

Consider the circuit below.



At node 1,

$$\begin{aligned}\frac{V_s - V_1}{R_1} &= j\omega C_1 V_1 \\ V_s &= (1 + j\omega R_1 C_1) V_1\end{aligned}\quad (1)$$

At node 2,

$$\begin{aligned}\frac{0 - V_1}{R_3} &= \frac{V_1 - V_o}{R_2} + j\omega C_2 (V_1 - V_o) \\ V_1 &= (V_o - V_1) \left(\frac{R_3}{R_2} + j\omega C_2 R_3 \right) \\ V_o &= \left(1 + \frac{1}{(R_3/R_2) + j\omega C_2 R_3} \right) V_1\end{aligned}\quad (2)$$

From (1) and (2),

$$\begin{aligned}V_o &= \frac{V_s}{1 + j\omega R_1 C_1} \left(1 + \frac{R_2}{R_3 + j\omega C_2 R_2 R_3} \right) \\ \frac{V_o}{V_s} &= \frac{R_2 + R_3 + j\omega C_2 R_2 R_3}{(1 + j\omega R_1 C_1)(R_3 + j\omega C_2 R_2 R_3)}\end{aligned}$$

Chapter 10, Problem 78.



Determine $v_o(t)$ in the op amp circuit in Fig. 10.121 below.

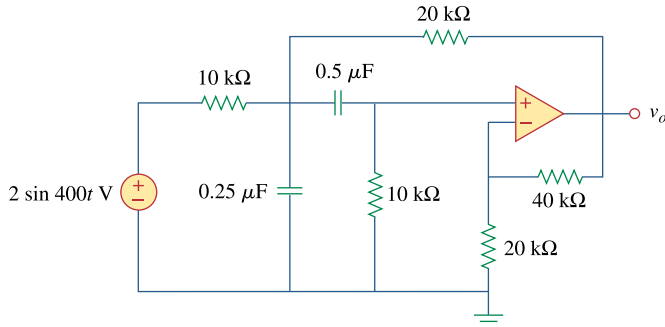


Figure 10.121

For Prob. 10.78.

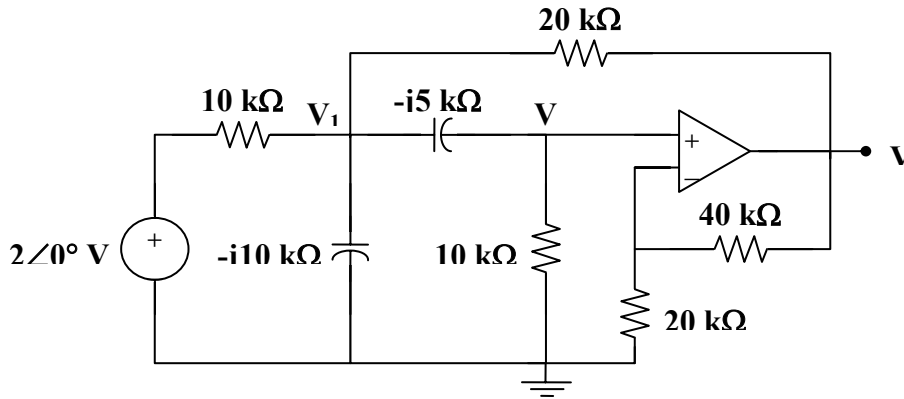
Chapter 10, Solution 78.

$$2 \sin(400t) \longrightarrow 2 \angle 0^\circ, \quad \omega = 400$$

$$0.5 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(400)(0.5 \times 10^{-6})} = -j5 \text{ k}\Omega$$

$$0.25 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(400)(0.25 \times 10^{-6})} = -j10 \text{ k}\Omega$$

Consider the circuit as shown below.



At node 1,

$$\begin{aligned} \frac{2 - V_1}{10} &= \frac{V_1}{-j10} + \frac{V_1 - V_2}{-j5} + \frac{V_1 - V_o}{20} \\ 4 &= (3 + j6)V_1 - j4V_2 - V_o \end{aligned} \quad (1)$$

At node 2,

$$\begin{aligned} \frac{V_1 - V_2}{-j5} &= \frac{V_2}{10} \\ V_1 &= (1 - j0.5)V_2 \end{aligned} \quad (2)$$

But

$$V_2 = \frac{20}{20 + 40} V_o = \frac{1}{3} V_o \quad (3)$$

From (2) and (3),

$$V_1 = \frac{1}{3} \cdot (1 - j0.5) V_o \quad (4)$$

Substituting (3) and (4) into (1) gives

$$\begin{aligned} 4 &= (3 + j6) \cdot \frac{1}{3} \cdot (1 - j0.5) V_o - j\frac{4}{3} V_o - V_o = \left(1 + j\frac{1}{6}\right) V_o \\ V_o &= \frac{24}{6 + j} = 3.945 \angle -9.46^\circ \end{aligned}$$

Therefore,

$$v_o(t) = \underline{\underline{3.945 \sin(400t - 9.46^\circ) \text{ V}}}$$

Chapter 10, Problem 79.

For the op amp circuit in Fig. 10.122, obtain $v_o(t)$.

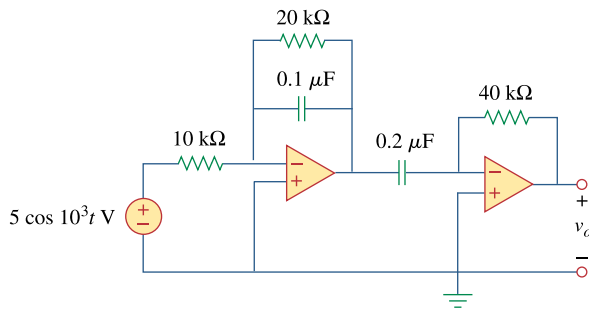


Figure 10.122
For Prob. 10.79.

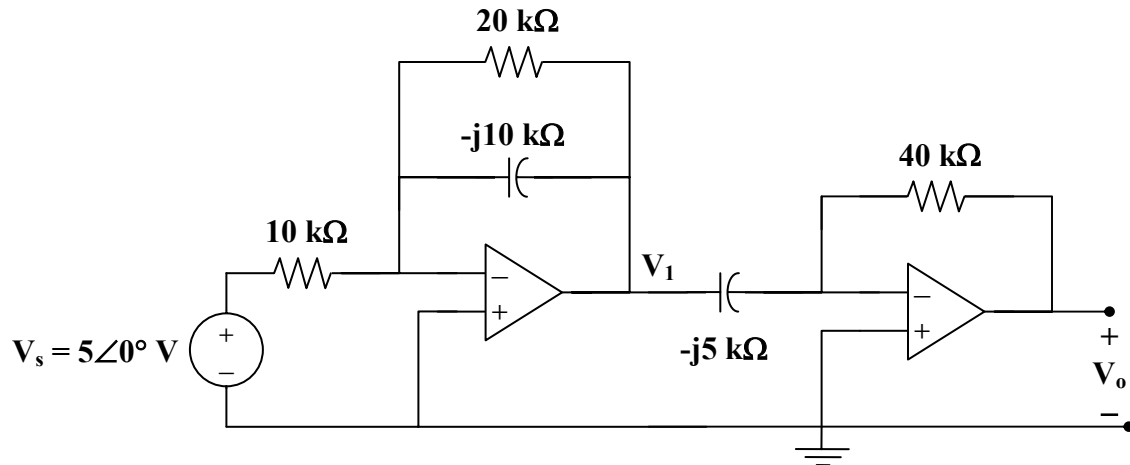
Chapter 10, Solution 79.

$$5 \cos(1000t) \longrightarrow 5 \angle 0^\circ, \quad \omega = 1000$$

$$0.1 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(1000)(0.1 \times 10^{-6})} = -j10 \text{ k}\Omega$$

$$0.2 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(1000)(0.2 \times 10^{-6})} = -j5 \text{ k}\Omega$$

Consider the circuit shown below.



Since each stage is an inverter, we apply $V_o = \frac{-Z_f}{Z_i} V_i$ to each stage.

$$V_o = \frac{-40}{-j5} V_1 \quad (1)$$

and

$$V_1 = \frac{-20 \parallel (-j10)}{10} V_s \quad (2)$$

From (1) and (2),

$$V_o = \left(\frac{-j8}{10} \right) \left(\frac{-(20)(-j10)}{20 - j10} \right) 5 \angle 0^\circ$$

$$V_o = 16(2 + j) = 35.78 \angle 26.56^\circ$$

Therefore, $v_o(t) = \underline{\underline{35.78 \cos(1000t + 26.56^\circ) \text{ V}}}$

Chapter 10, Problem 80.



Obtain $v_o(t)$ for the op amp circuit in Fig. 10.123 if $v_s = 4\cos(1000t - 60^\circ)$ V.

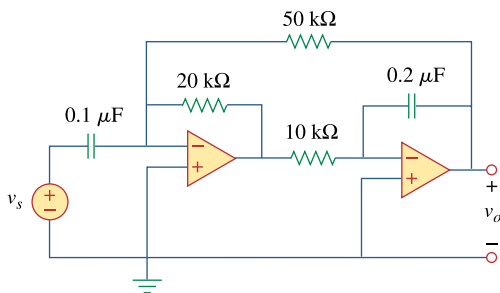


Figure 10.123

For Prob. 10.80.

Chapter 10, Solution 80.

$$4\cos(1000t - 60^\circ) \longrightarrow 4\angle -60^\circ, \quad \omega = 1000$$

$$0.1 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(1000)(0.1 \times 10^{-6})} = -j10 \text{ k}\Omega$$

$$0.2 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(1000)(0.2 \times 10^{-6})} = -j5 \text{ k}\Omega$$

The two stages are inverters so that

$$\mathbf{V}_o = \left(\frac{20}{-j10} \cdot (4\angle -60^\circ) + \frac{20}{50} \mathbf{V}_o \right) \left(\frac{-j5}{10} \right)$$

$$= \frac{-j}{2} \cdot (j2) \cdot (4\angle -60^\circ) + \frac{-j}{2} \cdot \frac{2}{5} \mathbf{V}_o$$

$$(1 + j/5) \mathbf{V}_o = 4\angle -60^\circ$$

$$\mathbf{V}_o = \frac{4\angle -60^\circ}{1 + j/5} = 3.922\angle -71.31^\circ$$

Therefore, $v_o(t) = \underline{\underline{3.922 \cos(1000t - 71.31^\circ) \text{ V}}}$

Chapter 10, Problem 81.



Use *PSpice* to determine V_o in the circuit of Fig. 10.124. Assume $\omega = 1$ rad/s.

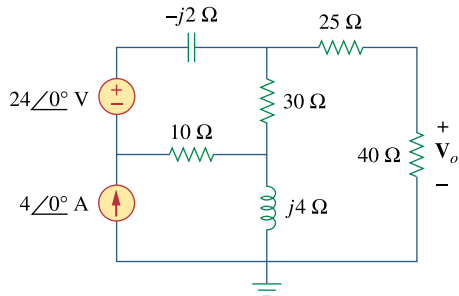


Figure 10.124
For Prob. 10.81.

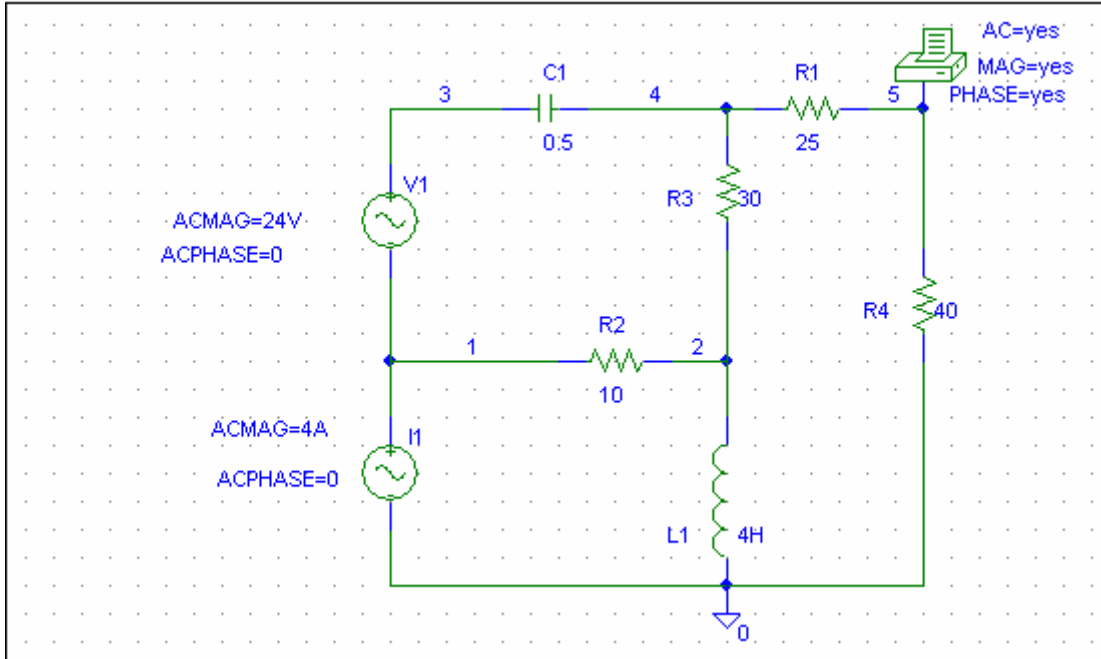
Chapter 10, Solution 81.

We need to get the capacitance and inductance corresponding to $-j2\ \Omega$ and $j4\ \Omega$.

$$-j2 \longrightarrow C = \frac{1}{\omega X_c} = \frac{1}{1 \times 2} = 0.5F$$

$$j4 \longrightarrow L = \frac{X_L}{\omega} = 4H$$

The schematic is shown below.



When the circuit is simulated, we obtain the following from the output file.

FREQ	VM(5)	VP(5)
1.592E-01	1.127E+01	-1.281E+02

From this, we obtain

$$V_o = \underline{11.27 \angle 128.1^\circ \text{ V.}}$$

Chapter 10, Problem 82.

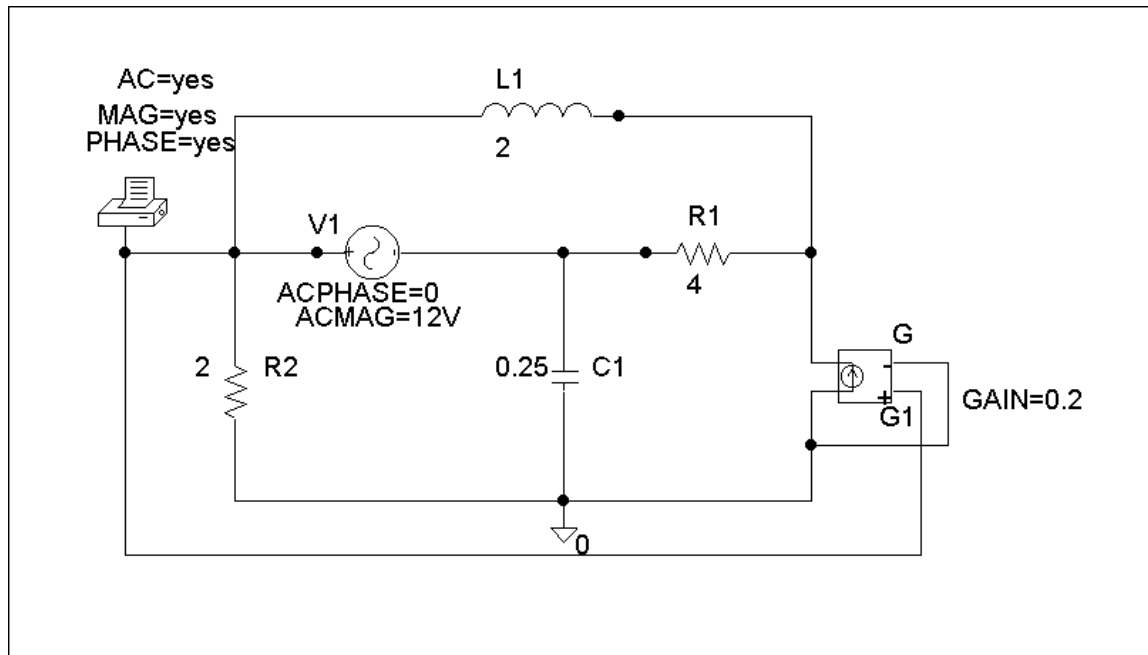
Solve Prob. 10.19 using *PSpice*.

Chapter 10, Solution 82.

The schematic is shown below. We insert PRINT to print V_o in the output file. For AC Sweep, we set Total Pts = 1, Start Freq = 0.1592, and End Freq = 0.1592. After simulation, we print out the output file which includes:

FREQ	VM(\$N_0001)	VP(\$N_0001)
1.592 E-01	7.684 E+00	5.019 E+01

which means that $V_o = \underline{7.684 \angle 50.19^\circ \text{ V}}$



Chapter 10, Problem 83.

Use *PSpice* to find $v_o(t)$ in the circuit of Fig. 10.125. Let $i_s = 2 \cos(10_3 t)$ A.

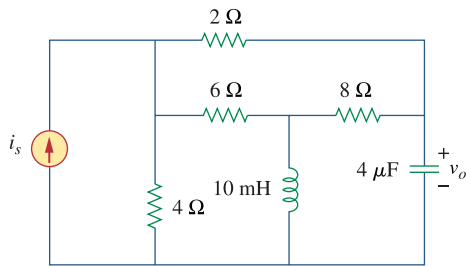
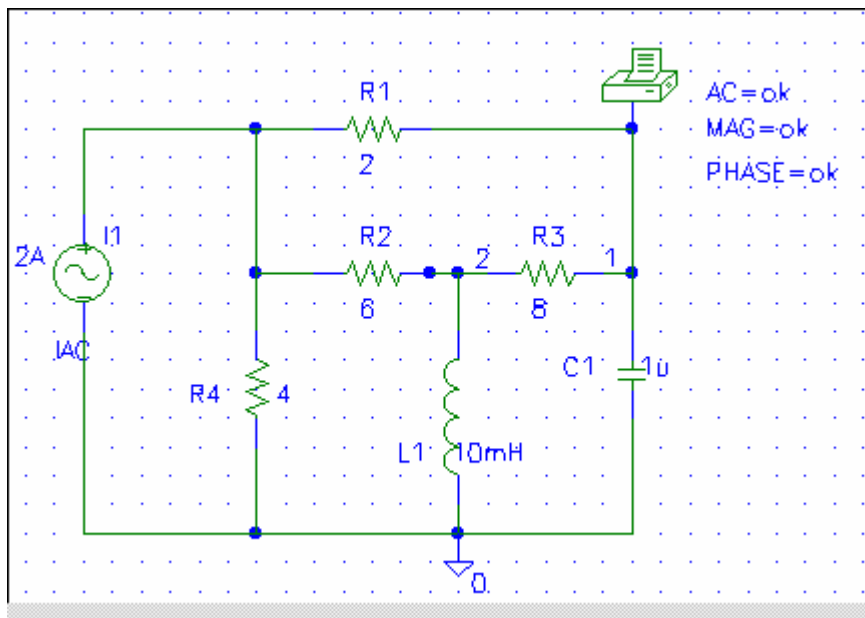


Figure 10.125

For Prob. 10.83.

Chapter 10, Solution 83.

The schematic is shown below. The frequency is $f = \omega / 2\pi = \frac{1000}{2\pi} = 159.15$



When the circuit is saved and simulated, we obtain from the output file

FREQ	VM(1)	VP(1)
1.592E+02	6.611E+00	-1.592E+02

Thus,

$$v_o = \underline{\underline{6.611 \cos(1000t - 159.2^\circ) \text{ V}}}$$

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Chapter 10, Problem 84.

Obtain V_o in the circuit of Fig. 10.126 using *PSpice*.

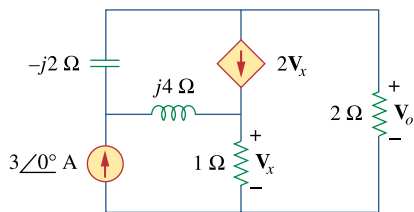


Figure 10.126

For Prob. 10.84.

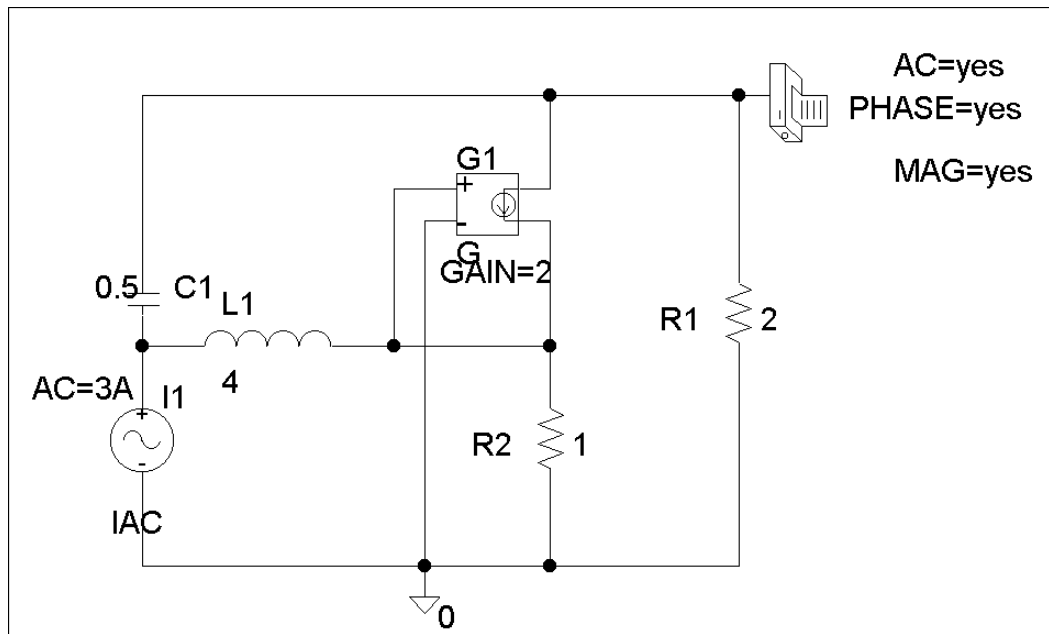
Chapter 10, Solution 84.

The schematic is shown below. We set PRINT to print V_o in the output file. In AC Sweep box, we set Total Pts = 1, Start Freq = 0.1592, and End Freq = 0.1592. After simulation, we obtain the output file which includes:

VP(\$N_0003)	FREQ	VM(\$N_0003)	
	1.592 E-01	1.664 E+00	-1.646
E+02			

Namely,

$$V_o = \underline{1.664 \angle -146.4^\circ \text{ V}}$$



Chapter 10, Problem 85.

Use *PSpice* to find V_o in the circuit of Fig. 10.127.

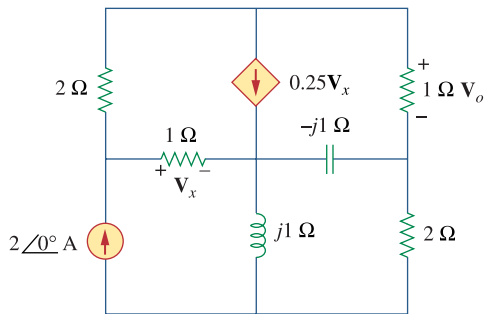
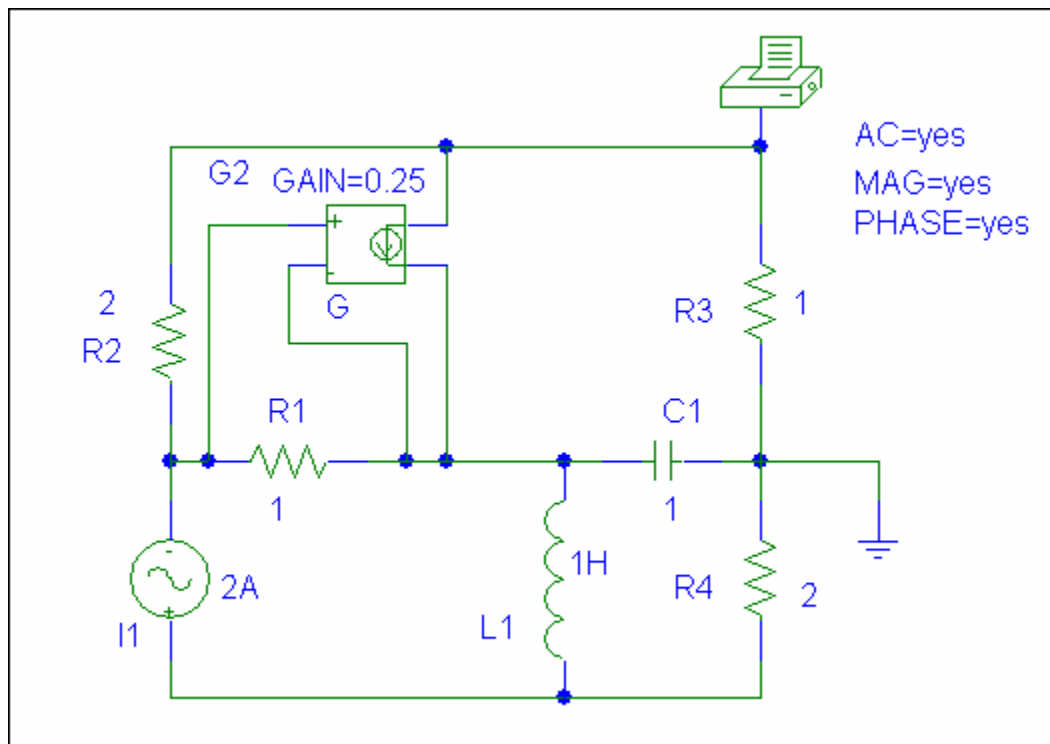


Figure 10.127
For Prob. 10.85.

Chapter 10, Solution 85.

The schematic is shown below. We let $\omega = 1$ rad/s so that $L=1$ H and $C=1$ F.



When the circuit is saved and simulated, we obtain from the output file

```
FREQ      VM($N_0001) VP($N_0001)
1.592E-01  4.471E-01  1.437E+01
```

From this, we conclude that

$$V_o = \underline{447.1 \angle 14.37^\circ \text{ mV}}$$

Checking using MATLAB and nodal analysis we get,

```
>> Y=[1.5,-0.25,-0.25,0;0,1.25,-1.25,1i;-0.5,-1,1.5,0;0,1i,0,0.5-1i]
```

Y =

```
1.5000    -0.2500    -0.2500         0
         0     1.2500    -1.2500    0 + 1.0000i
-0.5000    -1.0000     1.5000         0
         0     0 + 1.0000i         0    0.5000 - 1.0000i
```

```
>> I=[0;0;2;-2]
```

I =

```
0
0
2
-2
```

```
>> V=inv(Y)*I
```

V =

```
0.4331 + 0.1110i = V_o = 0.4471∠14.38°, answer checks.
0.6724 + 0.3775i
1.9260 + 0.2887i
-0.1110 - 1.5669i
```

Chapter 10, Problem 86.

Use *PSpice* to find V_1 , V_2 , and V_3 in the network of Fig. 10.128.

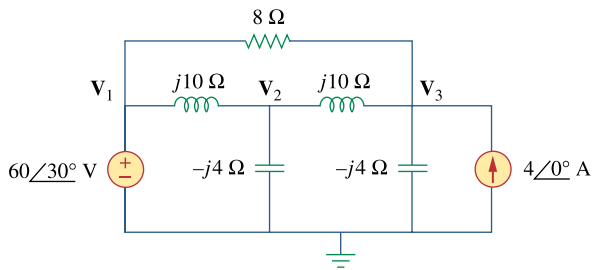


Figure 10.128
For Prob. 10.86.

Chapter 10, Solution 86.

The schematic is shown below. We insert three pseudocomponent PRINTs at nodes 1, 2, and 3 to print V_1 , V_2 , and V_3 , into the output file. Assume that $w = 1$, we set Total Pts = 1, Start Freq = 0.1592, and End Freq = 0.1592. After saving and simulating the circuit, we obtain the output file which includes:

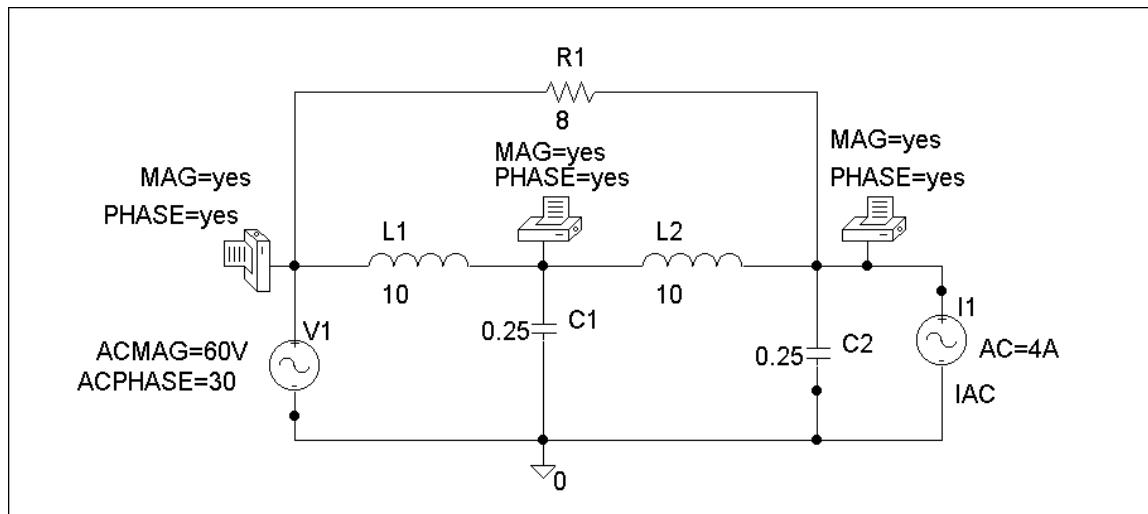
	FREQ	VM(\$N_0002)	
VP(\$N_0002)	1.592 E-01	6.000 E+01	3.000
E+01			

	FREQ	VM(\$N_0003)	
VP(\$N_0003)	1.592 E-01	2.367 E+02	-8.483
E+01			

	FREQ	VM(\$N_0001)	
VP(\$N_0001)	1.592 E-01	1.082 E+02	1.254
E+02			

Therefore,

$$V_1 = \underline{60\angle 30^\circ \text{ V}} \quad V_2 = \underline{236.7\angle -84.83^\circ \text{ V}} \quad V_3 = \underline{108.2\angle 125.4^\circ \text{ V}}$$



Chapter 10, Problem 87.

Determine V_1 , V_2 , and V_3 in the circuit of Fig. 10.129 using *PSpice*.

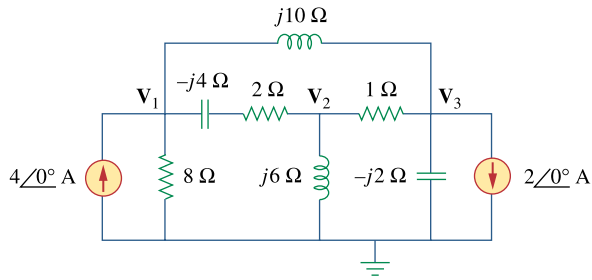


Figure 10.129
For Prob. 10.87.

Chapter 10, Solution 87.

The schematic is shown below. We insert three PRINTs at nodes 1, 2, and 3. We set Total Pts = 1, Start Freq = 0.1592, End Freq = 0.1592 in the AC Sweep box. After simulation, the output file includes:

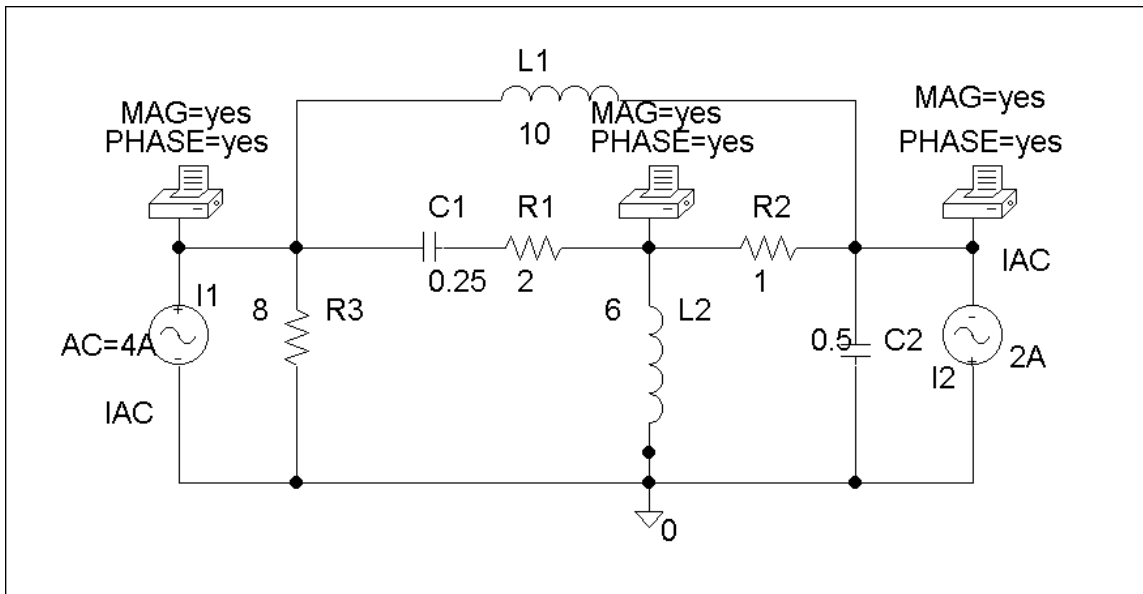
	FREQ	VM(\$N_0004)	
VP(\$N_0004)	1.592 E-01	1.591 E+01	1.696
E+02			

	FREQ	VM(\$N_0001)	
VP(\$N_0001)	1.592 E-01	5.172 E+00	-1.386
E+02			

	FREQ	VM(\$N_0003)	
VP(\$N_0003)	1.592 E-01	2.270 E+00	-1.524
E+02			

Therefore,

$$V_1 = \underline{15.91\angle 169.6^\circ \text{ V}} \quad V_2 = \underline{5.172\angle -138.6^\circ \text{ V}} \quad V_3 = \underline{2.27\angle -152.4^\circ \text{ V}}$$



Chapter 10, Problem 88.

Use *PSpice* to find v_o and i_o in the circuit of Fig. 10.130 below.

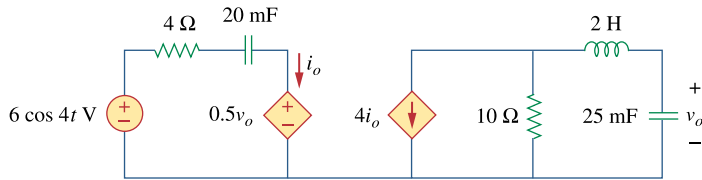


Figure 10.130
For Prob. 10.88.

Chapter 10, Solution 88.

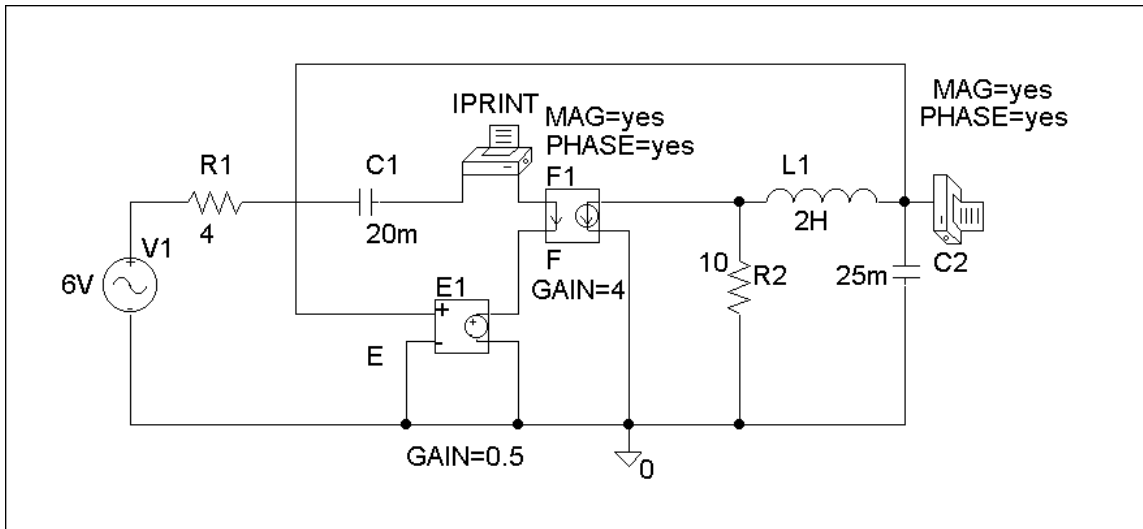
The schematic is shown below. We insert IPRINT and PRINT to print I_o and V_o in the output file. Since $\omega = 4$, $f = \omega/2\pi = 0.6366$, we set Total Pts = 1, Start Freq = 0.6366, and End Freq = 0.6366 in the AC Sweep box. After simulation, the output file includes:

VP(\$N_0002)	FREQ	VM(\$N_0002)	
	6.366 E-01	3.496 E+01	1.261
E+01			

(V_PRINT2)	FREQ	IM(V_PRINT2)	IP
	6.366 E-01	8.912 E-01	
-8.870 E+01			

Therefore, $V_o = 34.96\angle 12.6^\circ \text{ V}$, $I_o = 0.8912\angle -88.7^\circ \text{ A}$

$$v_o = \underline{34.96 \cos(4t + 12.6^\circ) \text{ V}}, \quad i_o = \underline{0.8912 \cos(4t - 88.7^\circ) \text{ A}}$$



Chapter 10, Problem 89.

The op amp circuit in Fig. 10.131 is called an *inductance simulator*. Show that the input impedance is given by

$$Z_{\text{in}} = \frac{V_{\text{in}}}{I_{\text{in}}} = j\omega L_{\text{eq}}$$

where

$$L_{\text{eq}} = \frac{R_1 R_3 R_4}{R_2} C$$

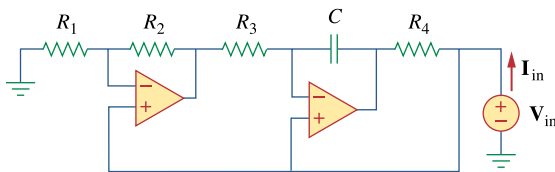
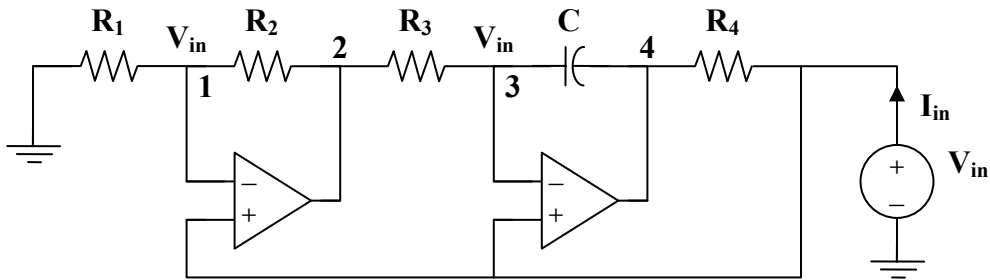


Figure 10.131
For Prob. 10.89.

Chapter 10, Solution 89.

Consider the circuit below.



At node 1,

$$\begin{aligned}\frac{0 - V_{in}}{R_1} &= \frac{V_{in} - V_2}{R_2} \\ -V_{in} + V_2 &= \frac{R_2}{R_1} V_{in}\end{aligned}\tag{1}$$

At node 3,

$$\begin{aligned}\frac{V_2 - V_{in}}{R_3} &= \frac{V_{in} - V_4}{1/j\omega C} \\ -V_{in} + V_4 &= \frac{V_{in} - V_2}{j\omega C R_3}\end{aligned}\tag{2}$$

From (1) and (2),

$$-V_{in} + V_4 = \frac{-R_2}{j\omega C R_3 R_1} V_{in}$$

Thus,

$$I_{in} = \frac{V_{in} - V_4}{R_4} = \frac{R_2}{j\omega C R_3 R_1 R_4} V_{in}$$

$$Z_{in} = \frac{V_{in}}{I_{in}} = \frac{j\omega C R_1 R_3 R_4}{R_2} = j\omega L_{eq}$$

$$\text{where } L_{eq} = \frac{R_1 R_3 R_4 C}{R_2}$$

Chapter 10, Problem 90.

Figure 10.132 shows a Wien-bridge network. Show that the frequency at which the phase shift between the input and output signals is zero is $f = \frac{1}{2\pi RC}$, and that the necessary gain is $A_v = V_o/V_i = 3$ at that frequency.

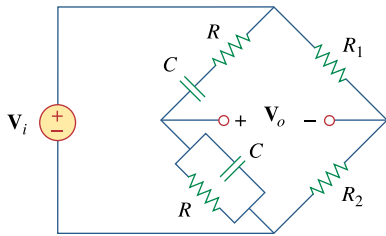


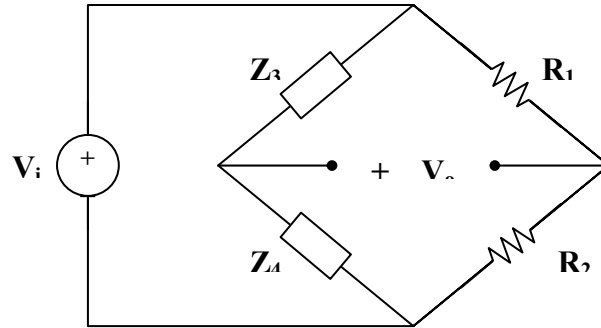
Figure 10.132
For Prob. 10.90.

Chapter 10, Solution 90.

Let
$$\mathbf{Z}_4 = R \parallel \frac{1}{j\omega C} = \frac{R}{1 + j\omega RC}$$

$$\mathbf{Z}_3 = R + \frac{1}{j\omega C} = \frac{1 + j\omega RC}{j\omega C}$$

Consider the circuit shown below.



$$\mathbf{V}_o = \frac{\mathbf{Z}_4}{\mathbf{Z}_3 + \mathbf{Z}_4} \mathbf{V}_i - \frac{R_2}{R_1 + R_2} \mathbf{V}_i$$

$$\begin{aligned} \frac{\mathbf{V}_o}{\mathbf{V}_i} &= \frac{\frac{R}{1 + j\omega C}}{\frac{R}{1 + j\omega C} + \frac{1 + j\omega RC}{j\omega C}} - \frac{R_2}{R_1 + R_2} \\ &= \frac{j\omega RC}{j\omega RC + (1 + j\omega RC)^2} - \frac{R_2}{R_1 + R_2} \end{aligned}$$

$$\frac{\mathbf{V}_o}{\mathbf{V}_i} = \frac{j\omega RC}{1 - \omega^2 R^2 C^2 + j3\omega RC} - \frac{R_2}{R_1 + R_2}$$

For $\mathbf{V}_o$ and $\mathbf{V}_i$ to be in phase, $\frac{\mathbf{V}_o}{\mathbf{V}_i}$ must be purely real. This happens when

$$1 - \omega^2 R^2 C^2 = 0$$

$$\omega = \frac{1}{RC} = 2\pi f$$

or
$$f = \frac{1}{2\pi RC}$$

At this frequency,
$$\mathbf{A}_v = \frac{\mathbf{V}_o}{\mathbf{V}_i} = \frac{1}{3} - \frac{R_2}{R_1 + R_2}$$

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Chapter 10, Problem 91.

Consider the oscillator in Fig. 10.133.

- (a) Determine the oscillation frequency.
- (b) Obtain the minimum value of R for which oscillation takes place.

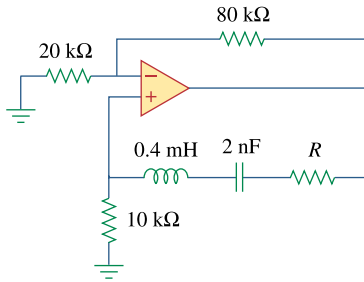


Figure 10.133
For Prob. 10.91.

Chapter 10, Solution 91.

- (a) Let V_2 = voltage at the noninverting terminal of the op amp
 V_o = output voltage of the op amp
 $Z_p = 10 \text{ k}\Omega = R_o$
 $Z_s = R + j\omega L + \frac{1}{j\omega C}$

As in Section 10.9,

$$\frac{V_2}{V_o} = \frac{Z_p}{Z_s + Z_p} = \frac{R_o}{R + R_o + j\omega L - \frac{j}{\omega C}}$$

$$\frac{V_2}{V_o} = \frac{\omega C R_o}{\omega C (R + R_o) + j(\omega^2 LC - 1)}$$

For this to be purely real,

$$\omega_o^2 LC - 1 = 0 \longrightarrow \omega_o = \frac{1}{\sqrt{LC}}$$

$$f_o = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{(0.4 \times 10^{-3})(2 \times 10^{-9})}}$$

$$f_o = \underline{\underline{180 \text{ kHz}}}$$

- (b) At oscillation,

$$\frac{V_2}{V_o} = \frac{\omega_o C R_o}{\omega_o C (R + R_o)} = \frac{R_o}{R + R_o}$$

This must be compensated for by

$$A_v = \frac{V_o}{V_2} = 1 + \frac{80}{20} = 5$$

$$\frac{R_o}{R + R_o} = \frac{1}{5} \longrightarrow R = 4R_o = \underline{\underline{40 \text{ k}\Omega}}$$

Chapter 10, Problem 92.

The oscillator circuit in Fig. 10.134 uses an ideal op amp.

- (a) Calculate the minimum value of R_o that will cause oscillation to occur.
- (b) Find the frequency of oscillation.

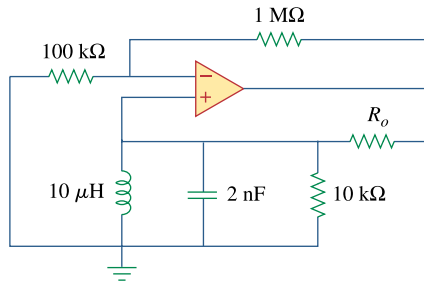


Figure 10.134
For Prob. 10.92.

Chapter 10, Solution 92.

Let V_2 = voltage at the noninverting terminal of the op amp

V_o = output voltage of the op amp

$$Z_s = R_o$$

$$Z_p = j\omega L \parallel \frac{1}{j\omega C} \parallel R = \frac{1}{\frac{1}{R} + j\omega C + \frac{1}{j\omega L}} = \frac{\omega RL}{\omega L + jR(\omega^2 LC - 1)}$$

As in Section 10.9,

$$\frac{V_2}{V_o} = \frac{Z_p}{Z_s + Z_p} = \frac{\frac{\omega RL}{\omega L + jR(\omega^2 LC - 1)}}{R_o + \frac{\omega RL}{\omega L + jR(\omega^2 LC - 1)}}$$

$$\frac{V_2}{V_o} = \frac{\omega RL}{\omega RL + \omega R_o L + jR_o R(\omega^2 LC - 1)}$$

For this to be purely real,

$$\omega_o^2 LC = 1 \longrightarrow f_o = \frac{1}{2\pi\sqrt{LC}}$$

(a) At $\omega = \omega_o$,

$$\frac{V_2}{V_o} = \frac{\omega_o RL}{\omega_o RL + \omega_o R_o L} = \frac{R}{R + R_o}$$

This must be compensated for by

$$A_v = \frac{V_o}{V_2} = 1 + \frac{R_f}{R_o} = 1 + \frac{1000k}{100k} = 11$$

Hence,

$$\frac{R}{R + R_o} = \frac{1}{11} \longrightarrow R_o = 10R = \underline{\underline{100 \text{ k}\Omega}}$$

$$(b) \quad f_o = \frac{1}{2\pi\sqrt{(10 \times 10^{-6})(2 \times 10^{-9})}}$$

$$f_o = \underline{\underline{1.125 \text{ MHz}}}$$

Chapter 10, Problem 93.

ed

Figure 10.135 shows a *Colpitts oscillator*. Show that the oscillation frequency is

$$f_o = \frac{1}{2\pi\sqrt{LC_T}}$$

where $C_T = C_1 C_2 / (C_1 + C_2)$. Assume $R_i \gg X_{C_2}$

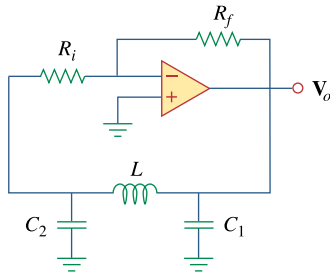


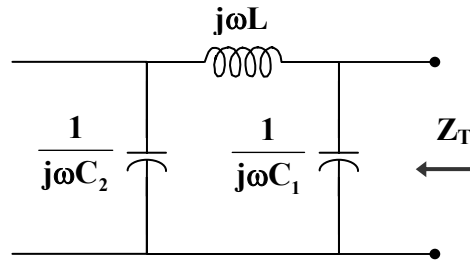
Figure 10.135

A Colpitts oscillator; for Prob. 10.93.

(Hint: Set the imaginary part of the impedance in the feedback circuit equal to zero.)

Chapter 10, Solution 93.

As shown below, the impedance of the feedback is



$$Z_T = \frac{1}{j\omega C_1} \parallel \left(j\omega L + \frac{1}{j\omega C_2} \right)$$

$$Z_T = \frac{\frac{-j}{\omega C_1} \left(j\omega L + \frac{-j}{\omega C_2} \right)}{\frac{-j}{\omega C_1} + j\omega L + \frac{-j}{\omega C_2}} = \frac{\frac{1}{\omega} - \omega L C_2}{j(C_1 + C_2 - \omega^2 L C_1 C_2)}$$

In order for Z_T to be real, the imaginary term must be zero; i.e.

$$C_1 + C_2 - \omega_0^2 L C_1 C_2 = 0$$

$$\omega_0^2 = \frac{C_1 + C_2}{L C_1 C_2} = \frac{1}{L C_T}$$

$$f_0 = \frac{1}{2\pi\sqrt{L C_T}}$$

Chapter 10, Problem 94.

ed

Design a Colpitts oscillator that will operate at 50 kHz.

Chapter 10, Solution 94.

If we select $C_1 = C_2 = 20 \text{ nF}$

$$C_T = \frac{C_1 C_2}{C_1 + C_2} = \frac{C_1}{2} = 10 \text{ nF}$$

Since $f_o = \frac{1}{2\pi\sqrt{LC_T}}$,

$$L = \frac{1}{(2\pi f)^2 C_T} = \frac{1}{(4\pi^2)(2500 \times 10^6)(10 \times 10^{-9})} = 10.13 \text{ mH}$$

$$X_c = \frac{1}{\omega C_2} = \frac{1}{(2\pi)(50 \times 10^3)(20 \times 10^{-9})} = 159 \Omega$$

We may select $R_i = 20 \text{ k}\Omega$ and $R_f \geq R_i$, say $R_f = 20 \text{ k}\Omega$.

Thus,

$$C_1 = C_2 = \underline{20 \text{ nF}}, \quad L = \underline{10.13 \text{ mH}} \quad R_f = R_i = \underline{20 \text{ k}\Omega}$$

Chapter 10, Problem 95.

Figure 10.136 shows a *Hartley oscillator*. Show that the frequency of oscillation is

$$f_o = \frac{1}{2\pi\sqrt{C(L_1 + L_2)}}$$

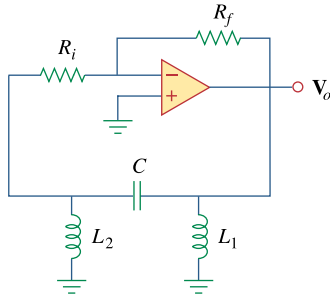
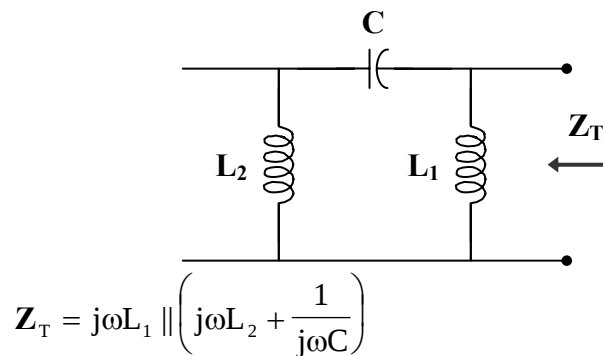


Figure 10.136

A Hartley oscillator; For Prob. 10.95.

Chapter 10, Solution 95.

First, we find the feedback impedance.



$$Z_T = \frac{j\omega L_1 \left(j\omega L_2 - \frac{j}{\omega C} \right)}{j\omega L_1 + j\omega L_2 - \frac{j}{\omega C}} = \frac{\omega^2 L_1 C (1 - \omega L_2)}{j(\omega^2 C (L_1 + L_2) - 1)}$$

In order for Z_T to be real, the imaginary term must be zero; i.e.

$$\omega_o^2 C (L_1 + L_2) - 1 = 0$$

$$\omega_o = 2\pi f_o = \frac{1}{C(L_1 + L_2)}$$

$$f_o = \frac{1}{2\pi\sqrt{C(L_1 + L_2)}}$$

Chapter 10, Problem 96.

Refer to the oscillator in Fig. 10.137.

(a) Show that

$$\frac{V_2}{V_o} = \frac{1}{3 + j(\omega L / R - R / \omega L)}$$

(b) Determine the oscillation frequency f_o .

(c) Obtain the relationship between R_1 and R_2 in order for oscillation to occur.

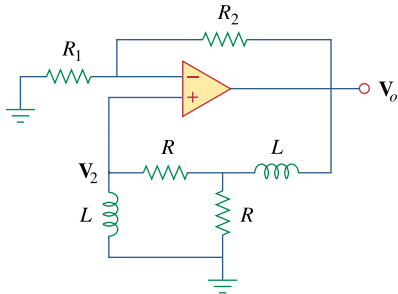
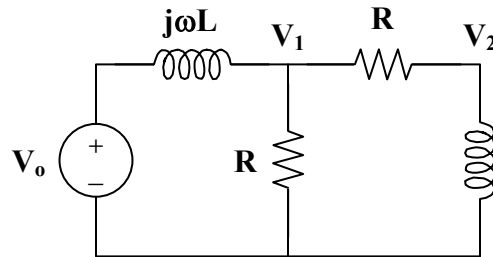


Figure 10.137
For Prob. 10.96.

Chapter 10, Solution 96.

- (a) Consider the feedback portion of the circuit, as shown below.



$$V_2 = \frac{j\omega L}{R + j\omega L} V_1 \longrightarrow V_1 = \frac{R + j\omega L}{j\omega L} V_2 \quad (1)$$

Applying KCL at node 1,

$$\frac{V_o - V_1}{j\omega L} = \frac{V_1}{R} + \frac{V_1}{R + j\omega L}$$

$$V_o - V_1 = j\omega L V_1 \left(\frac{1}{R} + \frac{1}{R + j\omega L} \right)$$

$$V_o = V_1 \left(1 + \frac{j2\omega RL - \omega^2 L^2}{R(R + j\omega L)} \right)$$

(2)

From (1) and (2),

$$V_o = \left(\frac{R + j\omega L}{j\omega L} \right) \left(1 + \frac{j2\omega RL - \omega^2 L^2}{R(R + j\omega L)} \right) V_2$$

$$\frac{V_o}{V_2} = \frac{R^2 + j\omega RL + j2\omega RL - \omega^2 L^2}{j\omega RL}$$

$$\frac{V_2}{V_o} = \frac{1}{3 + \frac{R^2 - \omega^2 L^2}{j\omega RL}}$$

$$\frac{V_2}{V_o} = \frac{1}{3 + j(\omega L/R - R/\omega L)}$$

(b) Since the ratio $\frac{V_2}{V_o}$ must be real,

$$\frac{\omega_o L}{R} - \frac{R}{\omega_o L} = 0$$

$$\omega_o L = \frac{R^2}{\omega_o L}$$

$$\omega_o = 2\pi f_o = \frac{R}{L}$$

$$\underline{f_o = \frac{R}{2\pi L}}$$

(c) When $\omega = \omega_o$

$$\frac{V_2}{V_o} = \frac{1}{3}$$

This must be compensated for by $A_v = 3$. But

$$A_v = 1 + \frac{R_2}{R_1} = 3$$

$$\underline{R_2 = 2R_1}$$